## Quantum field theory Exercises 5.

2005-11-28

## • Exercise 5.1.

Find the center-of-mass energy for scattering of a high energy proton with energy E (and mass  $M=1~{\rm GeV}$ ) on the CMB photon (average temperature  $T=2.7{\rm K}^{\circ}$ ). Compare the kinetic energy with the mass of  $\pi^0$ ,  $m_{\pi^0}=135~{\rm MeV}$ .

## • Exercise 5.2.

Check the formulas

$$\begin{split} \sigma^{\mu}\bar{\sigma}^{\nu} + \sigma^{\nu}\bar{\sigma}^{\mu} &= 2g^{\mu\nu}\mathbb{1} \\ \bar{\sigma}^{\mu}\sigma^{\nu} + \bar{\sigma}^{\nu}\sigma^{\mu} &= 2g^{\mu\nu}\mathbb{1} \\ \operatorname{tr}\sigma^{\mu}\bar{\sigma}^{\nu} &= 2g^{\mu\nu}\,. \end{split}$$