

# *Measuring Systemic Risk*

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## *Systemic Risk: Motivation*

- Systemic risk can be defined as:
  - Joint distress of several financial institutions with externalities that disrupt the real economy
  
- Systemic risk is very costly
  - Bailout costs
    - Bank credit risk leads to sovereign credit risk
  - Impact on the real economy
    - GDP
    - Unemployment
    - World trade
  - Financial institutions fail to internalize externalities

## *Systemic Risk: Way Forward*

- Systemic risk must be measured to be managed
  - Overall systemic risk:
  - Each institution's contribution to systemic risk
  
- Once measured, financial institutions must be incentivized to
  - Internalize expected costs
  - Reduce risk taking and increase capital / reduce leverage
  - Consider interconnections
  
- The challenges are:
  - to use economic theory to find a measure of systemic risk
  - that is useful in managing it
  - and assess its empirical success

# What are Systemic Risk and Systemic Risk Contributions?

## ➤ Conventional wisdom:

Systemic risk (contribution) =

- what would happen if bank X failed?
- or, what crucial infrastructure is operated by bank X? (triparty repo, payment system, etc.)

## ➤ Our view:

Systemic risk =

- Too little aggregate capital in the financial system
  - Too little capital inhibits intermediation and credit provision
  - A failed bank with crucial infrastructure can be taken over if there is enough capital in the system
  - Example: Lehman vs. Barings

Systemic risk contribution =

- A financial institution's capital shortfall when the aggregate capital in the system is too

## *Our Results: Insights from Economic Theory*

- Each financial institution's *contribution* to systemic crisis can measured as its systemic expected shortfall (SES):
  - SES = expected capital shortfall, conditional on a future crisis
  
- A financial institution's SES increases in:
  - its own leverage and risk
  - the system's leverage and risk
  - the tail dependence between the institution and the system
  - the severity of the externality from a systemic crisis
  
- Managing systemic risk:
  - Incentives can be aligned by imposing
    - Systemic capital requirements
    - Systemic risk fee, and/or
    - Mandatory insurance scheme against systemic losses

## Measuring Systemic Risk: The Right Units for a Systemic Tax

- How to regulate based on the systemic risk measure?
  - We show that taxing based on SES implies that banks internalize externalities
  - Taxing based on “crucial infrastructure” does not work since infrastructure crucial no matter how well capitalized
- In case of tax, how to translate into right units?
  - We show that SES is scaled in meaningful units
- How to scale wrt. size of institution? Example, consider these three firms:
  - Firm A = Citibank
  - Firm B = 1 share of Citibank
  - Firm C = 1 share of Citibank + \$1 Trillion worth of Treasuries
  - We show that SES taxes each correctly
  - Other measure of systemic risk (e.g. based on “connections”) get this wrong
    - Same tax in dollars for A and B, or
    - Way higher tax for C than B
- How to handle if institutions merge or split up?
  - We show that SES handles this immediately

## *Our Results: Empirical Implementation*

- Empirical methodology:
  - we provide a very simple way of estimating SES
- SES in the cross-section:
  - higher for securities dealers and brokers – every year 1963-2008
  - higher for larger institutions that tend to be more levered
- Institutions' ex-ante SESs
  - predict their losses during the subprime crisis
  - with more explanatory power than measures of idiosyncratic risk
  - works with equity and CDS
  - predict the outcome of the stress tests
- SES in the time series:
  - higher during periods of macroeconomic stress, especially for securities dealers and brokers

## Managing risk within and across banks

➤ Standard measures of risk within banks:

- Value at risk:  $Pr ( R \leq - VaR ) = \alpha$
- Expected shortfall:  $ES = - E( R / R \leq - VaR )$

➤ Banks consists of several units  $i=1, \dots, I$  of size  $y_i$  :

- Return of bank is:  $R = \sum_i y_i r_i$
- Expected shortfall:  $ES = - \sum_i y_i E( r_i / R \leq - VaR )$

➤ Risk contribution of unit  $i$ : Marginal expected shortfall (MES)

$$MES^i := \frac{\partial ES}{\partial y_i} = -E[r_i | R \leq -VaR]$$

- We can re-interpret this as each bank's contributions to the risk of overall banking system:  
The loss of bank  $i$  when overall banking is in trouble
- We develop an economic theory that extends these ideas



