Pierre Collin-Dufresne GSAM-QIS

NBER - July 2007

Outline	Summary O	CDS/CDX Market 000000	CDO Market 00000	Credit Spread Puzzle	The model	The story	Final Thoughts

- Summary
- CDS/CDX Market
- CDO Market
- Credit Spread Puzzle
- The model
- The story
- Final Thoughts

Summary

Outline

- Propose simple story for large growth in structured product markets (specifically pooling and tranching):
 - ▶ Posit that ratings are sufficient statistic for expected loss.
 - ▶ Tranching process pools risky securities (e.g., BBB) to create lower risk (e.g., AAA) and higher risk (e.g., Z) securities by creating different levels of subordination (tranches).
 - ▶ By nature of that process senior tranches have more systematic risk and therefore should have higher expected return for given expected loss (~ rating).
 - ightharpoonup However investors care only about expected loss (\sim rating).
- ⇒ Effectively, the banking sector exploits the "stupidity" of investors by manufacturing portfolios with same expected loss but different systematic risk and selling them at identical prices.
 - ▶ Provide evidence for their story using CDX.IG synthetic tranche prices:
 - Use a simple pricing model for tranches based on the one-factor Gaussian copula market standard.
 - Instead of assuming that the common factor has a Gaussian density (as in the market model), the authors extract its density from long-term S&P500 option prices.
 - ► Their results suggest that observed market spreads on all mezzanine and senior tranches are substantially lower than model-implied 'fair' spreads.

 Summary
 CDS/CDX Market
 CDO Market
 Credit Spread Puzzle
 The model
 The story
 Final Thoughts

 O
 ●00000
 00000
 000
 00
 00
 00

Credit markets characterized by rapid financial innovation

- Innovation in contracts,
 - from traditional funded securities: corporate bonds
 - to new unfunded derivatives: credit default swaps (CDS)
- And increased liquidity,
- Allow investors to express views on:
 - Single-names CDS
 - Baskets of names (CDX.IG, CDX.HV, iTraxx)
 - ► Correlation (Synthetic liquid CDO, Bespoke CDO, CDO²...)
 - Emerging Market Countries (EMCDS)
 - Basket of Countries (EMCDX)
 - Asset Backed Securities such as credit card receivables or Home equity loans (ABS-CDS)
 - Baskets of Asset Backed Securities (ABX)
 - ► Correlation (TABX)
 - Senior secured Loans (LCDS)
 - ► Basket of Loans (LCDX)

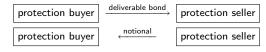
CDS Contract Structure

▶ A CDS is an insurance contract against a credit event of Counterparty:

Prior to credit event:



Upon arrival of credit event:



Definition of credit event:

Bankruptcy
Failure to pay
Obligation acceleration or default
Repudiation/moratorium
Restructuring (Full R, Mod R, ModMod R, No R)

Arbitrage Relation

- lacktriangle Buy XYZ bond + Buy XYZ protection \sim Earn risk-free rate
- lacktriangle Buy risk-free bond + Sell XYZ protection \sim Earn XYZ bond yield

CDS spread
$$\approx Y_{XYZ} - R_f$$

- ⇒ CDS allows pure unfunded play on credit risk.
- ▶ Empirical evidence on Basis = CDS spread $-(Y_{XYZ} R_f)$.

	Basis	wrt Tsy (bp)	Basis wr	t Swap (bp)	implied R_f/Tsy		
	Mean	S.E. (of mean)	Mean	S.E.	Mean	S.E.	
- Aaa/Aa	-51.30	1.97	9.55	1.31	0.834	0.0250	
Α	-64.33	1.82	5.83	1.59	0.927	0.0229	
Baa	-84.93	3.63	2.21	2.79	0.967	0.0364	
All Categories	-62.87	1.38	6.51	1.06	0.904	0.0160	

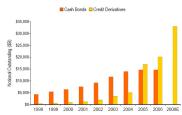
source: Hull, Pedrescu, White (2006)

 Summary
 CDS/CDX Market
 CDO Market
 Credit Spread Puzzle
 The model
 The story
 Final Thoughts

 0
 000●00
 0000
 000
 00
 00
 00
 00

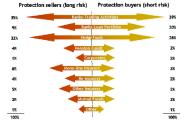
CDS Market Statistics

Exhibit 1.1: The notional amount of credit derivatives globally is larger than the global amount of debt outstanding



Sources: British Bankers' Association Credit Derivatives Report 2006, Bank for International Settlements and ISDA. Note: Cash bonds through June 2006.

