

Financing Cycles*

Thomas Geelen[†] Jakub Hajda[‡] Erwan Morellec[§] Adam Winegar[¶]

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Abstract

Capital ages and must eventually be replaced. We propose a theory of financing in which firms finance new capital with debt and optimally deleverage to free up debt capacity as their capital ages, thereby generating debt cycles. Concurrently, firms shorten the maturity of their debt to match the remaining life of their capital, generating maturity cycles. We provide time series and cross-sectional evidence that strongly supports these independent predictions and highlights the key roles of capital age and asset life in financing cycles.

Keywords: capital age, debt cycles, maturity cycles.

JEL Classification: E32, G31, G32.

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[†]Copenhagen Business School and Danish Finance Institute. E-mail: tag.fi@cbs.dk

[‡]HEC Montréal. E-mail: jakub.hajda@hec.ca

[§]Corresponding author. EPFL, Swiss Finance Institute, and CEPR. E-mail: erwan.morellec@epfl.ch

[¶]BI Norwegian Business School. E-mail: adam.w.winegar@bi.no

Capital ages and must eventually be replaced (Feldstein and Rothschild, 1974). As an example, in 2011 American Airlines ordered 460 airplanes to replace its ageing fleet.¹ Large, planned replacement investments are not exclusive to airlines, but are a hallmark of real-world business operations. For instance, the aggregate replacement investments of U.S. public firms amounted to \$1.27tn in 2019—representing around 21% of their capital stock. In this paper, we argue that planned replacement investments are an important driver of financing choices that lead to debt and maturity cycles at the firm level.

To demonstrate how planned replacement investments fundamentally affect firm financing, we proceed in two steps. We first develop a dynamic model of investment and financing in which capital ages and firms can choose not only how much debt to issue but also the maturity of this debt. In this model, firms borrow to finance investment and optimally deleverage to free up debt capacity as capital ages, allowing them to issue new debt when old capital needs to be replaced. To achieve these dynamics, firms issue debt with a maturity that matches the useful life of new assets and a repayment schedule that reflects the need to free up debt capacity as capital ages. These dynamics lead to firm-level debt cycles and to a matching between debt maturity and asset life. They additionally imply that leverage and debt maturity are negatively related to capital age while debt maturity and the length of debt cycles are positively related to the useful life of assets. We then test these predictions on a large sample of listed U.S. firms over the 1975–2018 period and, as hinted by Figure 1, find strong support for all of them in the data.

Our model builds on prior dynamic models of firm investment and financing (Gomes, 2001; Hennessy and Whited, 2005; DeAngelo, DeAngelo, and Whited, 2011). But it differs in that capital has a finite useful life, as in e.g. Arrow (1964), Rogerson (2008), Rampini (2019), or Livdan and Nezlobin (2021), instead of being geometrically depreciated.² Just as any non-geometric form of depreciation, a finite useful life makes capital age relevant for

¹See the Financial Times of July 7 2012, Procurement: Dependent on vision and strategy.

²The standard assumption of geometric depreciation makes capital age irrelevant for the firm’s problem since a capital’s future productivity (and value) can be perfectly described by its current productivity. Subsection I.D shows that our results are robust to alternative forms of depreciation. The key force underlying our results and predictions is that the firm replaces ageing capital via large, planned investments. As a result, similar financing dynamics would arise in a model with fixed investment costs; see Subsection I.D.