# Economic model

- Many banks  $i=1, \dots, N$  and two dates
- Time 0: Choice of investments & leverage
  - Each bank has given initial level of capital  $w_{i,0}$
  - Issue debt  $b_i$  at face value  $f_i$  : a fraction  $\alpha_i$  can be insured by govt
  - Assets:  $a_i = w_{i,0} + b_i$
  - Allocate investments among  $j=1 \dots J$  risky assets and cash
- Time 1: Returns are realized
  - Limited liability if insolvent, but government bails out insured depositors

Pre-distress income

cost of financial distress

net worth

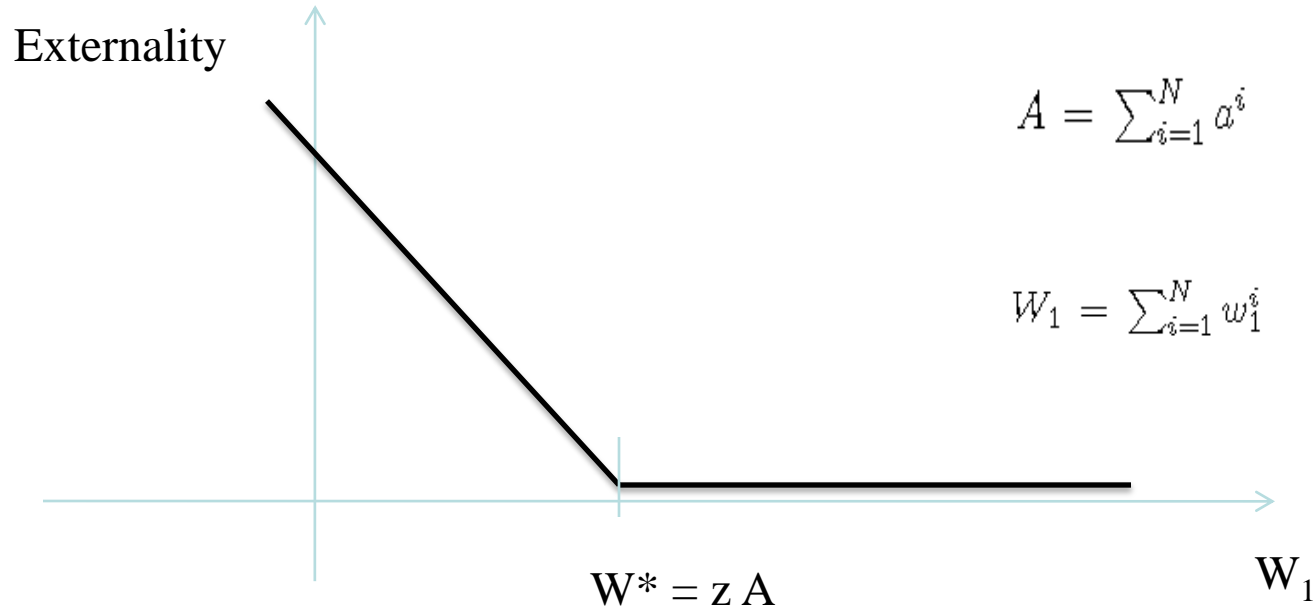
$$\hat{y}^i = \sum_{j=1}^J r_j^i x_j^i$$

$$\phi^i = \Phi(\hat{y}^i, f^i)$$

$$w_1^i = \hat{y}^i - \phi^i - f^i$$

# Externality

- $W_1$  be aggregate net worth of financial system at time 1
- Systemic distress happens if  $W_1$  falls below a cutoff  $W^*=zA$
- Imposes negative externality  $e(W^*-W_1)$  on economy
  - Extension:
    - Institutions run crucial infrastructure
    - Endogenous merger market
    - Low aggregate capital ~ failures and inability of other institutions to take over



## Objective functions

- Each bank:

$$\max_{w_0^i, b^i, \{a_j^i\}_j} c \cdot (\bar{w}_0^i - w_0^i - \tau^i) + E \left( u \left( 1_{[w_1^i > 0]} \cdot w_1^i \right) \right)$$