Exhibit 7.1: Participants in the credit derivatives market. Some favor one direction over the other.



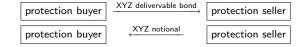
Source: British Bankers' Association Credit Derivatives Report 2006.

The CDX index

- The CDX index is an insurance contract against credit events of a portfolio of counterparties (e.g., 125 names in CDX.IG):
 - Prior to credit event:

 $\boxed{ \text{protection buyer} } \xrightarrow[\text{outstanding notional} \times \text{spread}]{} \boxed{ \text{protection seller} }$

Upon arrival of credit event of XYZ:



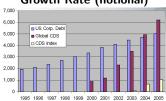
- ▶ Following credit event outstanding notional is reduced by notional of XYZ in portfolio (i.e., $\frac{1}{125}$ in CDX.IG).
- ▶ Contract expires at maturity or when notional exhausted.
- ▶ N.B.: CDX contract \neq equally weighted portfolio of single name CDS contracts CDX spread \neq average of single name CDS spreads

 Summary
 CDS/CDX Market
 CDO Market
 Credit Spread Puzzle
 The model
 The story
 Final Thoughts

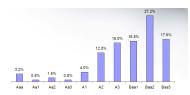
 0
 00000
 00000
 00
 00
 00
 00

CDX Market Statistics

Growth Rate (notional)

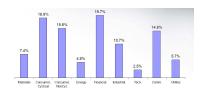


CDX.IG Moody's Ratings

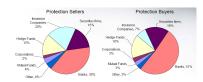


source: BBA & White (2006)

Industry Composition of CDX.IG



End Users



Synthetic CDO Tranches

- Selling protection on CDO tranche with attachment points [L, U] (i.e., notional = U L) written on underlying basket of 125 single names (CDX):
 - Prior to a credit event:

▶ Upon arrival of credit event (LGD = notional - deliverable bond price), if cumulative loss exceeds lower attachment point (i.e., $\mathcal{L}_t = \sum_{i=1}^{125} LGD_i \mathbf{1}_{\{\tau_i \leq t\}} > L$) then

 $protection \ buyer \ | \ \stackrel{min(\mathit{LGD}, outstanding \ notional)}{\longleftarrow} \ [\ protection \ seller \]$

- Following credit event outstanding tranche notional is reduced by LGD (up to exhaustion of outstanding notional).
- Also, super senior tranche notional is reduced by recovery (to satisfy 'adding up constraint').
- Contract expires at maturity or when tranche notional is exhausted.
- ▶ Tranche payoff is call spread on cumulative loss: $\max(\mathcal{L}_t L, 0) \max(\mathcal{L}_t U, 0)$.
- ⇒ Tranche valuation depends on entire distribution of cumulative portfolio losses and crucially on default event correlation model.

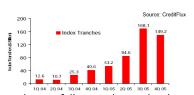
 Summary
 CDS/CDX Market
 CD0 Market
 Credit Spread Puzzle
 The model
 The story
 Final Thoughts

 0
 000000
 00000
 000
 00
 00
 00

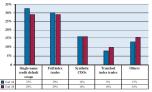
Market Size

Outline

▶ Liquid tranche market is growing steadily







Credit Derivatives Products

- Bespoke portfolio tranche market is much larger (ten times?) than synthetic tranche market:
 - Investors sell or buy protection on a portfolio of specific names for speculative or hedging motives.
 - ▶ Dealers take the other side and turn to the synthetic tranche market to hedge their resulting net exposure (keep some basis risk).
 - Hedge funds and other dealers participate in synthetic tranche market to redistribute risks.