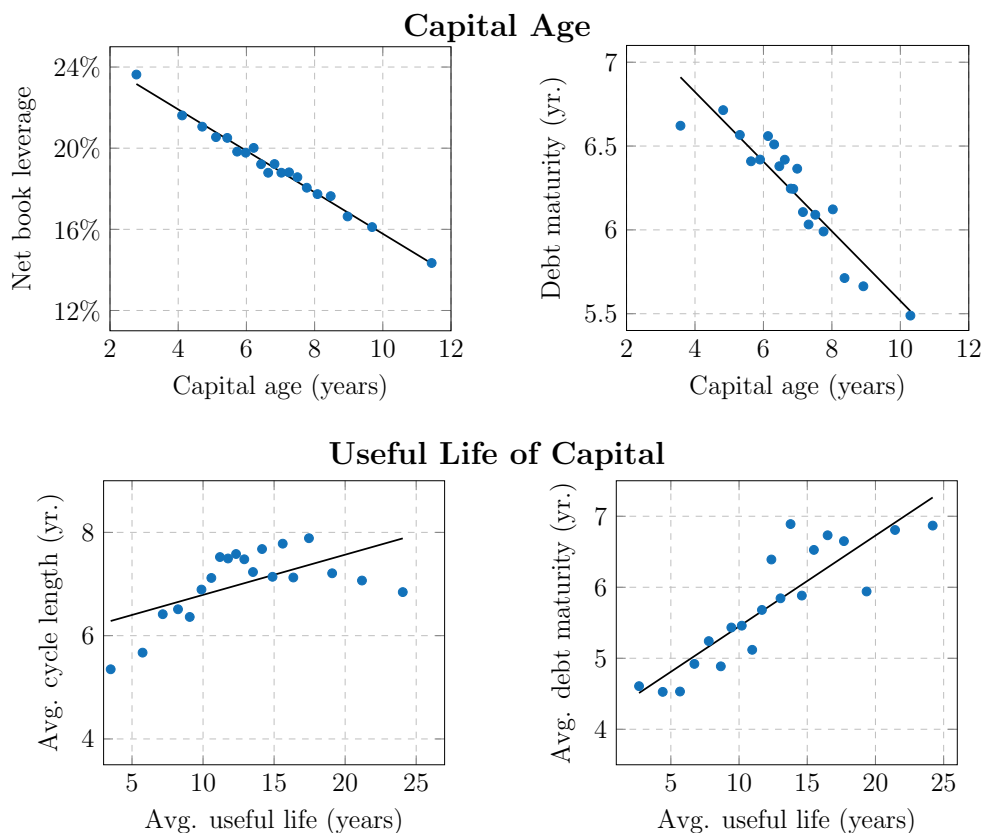


Figure 1: **Debt financing, capital age, and capital's useful life.** The top panels control for firm fixed effects. Each dot corresponds to $1/20^{th}$ of the sample firms. The sample period is from 1975 to 2018. Variables are defined in Table A.1.

investment and financing decisions. A finite useful life means that the productivity of capital, but not its value, remains constant over its lifespan after which it needs to be replaced—a good approximation for many forms of capital. As an example, consider two airlines with the same number of airplanes. One airline utilizes airplanes which are, on average, older than the airplanes of the other airline. Geometric depreciation of the airplanes would imply that the airline with younger airplanes should fly more passengers, as its capital is younger and therefore more productive. However, since the airlines have the same number of airplanes, they roughly fly the same number of passengers. In our model, as in the airline example, the firm knows it needs to make replacement investments in the future as its capital ages due to the finite life of its assets (airplanes). That is, the firm faces large, planned investments.

In the model, the firm has an incentive to finance investment with debt because creditors are more patient than shareholders, which is equivalent to debt providing tax benefits. But since the firm faces a borrowing constraint (Lian and Ma, 2021; Griffin, Nini, and Smith, 2019), it manages its leverage keeping in mind future funding needs. Therefore, the firm initially levers up when buying new capital. However, as its capital ages, it progressively reduces its net debt to free up debt capacity that will be used to finance future replacement investments. These net debt dynamics generate firm-level debt cycles, imply that firms have inherently unstable leverage, consistent with the findings of DeAngelo and Roll (2015), and rationalize the *pro-active* leverage declines documented in Denis and McKeon (2012) and DeAngelo, Gonçalves, and Stulz (2018).³ They also imply a negative relation between capital age and leverage and a positive relation between the length of debt cycles and the useful life of capital, in line with the patterns highlighted in Figure 1. These leverage dynamics arise in our model from the fact that capital ages and has a finite useful life, leading the firm to *predictably* replace existing capital in *lumps*.

In our baseline model, debt issuance is costless and the firm issues and rolls-over one-period debt. With debt issuance costs (Altinkılıç and Hansen, 2000; Yasuda, 2005), the firm implements the same net debt dynamics as in the baseline model but only issues debt when buying capital to minimize issuance costs. To do so, the firm issues debt with a maturity that matches the useful life of new assets and with a repayment schedule that progressively frees up debt capacity. By doing so, the firm ensures that the repayment of maturing debt provides enough financial slack to finance replacement investments. Therefore, capital ageing leads to a matching theory of debt maturity and to firm-level maturity cycles. Notably, our model predicts that debt maturity should increase with the useful life of assets but decrease with capital age, in line with the empirical patterns highlighted in Figure 1.

The mechanism in our model produces firm-level time-series predictions and cross-sectional predictions. We test these using data on U.S. public firms and produce two main findings. First, in line with the model predictions, we find that capital age is a significant predictor of

³Notably, DeAngelo et al. (2018) find that this deleveraging reflects decisions to repay debt and retain earnings as opposed to exogenous shocks that drive stock-market prices up and leverage ratios down.

both leverage and debt maturity, even after conditioning on a standard set of leverage and maturity controls, including firm age or market-to-book. In addition, when examining the importance of different factors in explaining leverage ratios as in [Frank and Goyal \(2009\)](#), we find that capital age is the factor with the most explanatory power. In separate tests aimed at exploring the mechanism, we show that the effects of capital age on leverage and debt maturity are stronger for smaller firms, firms in which investment is more lumpy, and firms with a lower return on investment, in line with the model predictions. Second, we find in cross-sectional tests that the useful life of assets is a significant predictor of both the length of debt cycles and average debt maturity. Notably, firms with longer-lived assets follow longer debt cycles and have a higher average debt maturity, in line with our predictions. We perform various robustness tests to confirm the validity of our results, using alternative proxies for capital age and the useful life of assets, alternative measures of debt maturity, and alternative industry definitions. All these robustness tests confirm our findings.