- Tax  $\tau_i$  is set by the planner whose objective is to maximize  
P1 + P2 + P3 :

$$P^1 = \sum_{i=1}^N c \cdot (\bar{w}_0^i - w_0^i - \tau^i) + E \left[ \sum_{i=1}^N u^i \left( 1_{[w_1^i > 0]} \cdot w_1^i \right) \right]$$

$$P^2 = E \left[ g \sum_{i=1}^N 1_{[w_1^i < 0]} \alpha^i w_1^i \right]$$

$$P^3 = E \left[ e \cdot 1_{[W_1 < zA]} \cdot (zA - W_1) \right]$$

## *Economic model - results*

- Without government intervention,
  - Banks choose leverage level and exposures  $x=(x_I, \dots, x_S)$  with a risk level higher than socially optimal.
- To correct this, government could charge a tax based on two components:

$$ES^i \equiv -E[w_1^i | w_1^i < 0] \quad SES^i \equiv E[za^i - w_1^i | W_1 < zA]$$

$$\tau^i = \frac{\alpha^i g}{c} \cdot Pr(w_1^i < 0) \cdot ES^i + \frac{e}{c} \cdot Pr(W_1 < zA) \cdot SES^i.$$

- In our model, these are sufficient metrics of systemic risk contributions available to design optimal taxation (a normative benchmark)

## *Efficient regulation*

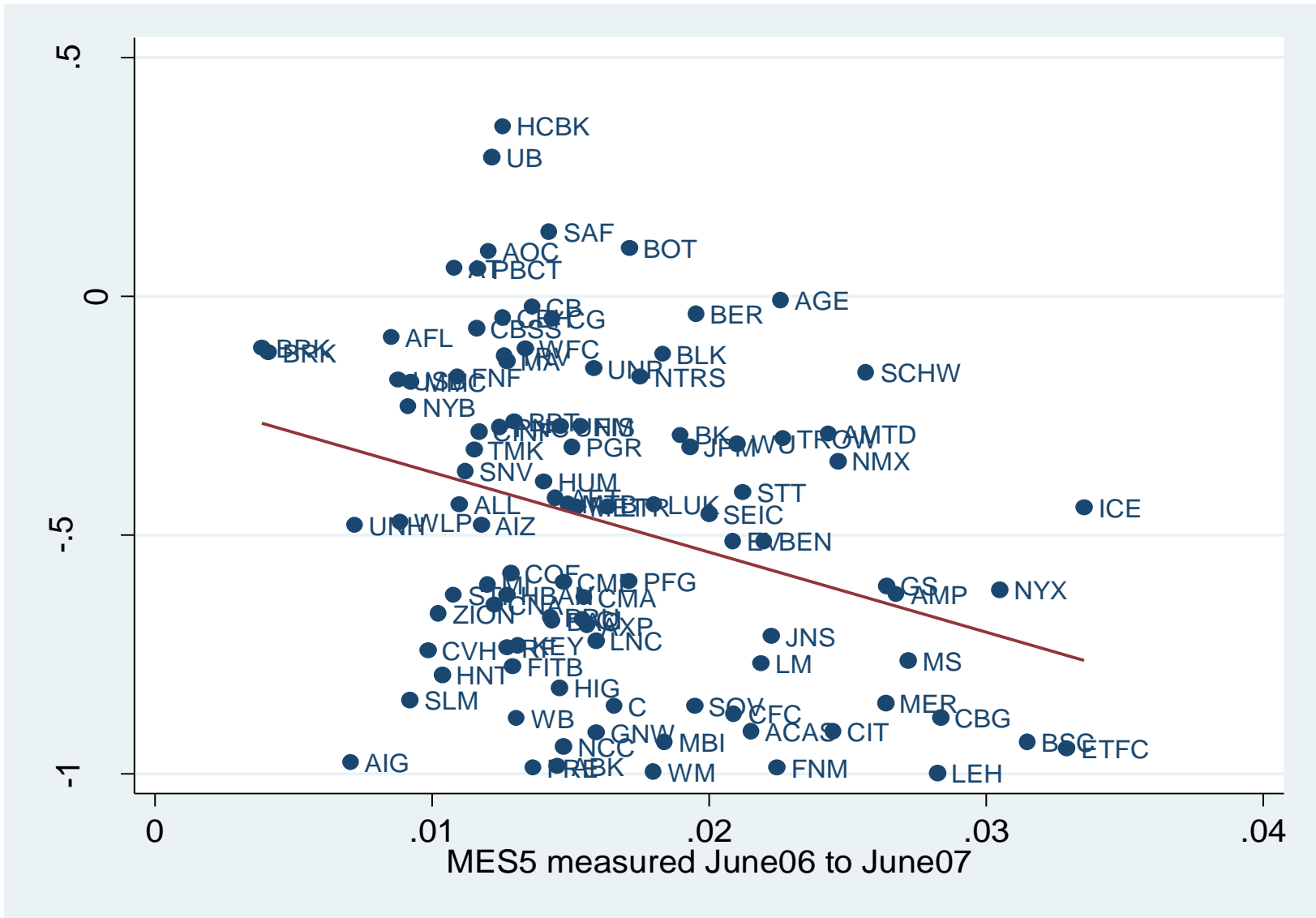
- Tax system with two components
- Default Expected Shortfall (DES):
  - *The bank's expected losses upon default*
  - Analogous to the FDIC insurance premium.
  - Justified by government guarantees on deposits and related cost (g).
- Systemic Expected Shortfall (SES):
  - *The bank's expected losses in a crisis*
  - Expected contribution of bank to the aggregate shortfall of capital during a crisis.
  - Justified by the externality (e).