Market Model: Implied Gaussian Copula Correlation

- Market standard for quoting CDO tranche prices is the implied correlation of the Gaussian Copula framework.
- Intuition builds on structural model of default (CDO model due to Vasicek 1987 who combines Merton (1974) with CAPM idea):
 - Each name in basket characterized by an 'asset value' driven by two factors: a common market factor and an idiosyncratic factor $(V_i = \sqrt{\rho_i} \ M + \sqrt{1-\rho_i} \ \epsilon_i$ with M, ϵ_i independent centered Gaussian).
 - ▶ Pairwise 'asset correlation' is the product of the individual asset betas $(\sqrt{\rho_i \rho_j})$.
 - lacktriangle Default occurs when asset value falls below a constant barrier (DefProb = $P(V_i \leq B_i)$).
- ▶ Market convention for quoting tranche values in terms of *implied correlation* assumes:
 - ▶ The individual beta is identical across all names in the basket.
 - ▶ The default boundary is identical and calibrated to CDX level.
 - ► All firms have identical LGD of 60%.
- \Rightarrow With these heroic assumptions, a single number, the *implied correlation* (= ρ), allows to match a given tranche's model price with the market price (for a given CDX level).

Outline	Summary O	CDS/CDX Market 000000	CDO Market	Credit S	pread Puzzle	The model	The story	Final Thoughts
The	implied o	correlation	smile					
► N	Narket Qu	otes on Aug.	4, 2004 (CDX ind	dex spread	63.25 bp)		
		Tranche	0-3%	3-7%	7-10%	10-15%	15-30	%
		CDX.IG	41.38%	3.49%	1.355%	0.46%	0.149	6
▶ T	he market	displays an	implied co	orrelation	n smile:			
		Tranche	0-3%	3-7%	7-10%	10-15%	15-30%	
		CDX.IG	21.7%	4.1%	17.8%	18.5%	29.8%	
\Rightarrow T	he smile s	shows that th	ne Gaussia	n copula	model is	mis-specif	ied (\sim op	— otion skew).
N	∕larket quo	tes on June	1st 2005 I	G4-5Y (CDX inde	x spread o	f 42 bp):	
		Tranche	0-3%	3-7%	7-10%	10-15%	15-30%	o o
		CDX.IG	30.5%	0.66%	.095%	.075%	0.04%	
▶ T	he correst	onding impl	lied correla	tion sm	ile:			_
		Tranche	0-3%	3-7%	7-10%	10-15%	15-30%	<u></u>
		CDX.IG	9.08%	5.8%	10.02%	16.77%	27.62%	<u>′</u>
► N	Market quo	otes on July	7 2007 IG8	3-5Y (CI	OX index s	pread of 4	8 bp):	_
		Tranche	0-3%	3-7%	7-10%	10-15%	15-30%	o o
		CDX.IG	33.5%	1.80%	.40%	.225%	0.065%	, 0

Correlation 'trading'

Outline

- lacktriangle Selling protection on the equity Tranche (delta-hedged) \sim long correlation:
 - ▶ Selling protection on equity is equivalent to being long a put on aggregate losses with strike equal to 3%. The value is increasing in the volatility of total losses which increases with default correlation.
 - The equity tranche is exposed to idiosyncratic Jump-to-default risk since it gets hit at the first default.
- lacktriangle Selling protection on the senior tranches \sim short correlation:
 - Selling protection on super senior tranche is short a call option on aggregate portfolio losses struck at 30%. Its value is decreasing in loss volatility and hence decreasing in correlation.
 - ► The Super senior tranche is exposed to systematic (cataclysmic?) risk: What is the probability that > 30% of investment grade default within a year?
- ▶ At least two reasons for the rapid development of CDS/CDX/CDO markets:
 - Credit spread puzzle
 - ▶ Rating 'arbitrage'

The Credit spread puzzle

▶ Investment-grade (IG) firms rarely default:

Average Issuer-Weighted Cumulative Default Rates 1970-2004

	Exhibit 18 - Moody's 2005 report										
Years	1	2	3	4	5	6	7	8	9	10	
Aaa	0.00	0.00	0.00	0.04	0.12	0.21	0.30	0.41	0.52	0.63	
Baa	0.19	0.54	0.98	1.55	2.08	2.59	3.12	3.65	4.25	4.89	

Further, recovery rates are substantial:

Average Recovery Rates by Seniority Class, 1982-2004

Exhibit 27 - Moody's 2005 report									
Year	Sr. Sec.	Sr. Unsec.	Sr. Subord.	Jr. Subord.	Subord.	All			
Mean	0.574	0.449	0.391	0.320	0.289	0.422			

- Structural models, when calibrated to match average loss rate, tend to underpredict yield spreads (relative to Treasury)
- \Rightarrow Structural models underestimate the risk-premium component of credit spreads, and/or
- ⇒ Spreads compensate for other factors (i.e, liquidity, taxes) in addition to credit risk

A Simple Calibration Exercise

► Consider simple Merton (1974) model

$$\frac{dV}{V} + \delta dt = (r + \theta \sigma) dt + \sigma dz$$

where θ is the asset value Sharpe ratio.