Our paper makes several contributions. First, we develop a framework in which investment cycles lead to endogenous debt and maturity cycles. From a modeling perspective, this framework brings together the literature on vintage capital ([Arrow, 1964](#); [Ramey and Shapiro, 2001](#); [Rogerson, 2008](#); [Rampini, 2019](#); [Livdan and Nezlobin, 2021](#)) and the literature on lumpy investment ([Cooper and Haltiwanger, 1993](#); [Caballero and Engel, 1999](#); [Cooper, Haltiwanger, and Power, 1999](#); [Winberry, 2021](#)). While existing papers focus on investment dynamics, our paper instead articulates the effects of vintage capital and lumpy investment on financing decisions. Notably, our paper is the first to outline the consequences of the investment cycles associated with lumpy investment for financing cycles and to shed light on the implications of capital age for debt dynamics.

Second, our paper advances the literature studying dynamic financing and investment decisions ([Gomes, 2001](#); [Hennessy and Whited, 2005](#); [Clementi and Hopenhayn, 2006](#); [Nikolov, Schmid, and Steri, 2019](#)) by highlighting the role of capital age and asset life in determining not only debt dynamics but also debt maturity choices. In this literature, our model shares several features with [DeAngelo et al. \(2011\)](#) in that investment spikes are accompanied by leverage spikes and firms deleverage progressively to free up debt capacity. However, our

analysis is distinctive for *i*) the roles it assigns to capital age and asset life, *ii*) the associated implications it derives for firm-level cycles, and *iii*) its analysis of debt maturity. Our model is also related to [Rampini and Viswanathan \(2013\)](#) and [Rampini \(2019\)](#), who investigate the consequences of asset-based borrowing constraints for firm financing. In these studies, the market for physical capital is frictionless so that capital only affects the firm’s future through its residual value. In addition, investment is smooth and firms only issue one-period debt so that there is no notion of debt cycles or maturity matching. Our paper instead allows for frictions in the market for physical capital. In our model, firms retain and eventually replace their capital, which drives their financing decisions. Capital ageing leads to debt cycles, consistent with the dynamics documented by [Denis and McKeon \(2012\)](#) and [DeAngelo et al. \(2018\)](#), and has important implications for debt maturity choices.

Third, we contribute to the literature on debt maturity choice by proposing a theory in which firms match the maturity of their assets and debt liabilities.⁴ We show that the maturity structure linkage emerges naturally in worlds in which *i*) firms borrow to meet funding needs for immediate investment and *ii*) subsequently deleverage to have debt capacity when assets in place reach the end of their useful life. Importantly, while [Graham and Harvey \(2001\)](#) find in their survey of corporate managers that the desire to match debt maturity to asset maturity is the most important factor in the choice between short- and long-term debt, this “matching principle” has so far received mixed empirical support.⁵ Our paper highlights the distinct roles of capital age and useful life of assets in explaining debt maturity choices and leverages this distinction to provide large sample evidence in support of the maturity matching principle. Notably, we demonstrate theoretically and verify empirically that maturity matching implies that capital age—which is a dynamic variable—predicts financing and debt maturity choices in time-series regressions. By contrast, the useful life of assets—which is primarily a time-invariant firm characteristic—explains cross-sectional differences in debt

⁴See e.g. [Cheng and Milbradt \(2012\)](#), [Diamond and He \(2014\)](#), [He and Milbradt \(2016\)](#), or [Huang, Oehmke, and Zhong \(2019\)](#) for recent contributions on the debt maturity choice.

⁵In an early contribution, [Stohs and Mauer \(1996\)](#) provide supporting evidence for this principle by documenting a positive relation between asset maturity and debt maturity. In recent research, [Custódio, Ferreira, and Laureano \(2013\)](#) challenge the maturity matching principle by showing that asset maturity is only significantly related to debt maturity in regressions without firm fixed effects.

maturity choices. In the literature on debt maturity, our paper is most closely related to [Myers \(1977\)](#) and [Hart and Moore \(1994\)](#). [Myers \(1977\)](#) argues that firms with more growth options should shorten debt maturity to reduce debt overhang.⁶ Instead, our theory ties the debt maturity choice to the useful life of assets in place. This allows us to show that optimal financing is characterized by cycles and to generate unique predictions relating capital age and the useful life of assets to leverage and debt maturity. [Hart and Moore \(1994\)](#) argue that managers’ ability to withdraw their human capital drives debt maturity choices and leads to maturity matching between assets and liabilities. In our model, this matching is driven by investment in physical capital and the need to free up debt capacity. Consistent with our mechanism, we find that financing cycles are stronger for smaller firms, firms with more investment lumpiness, and for firms with a lower return on investment.

Lastly, we leverage our theoretical analysis to contribute to the large empirical literatures on capital structure ([Leary and Roberts, 2005](#); [Lemmon, Roberts, and Zender, 2008](#); [Frank and Goyal, 2009](#)) and debt maturity ([Stohs and Mauer, 1996](#); [Custódio et al., 2013](#); [Choi, Hackbarth, and Zechner, 2018](#)). We do so by showing that our mechanism for the formation of debt cycles ([DeAngelo et al., 2018](#)) is consistent with the dynamics of leverage around investment peaks ([Bargeron, Denis, and Lehn, 2018](#)) and the incidence of large, proactive increases in leverage ([Denis and McKeon, 2012](#); [DeAngelo and Roll, 2015](#)). Our analysis also brings out the key roles of capital age and asset life in the dynamics of leverage and debt maturity and provides cross-sectional and time series evidence that strongly supports the proposed mechanism. An additional empirical contribution of this paper is to use net debt to EBITDA to measure leverage, with our model generating predictions specifically related to this measure. While [Graham \(2022\)](#) finds in his survey of CFOs that this is by far the most commonly used measure of leverage in practice, he also notes that “in The Journal of Finance articles published since 2015 that mention leverage [...] none use debt/EBITDA”.