## *Systemic Expected Shortfall*

- A bank's SES is larger if
  - the externality is more severe ( $e$ ),
  - systemic under-capitalization is more likely ( $Pr[W_I < W^*]$ )
  - the bank takes a larger exposure ( $x_s$ ) in an asset  $s$  that experiences losses when other banks are in trouble
  - the bank is more leveraged ( $w_0$ )
- In our empirical work, we focus on the cross-sectional part of SES, taking as given (i) the size of externality or the level of tax; (ii) the likelihood of systemic crisis, the time-series part

- MES:
  - Very simple non-parametric estimation:
    - find the 5% worst days for the market
    - compute each institution's return on these days
  - Parametric
- SES:
  - Consider both MES and Leverage
- Data: CRSP and COMPUSTAT
- Tests
  - Stock returns during July 2007- Dec 2008
  - CDS changes during July 2007- Dec 2008
  - First set of stress tests

# 2007-08: Predictive power of MES (Equity)

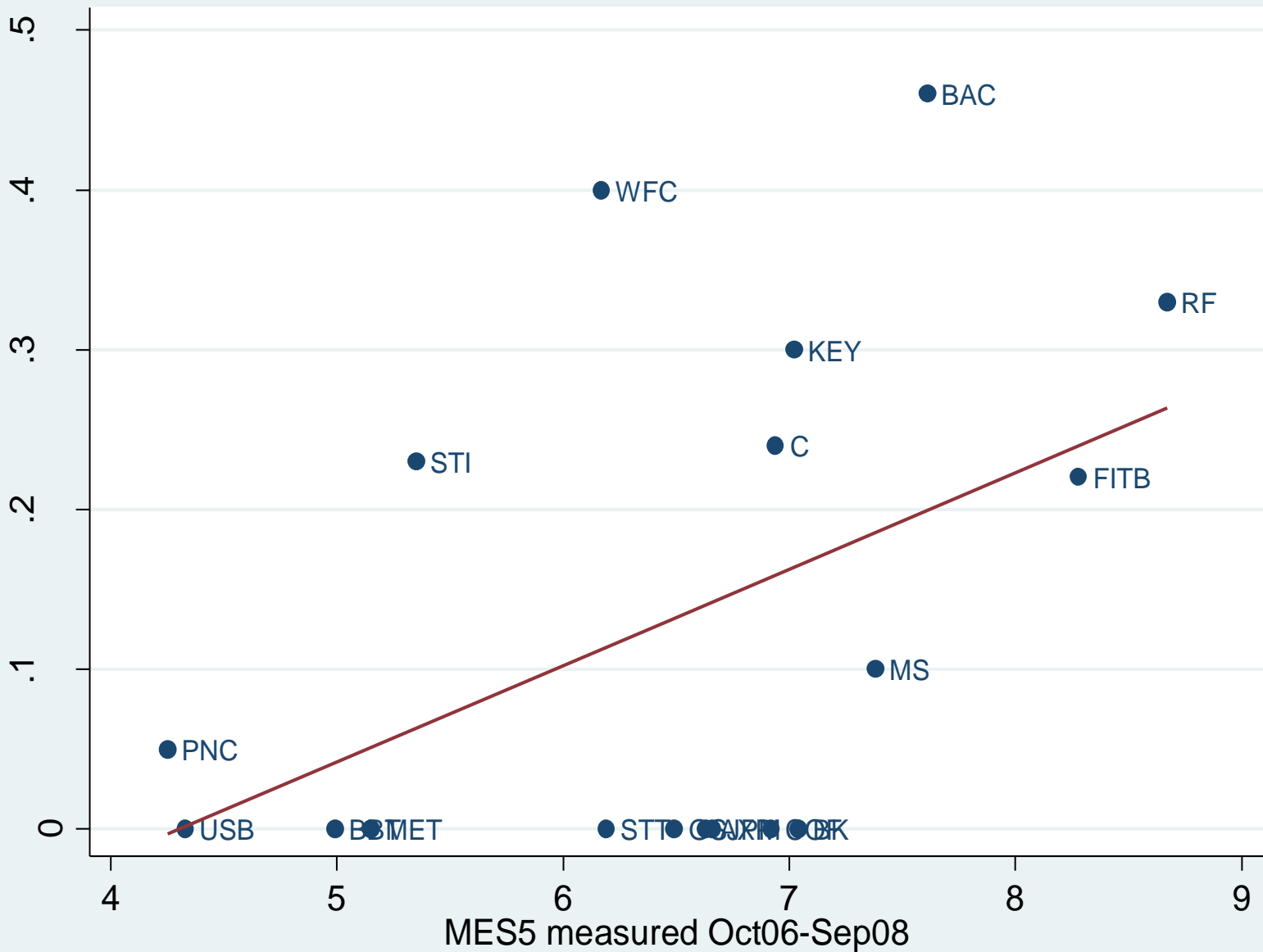




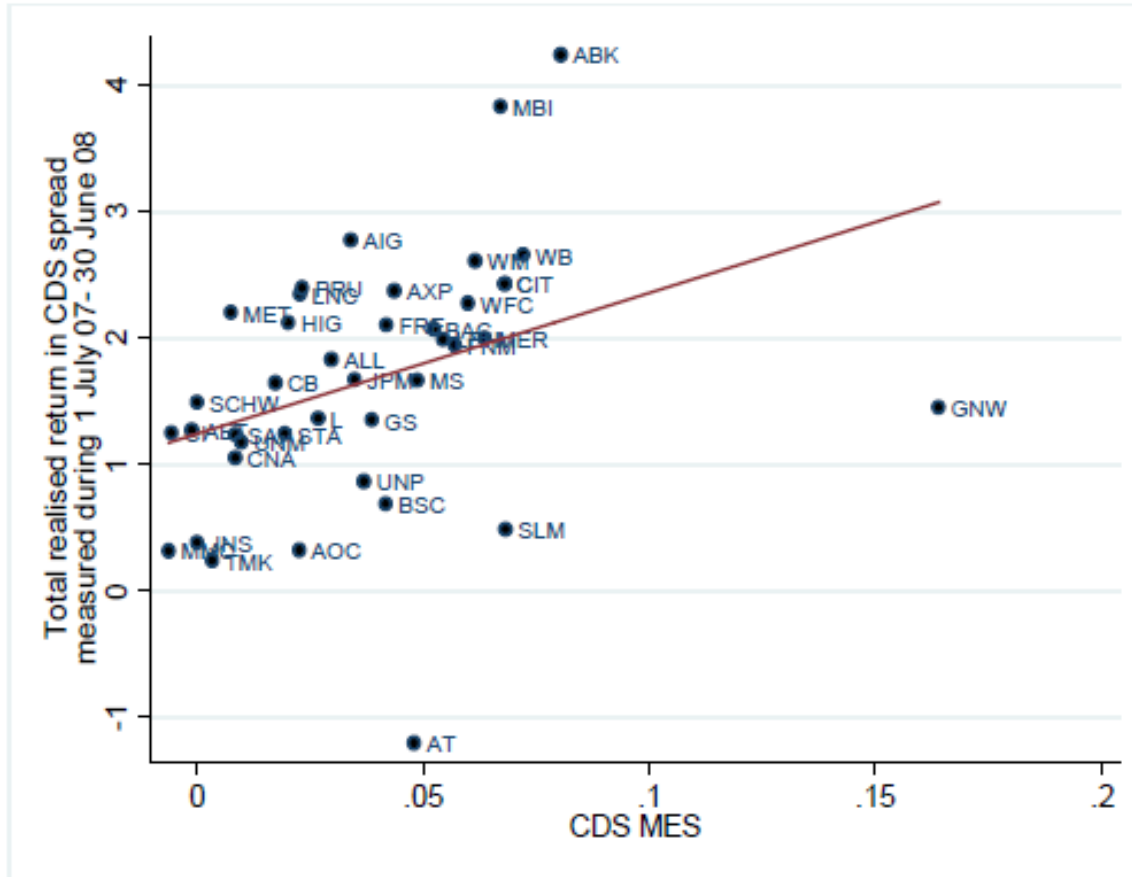
## 2007-08: Predictive power of MES (Equity)