- ▶ Default occurs at T if V(T) falls below B. in that case recover 1 L.
- Risky debt payoff is:

$$\min(F,V_T) = F - \max(F - V_T,0)$$

- \Rightarrow risky debt is equal to risk-free debt minus a put option.
- ▶ Spread (y r) on a date-T zero coupon bond is:

$$(y-r) = -\left(\frac{1}{T}\right)\log\left\{1-LN\left[N^{-1}\left(\pi^{P}\right)+\theta\sqrt{T}\right]\right\}.$$

 \Rightarrow Even though the model is specified by 7 parameters $\{r, \mu, \sigma, \delta, V(0), B, L\}$, credit spreads only depend on historical default probability, recovery and asset sharpe ratio $\{\pi^P, L, \theta\}$.

A Simple Calibration Exercise

		T = 4	Υ	T = 10Y			
Sharpe	Baa	Aaa	Baa-Aaa	Baa	Aaa	Baa-Aaa	
0.15	44.0	1.6	42.4	67.7	12.0	55.7	
0.20	54.9	2.2	52.7	88.1	17.4	70.7	
0.25	68.1	3.0	65.1	112.8	24.6	88.2	
0.30	83.7	4.1	79.6	141.7	34.2	107.5	
0.35	102.0	5.5	96.5	175.1	46.6	128.5	
0.40	123.4	7.4	116.0	212.9	62.2	150.7	

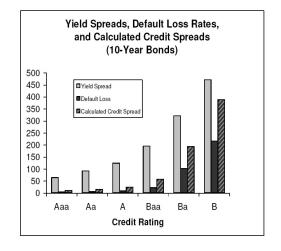
Table: (Baa - Aaa) spreads as a function of Sharpe ratio. 4Y Baa default rate = 1.55%. 4Y Aaa default rate = 0.04%. 10Y Baa default rate = 4.89%. 10Y Aaa default rate = 0.63%. Recovery rate = 0.449.

- ▶ Typical Baa firm asset value Sharpe ratio estimated around 0.22.
- ⇒ The credit spread puzzle says that historically, strategy going long corporate bonds seems very appealing (i.e., typical models cannot explain the level of observed spreads) because:
 - (i) historical expected loss rates have been low, and
 - (ii) Idiosyncratic (diversifiable!) risk on typical IG bonds is quite high (roughly half of the total risk).

 Summary
 CDS/CDX Market
 CDO Market
 Credit Spread Puzzle
 The model
 The story
 Final Thoughts

 0
 000000
 0000
 000
 00
 00
 00
 00

A Simple Calibration Exercise



source: Huang and Huang (2003)

Summary	CDS/CDX Market	CDO Market	Credit Spread Puzzle	The model	The story	Final Thoughts
0	000000	00000	0000	•0	00	00

The modeling framework

- ▶ The contribution (vs. Gaussian copula model) is to extract the density of the market factor *M* from SP500 Equity options.
 - Fit a parametric implied volatility function to observed implied vols on ATM and 30% OTM SP500 put options.
 - Use the Breeden Litzenberger (1978) formula to extract the density of market return (~ state price density) from option prices.
- Potential issues:
 - Prices of senior tranches very sensitive to tail events, i.e, very sensitive to the extrapolation of the implied vol curve where there is no data.
 - Results for senior tranche seem pretty sensitive to functional form of implied vol function (10bps difference on 40bps price).
 - ⇒ Important to insure that the implied vol parametric form is arbitrage-free. Not easy (e.g., Lee (2003), Fengler (2005)).
 - ⇒ Better to work in price space (use an option pricing model?).
 - Inconsistency between underlying SP500 return and IG portfolio (different names, leverage).
- Shares well-known short-comings of the Gaussian Copula model:
 - ► Assume covariance structure driven by one factor model
 - Assume that all firms in the basket are homogeneous (same distance to default, same recovery rate, same pair-wise correlation).
 - ▶ The model is purely static: gives loss distribution only at maturity.
 - ▶ Infinite *N* (large portfolio) approx. is not needed given homogeneity assumption.
 - Cannot 'explain' major repricing events such as May 05 (Auto sector), July 07 (Subprime).