⁶[Myers \(1977\)](#)’s conjecture has been recently challenged by [Diamond and He \(2014\)](#) who show that debt overhang may increase or decrease with debt maturity. Consistently, empirical work on debt maturity based on the hypothesis of reduced overhang of shorter term debt has had mixed success. [Barclay and Smith \(1995\)](#) and [Guedes and Opler \(1996\)](#) document a negative relation between maturity and growth opportunities, while [Stohs and Mauer \(1996\)](#) and [Johnson \(2003\)](#) find a positive relation after controlling for leverage.

I Model

A Assumptions

We first consider a dynamic model of investment and financing in which firms can invest in a single asset with constant productivity to highlight, in the simplest possible setting, the mechanism leading to financing cycles. Subsection I.D shows that our results are robust to introducing multiple assets, alternative types of economic depreciation, and shocks.

Time is discrete and indexed by $t \in \{0, 1, 2, \dots\}$. We consider a representative firm owned by a risk-neutral entrepreneur who discounts cash flows at rate $r > 0$. The firm has cash reserves C_0 at time $t = 0$. Each period, it can use one unit of capital to produce one unit of the final good in the next period, which yields a profit $\pi > 0$. The firm can acquire a unit of new capital, which is delivered immediately, for a price K . Capital cannot be sold—investment is irreversible—and has a finite useful life. Notably, capital has a constant productive capacity over a finite number n of periods after which it needs to be replaced.⁷ That is, capital has a constant productivity over its lifespan but a declining value. This type of economic depreciation is known as one-hoss-shay depreciation (see [Arrow, 1964](#); [Laffont and Tirole, 2001](#); [Rampini, 2019](#); [Livdan and Nezlobin, 2021](#)) and is largely used in practice. [Livdan and Nezlobin \(2021\)](#) note for example that firm-level data on capital goods, such as property, plant, and equipment (PP&E), is prepared in practice almost exclusively under the assumption that the efficiency of capital goods is constant over a finite useful life.⁸

As an example, consider two airlines with the same number of airplanes, one of which uses airplanes that are, on average, older than the other's. Geometric depreciation of the airplanes (as in e.g. [Hayashi, 1982](#)) would imply that the airline with younger airplanes should fly more passengers, as its capital is younger and therefore more productive. However,

⁷In this respect, we depart from most existing work, which relies on geometric depreciation of capital following [Hayashi \(1982\)](#). There exists ample empirical evidence that geometric depreciation does not fully reflect reality ([Feldstein and Rothschild, 1974](#); [Harper, 1982](#); [Ramey and Shapiro, 2001](#); [Rogerson, 2008](#)) and that depreciation is backloaded ([Giandrea, Kornfeld, Meyer, and Powers, 2021](#)). In our setting depreciation of capital can take the form of physical depreciation and/or (expected) technological obsolescence.

⁸While the use of one-hoss-shay depreciation makes our results and empirical predictions particularly crisp, Subsection I.D shows that they are robust to other forms of depreciation.

since the airlines have the same number of airplanes, they roughly fly the same number of passengers. In this case, using a finite useful life better reflects their productivity.⁹

We assume that investment is positive net present value (NPV) (Appendix A provides the exact parameter restriction). The present value of the cash flows of a firm that always produces goods is then given by

$$\sum_{t=1}^{\infty} \frac{1}{(1+r)^t} \pi - \sum_{i=0}^{\infty} \frac{1}{(1+r)^{i*n}} K = \frac{\pi}{r} - \frac{(1+r)^n K}{(1+r)^n - 1}.$$

Figure 2 shows the cash flows of a firm that produces each period and replaces capital at the end of its useful life. Under this policy, capital replacement leads to investment spikes, as seen in the data (Doms and Dunne, 1998; Cooper and Haltiwanger, 2006; Whited, 2006).

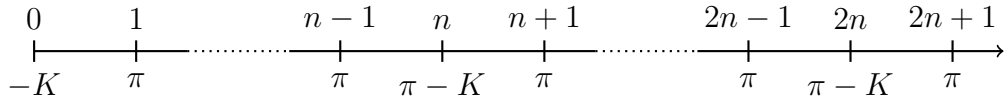


Figure 2: **Firm cash flows.** Each period, the firm produces and capital generates a profit of π the next period. Each n periods, new capital is bought at a price K .

As in Rampini and Viswanathan (2010), the firm finances investment with cash (retained earnings) and/or one-period debt.¹⁰ Creditors are more patient than the entrepreneur and discount cash flows at a rate $\rho_D < r$, which generates an incentive for the firm to issue debt. This assumption is standard in discrete time dynamic financing and investment models (e.g., DeAngelo et al., 2011), and is equivalent to the existence of tax benefits of debt $\rho_D = (1 - \tau)r < r$, where $\tau \in (0, 1)$ is the corporate tax rate.