Panel A, OLS regression analysis: The dependent variable is Realized SES, the company stock returns during the crisis								
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
ES	-0.05 (-1.14)							
Vol		0.04 (0.07)						-0.07 (-0.12)
MES			-0.21*** (-2.90)			-0.15** (-2.25)		-0.17** (-2.08)
Beta				-0.29** (-2.24)				
LVG					-0.04*** (-5.73)	-0.04*** (-5.43)		-0.03** (-2.29)
Log Assets							-0.09*** (-4.86)	-0.05* (-1.69)
<b>Industry dummies</b>								
Constant	-0.32*** (-2.71)	-0.44*** (-3.81)	-0.13 (-1.09)	-0.18 (-1.42)	-0.18** (-2.50)	0.02 (0.20)	0.61*** (2.75)	0.50 (1.61)
Other	-0.04 (-0.33)	-0.09 (-0.91)	0.01 (0.14)	0.012 (0.12)	-0.20** (-2.44)	-0.12 (-1.35)	-0.25*** (-2.87)	-0.15 (-1.61)
Insurance(x100)	0.43 (0.05)	-0.68 (-0.08)	-3.63 (-0.45)	-2.95 (-0.36)	-8.86 (-1.19)	-10.17 (-1.39)	-0.09 (-1.13)	-0.11 (-1.55)
Broker-dealers	-0.09 (-0.65)	-0.16 (-1.20)	0.11 (0.71)	0.06 (0.36)	-0.02 (-0.18)	0.16 (1.19)	-0.17 (-1.56)	0.14 (1.02)
Adj. R <sup>2</sup>	0%	-1.36%	6.72%	3.62%	24.27%	27.34%	18.46%	28.02%
No. Obs	102	102	102	102	101	101	101	101