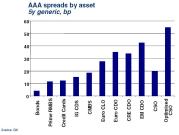
Quantitative implications

Outline

- ▶ The calibration procedure is a bit imprecise:
 - ▶ All securities handled as zero-coupon prices (no timing of cash-flows).
 - CDX is priced as a zero coupon bond (equation 21). But it is an unfunded product ~ basket of single-name CDS.
 - ► The calibration procedure has **one** constraint (matching CDX price) and **three** parameters (average leverage, average beta, average idiosyncratic risk). Therefore '**typically** require that the model implied equity beta equal one' (p.15)?
 - ⇒ Interesting to report idiosyncratic risk and distance to default numbers.
- ► Find that all senior and mezzanine tranches (3-7,7-10, 10-15,15-30) are well under-priced by the market. Differences are very large:
 - ► Fair value of selling protection on 3% to 30% should be approximately 23bps vs. 9.55bps in the market.
 - ▶ Most dramatic for senior 15-30 tranche: fair value of **47bps** vs. 9bps in the market.
 - ► To be compared to an average spread on CDX of 47.8bps!
- ▶ The authors should report all tranches, i.e., 0-3 and 30-100. The implication (if model is correct) is that the 0-3 tranche must be seriously over-priced by the market! Selling protection on the equity tranche should be a very profitable venture...
- Would be interesting to look at the CDX-tranche basis predicted by the model (potential impact of LGD risk).

Are senior tranches priced inefficiently by naive investors?

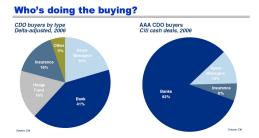
- Investors care only about expected losses (~ ratings) and not about covariance (ironic since they trade in correlation markets!).
- ⇒ Spreads across AAA assets should be equalized. Are they?



- ⇒ All spreads should converge to **Physical** measure expected loss.
 - $\,\blacktriangleright\,$ We observe large risk-premium across the board $(\lambda^Q/\lambda^P>6.)$
 - Large time-variation in that risk-premium.
- ⇒ Time-variation in spreads should be similar to that of rating changes (smoother?).
- ► Evidence seems inconsistent with marginal price setters caring only about expected loss (~ ratings).

Who is the marginal investor in synthetic tranche markets?

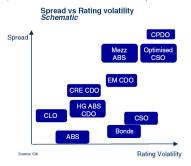
- Arbitrage relation ties price of all tranches to price of underlying. If some tranches are expensive other tranches are cheap.
- ⇒ Opportunities for smart investors (hedge funds, Harvard professors...?) to trade.
- ▶ Who is marginal investor in synthetic tranche market?



- Evidence from most markets is that "Crash risk premium" is very high (OTM put options, catastrophe bonds, reinsurance markets).
- ⇒ This would be 'unique' opportunity to purchase cheap crash insurance.

What drives differences between structured AAA spreads?

 Wall street's favorite story: Rating-stability premium ('reaching for yield' by rating constrained investors who want to take more risk - ratings simply do not reflect risk and/or expected payoff b/c to coarse and persistent).



- My favorite story: Moral hazard and marking to market.
 - Absent MtM risk, moral hazard would drive spreads on senior tranches to zero.
 - ⇒ Positive aspect of limits to arbitrage?
- ▶ Additional Consideration: Borrowing Constraints/funding costs.
 - Remote risks need to offer higher premium to attract capital which is in limited supply (given limited term-financing availability and variability of short term collateralized financing conditions; agents care about dollar NPV not IRR).

Conclusion

- Provocative paper with interesting idea to use option prices to extract common factor to replace Gaussian factor of market Copula model.
- Promising results with respect to fitting CDX 'out of sample'.
- More work needed to convince that model prices are realistic.
- ▶ Story seems hard to reconcile with simple facts (at least when taken at face value).