⁹One could argue that firms purchase many different types of capital and therefore geometric depreciation is a good approximation of their actual productive capacity. But as in the example given, there exists substantial within-firm variation in capital age in the data, and therefore depreciation of capital productivity \neq depreciation of capital value inside the firm, which is required to use geometric depreciation.

¹⁰Section II introduces proportional debt issuance costs, allows the firm to issue multi-period debt, and derives the optimal debt maturity structure. The model can also be extended to incorporate costly equity issuance. With proportional or convex equity issuance costs, leverage and debt maturity will follow the same patterns as in the current model. For large enough equity issuance costs, the firm will finance investment exclusively with debt and financing dynamics will be exactly as in the baseline model. For low enough issuance costs, the firm will partly rely on equity to finance investment, leading to dampened debt cycles.

The two most common approaches for modeling borrowing constraints in dynamic capital structure models is to consider either cash-flow based constraints (Clementi and Hopenhayn, 2006) or asset-based constraints (Rampini and Viswanathan, 2010). In our model, financing cycles arise with *either type of borrowing constraint*. In a recent study, Lian and Ma (2021) show that 80% of debt contracts in the U.S. are associated with cash-flow-based borrowing constraints (see also Griffin et al. (2019)).¹¹ We therefore assume that when the firm produces the final good at time t , it can issue debt up to the cash-flow-based constraint:

$$D_t \leq \phi \times \pi,$$

where D_t is total debt at time t and $\phi \in [\underline{\phi}, \bar{\phi}]$ is a constant multiple. The lower bound $\underline{\phi} > 0$ ensures that the firm can purchase the asset. The upper bound $\bar{\phi}$ ensures that debt is risk-free irrespective of the fraction of their principal creditors recover in default. Appendix A provides the exact parameter restrictions. Subsection I.D shows that asset-based borrowing constraints mechanically strengthen our result that firms lower net debt as capital ages since the collateral value declines as capital ages.

The firm earns a return $\rho_C \in (0, \rho_D)$ on its cash holdings, implying that the firm never holds both cash and debt (as in Hennessy and Whited (2005) or DeAngelo et al. (2011)) and has no incentives to retain more cash than is needed to fund investment.

¹¹Lian and Ma (2021) note that for U.S. nonfinancial firms “cash flow-based lending prevails (given the legal foundations in the United States that allow for high verifiable cash flows and the high asset specificity of nonfinancial firms), and borrowing constraints emphasize firms’ cash flow value. For models with riskless debt and quantity constraints (e.g. Kiyotaki and Moore (1997) [or our model]), for example, the data suggest that a prevalent form of borrowing constraint restricts a firm’s total debt as a function of its cash flows measured using current operating earnings.” This feature of the data may be due to the fact that many assets are specialized, illiquid, and subject to significant adjustment costs in liquidation. In addition, Lian and Ma (2021) note that in 90% of defaults file for Chapter 11 (leading to reorganization) and not for Chapter 7 (leading to liquidation). In Chapter 11, total payments to creditors are given by the cash flow value of the continuing operation of the restructured firm, which is verified and approved in court. U.S. bankruptcy laws also prohibit creditors from seizing assets to disrupt firms’ operations (due to the automatic stay of assets). “The institutional setting is therefore different from models where cash flows are not verifiable and creditors use seizing assets as a threat for debt enforcement.”

B Equity Value

At time t , the firm has cash reserves C_t and invests I_t in new capital (if at all). Dividends are then given by the budget constraint

$$\begin{aligned} Div_t &= \pi \mathbb{I}_{\{\text{firm produces}\}} - I_t + C_{t-1}(1 + \rho_C) - C_t + D_t - D_{t-1}(1 + \rho_D) \\ &= \pi \mathbb{I}_{\{\text{firm produces}\}} - I_t + ND_t - ND_{t-1} (1 + \rho_D \mathbb{I}_{\{ND_{t-1} \geq 0\}} + \mathbb{I}_{\{ND_{t-1} < 0\}} \rho_C) \geq 0, \end{aligned} \quad (1)$$

where $ND_t = D_t - C_t$ is the firm's net debt, which summarizes its financing policy, and $\mathbb{I}_{\{x \geq y\}}$ is the indicator function of the event $x \geq y$.

Management maximizes the present value of future dividends by choosing investment I_t and financing ND_t policies. That is, equity value solves

$$E_0 = \sup_{\{I_t, ND_t\}_{t \in \{0, 1, 2, \dots\}}} \sum_{t \geq 0}^{\infty} \frac{Div_t}{(1 + r)^t},$$

where dividends follow from the budget constraint in equation (1) and are non-negative, and net debt satisfies the borrowing constraint $ND_t \leq \phi \times \pi$.