## Stress tests: Predictive Power of MES (Equity)



## 2007-08: Predictive Power of MES (CDS)

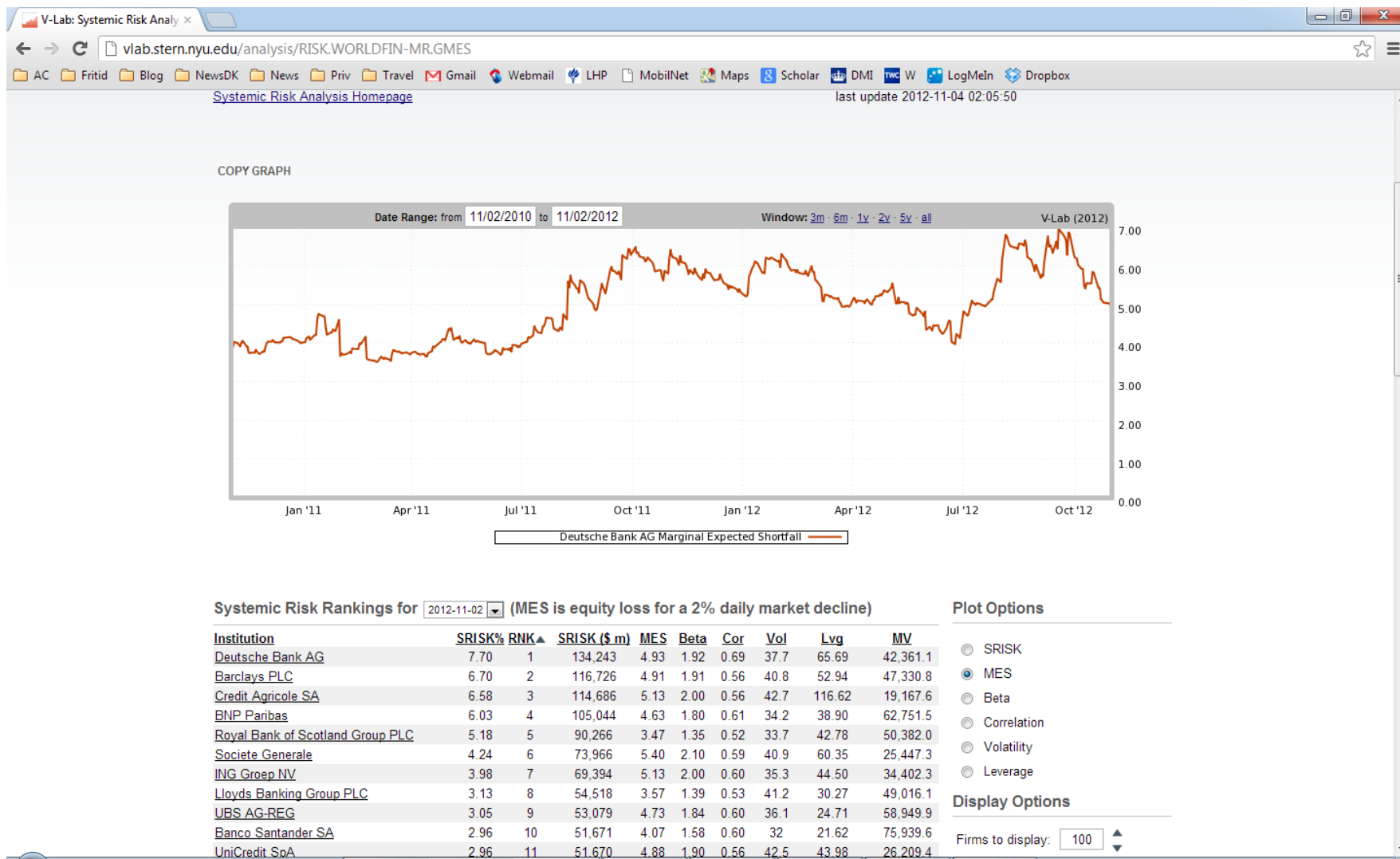


## *NYU-Stern VLAB'S Risk Page*

- Directed by Rob Engle
- We have introduced a page providing estimates of risk for the largest US and global financial firms
- *NYU Stern Systemic Risk Ranking*: Risk is estimated both for the firm itself and for its contribution to risk in the system.
- This is updated weekly/daily to allow regulators, practitioners and academics to see early warnings of system risks.
- Extended to global firms: Collaboration with Universite de Lausanne and Australian Graduate School in Sydney



# NYU-Stern VLAB'S Risk Page



## *Implementation: Our proposal*

- SES signals institutions likely to contribute to aggregate crises
  
- Three ways to implement our proposal
  1. Systemic Capital Requirement
    - Capital requirement proportional to estimated systemic risk
  2. Systemic Fees (FDIC-style)
    - Fees proportional to estimated systemic risk
    - Create systemic fund
  3. Private/public systemic insurance
    - Compulsory insurance against own losses during crisis
    - Payment goes to systemic fund, not the bank itself
    - Insurance from government, prices from the market
      - Say 5 cents from private; 95 cents from the government
      - Analogy to terrorism reinsurance by the government (TRIA, 2002)
      - A market-based estimate of the contribution to crises and externalities
        - » Private sector has incentives to be forward looking
  
- Gives bank an incentive to be less systemic and more transparent:
  - To lower capital requirements/ fees/ insurance payments

## Conclusion: Systemic Risk

- Economic model of systemic risk gives rise to SES
  - *How under-capitalized is a particular institution expected to be if the overall system becomes under-capitalized?*
- Systemic expected shortfall (SES)
  - Measures each financial institution's *contribution* to systemic crisis
  - Increases in: leverage, risk, comovement, tail dependence
  - An SES tax/insurance incentivizes banks to contribute less to crisis
- Empirically
  - Ex ante SES predicts ex post crisis losses
  - We analyze its cross-sectional and time series properties

## *Two Approaches to Regulation*

- Traditional approach: Firm-level risk management
  - Goal: Limit risk of collapse of each bank seen in isolation
  - Requirement: Detailed knowledge of activities inside the firm
  
- We advocate in addition: Systemic approach
  - Goal: Limit risk of collapse of the system
  - Requirement: Understand risks and externalities across firms