C Financing and Investment

In our model, investment is positive NPV. Furthermore, given the firm's borrowing constraint, management has no incentive to abscond with the debt proceeds since this would imply it has to forgo future investment opportunities. Finally, time discounting implies that management has no incentive to replace existing capital early and incur the investment cost early. As a consequence, we have that (see the Appendix for all proofs):

Proposition 1 (Firm Investment). *The firm never defaults on its debt and replaces existing capital when it reaches the end of its useful life and never before.*

Next, let $a \in \{0, 1, \dots, n - 1\}$ be the age of the firm's current capital. With a slight abuse of notation, we also use a as a time index. ND_a will therefore refer to net debt given that the

firm has capital with age a . Given that the return on cash is lower than the return on debt $\rho_C < \rho_D$, the firm never holds both cash and debt at the same time. Therefore, financing policies are summarized by the firm's net debt ND_a . Given debt's lower required rate of return $\rho_D < r$, the firm wants to utilise its debt capacity to maximize value. The firm thus wants maximize its borrowing while still being able to replace capital when it reaches the end of its useful life (Proposition 1). It does so by raising the maximum amount of debt when it invests $ND_0 = \phi\pi$. As capital ages, the firm then optimally starts repaying debt to create financial slack. This financial slack allows the firm to invest in new capital by issuing new debt when existing capital reaches the end of its useful life. The firm delays lowering its net debt as long as possible to maximize debt benefits without sacrificing its ability to replace ageing capital. The following theorem formalizes this result:

Theorem 1 (Debt Cycles). *As capital ages, the firm frees up debt capacity to finance replacement investments, in that*

$$ND_{a+1} \leq ND_a.$$

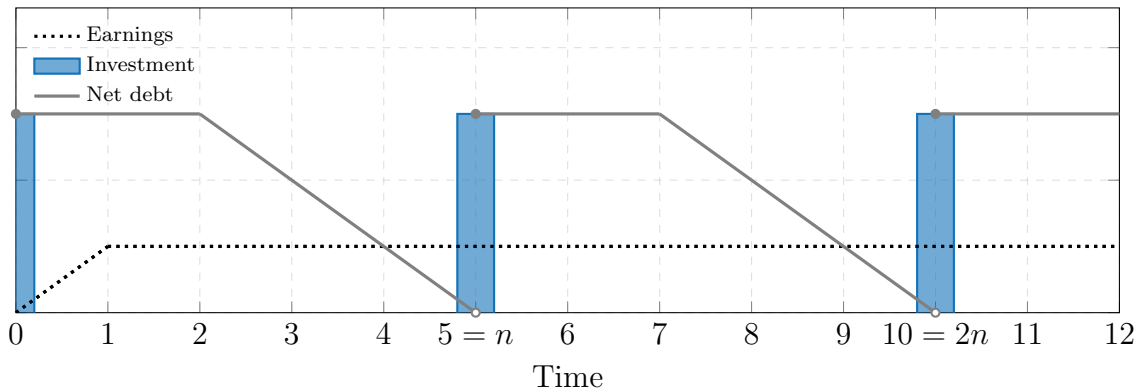


Figure 3: **Earnings, investment, and net debt dynamics.**

Figure 3 shows the optimal dynamics of investment and financing. The firm finances investment by increasing net debt because of the benefits of debt financing, i.e. $\rho_D < r$. It then optimally retains earnings to lower net debt. The firm does so to free up debt capacity

to be able to finance its replacement investment, which is positive NPV. These dynamics generate debt cycles that are driven by the firm’s ageing capital.

In our model, as in many recent dynamic capital structure models such as [Strebulaev \(2007\)](#), [Morellec, Nikolov, and Schürhoff \(2012\)](#), or [DeMarzo and He \(2021\)](#), the firm makes financing decisions with the objective of managing its net debt to earnings ratio. This is consistent with industry practice. [Graham \(2022\)](#) for example documents in his survey of corporate CFOs that debt/EBITDA is by far the most popular measure of debt usage. Indeed, the corporate credit market has norms about debt relative to earnings and, when firms issue debt, they generally cannot surpass the reference level of debt to EBITDA that lenders use. Also, when debt contracts include cash-flow based borrowing constraints, firms are explicitly subjected to specific debt to EBITDA ratios.¹² Thus, both in practice and in our model, firms actively manage their net debt to earnings ratio.

Importantly, the debt cycles depicted in [Figure 3](#) are consistent with several empirical findings: *i*) [Denis and McKeon \(2012\)](#) find that firms lever up to finance investment, which occurs in our model due to firms financing the replacement of ageing capital with debt; *ii*) [Denis and McKeon \(2012\)](#) and [DeAngelo et al. \(2018\)](#) find that firms significantly decrease leverage after reaching a peak, which occurs in our model because firms retain earnings and lower leverage to finance the eventual replacement of ageing capital; *iii*) [DeAngelo and Roll \(2015\)](#) find that corporate capital structure is inherently unstable, which is consistent with our debt cycles leading to inherently unstable firm leverage even in the absence of uncertainty; and *iv*) [Strebulaev and Yang \(2013\)](#) show that a large fraction of U.S. public firms has zero-leverage, which occurs in the model when $ND_a \leq 0$.

In addition to rationalizing prior findings, the model generates unique cross-sectional and time-series predictions for leverage. Within a firm, the model predicts that

Prediction 1. *Capital age and the ratio of net debt to earnings are negatively related.*

This negative relation arises because of the need to free up debt capacity as capital ages

¹²[Griffin et al. \(2019\)](#) show that debt/EBITDA is included in the most commonly used covenant packages and that there is an increasing use of cash flow-based covenants in recent years.

(Theorem 1). Across firms, the model predicts that

Prediction 2. *The duration of debt cycles is positively related to the useful life of assets.*

Our model also allows us to study the effects of lumpiness in investment and profitability on debt cycles. In our model, the cost of investment is given by K while its benefits are reflected in π . For a given level of cash flows π , a greater cost of investment K implies both that investment is more lumpy, as the firm needs to spend more whenever it invests, and that the return on investment, defined as $\frac{\pi}{K}$, is lower. In the Appendix, we show that:

Proposition 2 (Debt Cycles, Lumpy Investment, and Return on Investment). *As the cost of investment increases $K' > K$ the effects of capital age on net debt become more pronounced:*

$$|ND_{t+1} - ND_t| \leq |ND'_{t+1} - ND'_t|.$$

The more expensive capital becomes the more financial slack the firm needs to finance investment. As a result, as shown by Proposition 2, debt cycles become more pronounced as the cost of investment in physical capital K increases. This leads to the following prediction:

Prediction 3. *The effects of capital age on leverage, as measured by net debt over earnings, are more pronounced in firms with more lumpy investment and lower return on investment.*

D Robustness

I Other Forms of Capital Depreciation

Our model assumes that the efficiency of capital goods follows a one-hoss shay pattern, as in e.g. [Arrow \(1964\)](#), [Rogerson \(2008\)](#), [Rampini \(2019\)](#), or [Livdan and Nezlobin \(2021\)](#). This form of capital efficiency allows us to generate crisp empirical predictions on financing decisions and debt maturity choices. An important question is whether this form of capital efficiency is necessary for our results. *The short answer is no.* Debt cycles are generated by large replacement investments financed with debt. Thus, any form of economic depreciation that leads to large investments suffices as we show in Proposition 4 of the [Internet Appendix](#).

II Investment and Debt Dynamics

In the baseline model, the firm can invest in one unit of capital and replaces it every n periods. Assume now that the firm has N units of capital of different vintages, each of which generates a profit π per period for n periods. Furthermore, assume the firm replaces capital when it reaches the end of its useful life. Therefore, the firm invests at times $n * i - a_k^0$, $\forall i \in \mathbb{N}$ and $\forall k \in \{1, \dots, N\}$, where a_k^0 is the age of capital unit $k \in \{1, \dots, N\}$ at time zero.

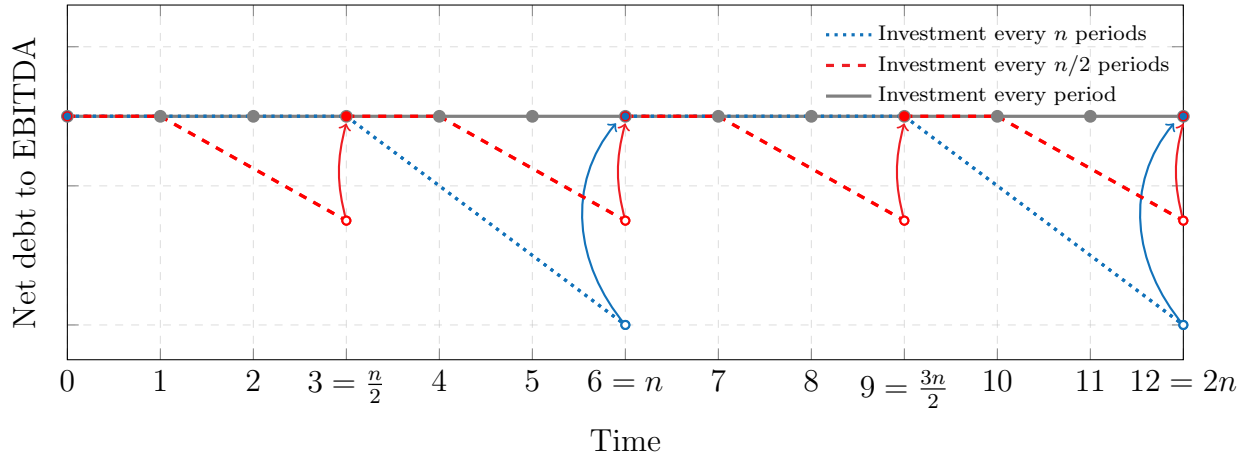


Figure 4: **Leverage dynamics for different investment frequencies.** Arrows indicate points in time when the firm makes a lumpy investment and starts a new debt cycle. The higher the frequency of investment, the less pronounced and the shorter the cycles are.

Proposition 5 of the [Internet Appendix](#) shows that, when firms operate multiple capital units of different vintages, the ratio of net debt to earnings is weakly decreasing until the next time the firm invests. In addition, the firm's capital stock ages when it does not invest, leading to a negative relationship between capital age and net debt over earnings. As Proposition 5 and Figure 4 highlight, the higher the frequency of investment, the shorter the periods over which leverage decreases. If the firm buys a new unit of capital every period, then leverage and capital age are constant. Otherwise, investment exhibits some lumpiness, which can lead to debt cycles and to a negative relation between capital age and net debt over earnings. Notably, debt cycles arise if in some periods investment costs exceed profits.

III Non-Geometric Depreciation Versus Fixed Investment Costs

In our model, financing cycles are driven by the predictable “lumps and bumps” in investment created by finite asset lives. In practice, other mechanisms/frictions could lead to predictable lumps and bumps in investment at the firm level, fixed investment costs being one of them. Indeed, in a standard model with decreasing returns to scale and geometric depreciation, the firm will postpone investment until the associated benefits are large enough to offset the fixed investment costs. This will happen when capital becomes sufficiently less productive (due to depreciation) that it becomes optimal to replace it (Cooper and Haltiwanger, 1993; Cooper et al., 1999). This alternative mechanism would lead to predictable investment cycles as in our model. In addition, and as in our model, the firm would need to free up debt capacity as capital ages to be able to finance replacement investments, thereby generating financing cycles. Financing cycles thus arise more generally in the presence of (predictable) investment cycles, independently of the nature of the technology or friction that drives these cycles. An important difference between the two mechanisms is that capital age is the natural predictor of investment and financing cycles in our setup, while the market/book ratio (i.e., marginal Q) is the natural predictor of these cycles in a model with fixed investment costs.

IV Shocks

Our baseline model considers a deterministic environment. Extending the model to introduce firm-level shocks and the possibility for the firm to invest in multiple units of capital would lead to debt patterns similar to those highlighted in Figure 4. Notably, if the firm faced very frequent shocks leading to investment, then capital age would be relatively constant and debt cycles would be absent. Otherwise, investment would display some lumpiness, leading to debt cycles. Section III shows that empirically capital age does vary over time and that debt ratios are characterized by cycles that are magnified by investment lumpiness.

V Cash-Flow Versus Asset-Based Borrowing Constraints

Recent research by [Lian and Ma \(2021\)](#) documents that 80% of debt of U.S. nonfinancial firms (in value terms) is based on constraints related to earnings, as assumed in our model, whereas 20% is based on the liquidation value of physical assets (“asset-based lending”). The [Internet Appendix](#) shows that debt cycles are *mechanically* stronger with an asset-based borrowing constraint. Indeed, asset-based borrowing constraints force firms to deleverage because they become tighter as capital ages, which does not happen with a cash-flow based constraint.

II Debt Maturity

In the baseline model, there is no cost of issuing debt so that there is no cost for the firm of issuing and rolling over one-period debt. In practice, issuing debt is costly ([Altinkılıç and Hansen, 2000](#); [Yasuda, 2005](#)). This section introduces debt issuance costs $\epsilon > 0$ that are proportional to the amount raised and allows the firm to have multiple debt issues outstanding at the same time with (possibly) different maturities. Interest on debt is paid each period. We study the situation in which debt issuance costs become small $\epsilon \rightarrow 0$. To make sure that the firm does not have permanent debt in its capital structure, we assume that capital investment cannot be fully financed by debt and current period profits:

$$K > \phi\pi + \pi. \tag{2}$$

All the results presented below apply to non-permanent debt if this assumption fails to hold.

With debt issuance costs, the firm implements the same net debt dynamics as in [Section I](#) but only issues debt when buying capital to minimize issuance costs. As a result, the debt maturity choice has no bearing on the debt cycles. To achieve these debt dynamics, the firm issues debt with a maturity that approximately matches the useful life of new assets and with a repayment schedule that progressively frees up debt capacity. This way, the firm makes sure that by repaying maturing debt it creates enough financial slack to finance replacement investments. The following theorem formalizes this result.

Theorem 2 (Long-Term Debt Financing). *With debt issuance costs, the firm only issues debt when buying new capital and optimally issues long-term debt with a repayment schedule such that net debt follows the same cycles as in Theorem 1.*

Let M_a be the average maturity of outstanding debt given that capital age is a . When $ND_a \leq 0$, the firm has no debt outstanding and $M_a = 0$. When $ND_a > 0$, we have that

$$M_a = \sum_{i=a}^{n-1} \mathbb{I}_{\{ND_i > 0\}} (i + 1 - a) \frac{ND_i - \max\{ND_{i+1}, 0\}}{ND_a}.$$

We can then show that capital age and average debt maturity are negatively related.

Proposition 3 (Debt Maturity Cycles). *Average debt maturity is decreasing in capital age:*

$$M_{a+1} \leq M_a.$$

Figure 5 shows how average debt maturity evolves through time when assets have a useful life of 6 years and the firm implements the optimal debt maturity structure at issuance. The firm only issues debt when buying new capital. Debt issuance leads to an increase in the average debt maturity which then decreases as capital ages until the firm invests again. Therefore, capital ageing not only leads to debt cycles but also to maturity cycles.¹³

An implication from the optimal financing policy is that the firm can postpone deleveraging when assets have a greater useful life and does so by issuing debt with a longer maturity. Notably we have that:

Theorem 3 (Maturity Matching). *Increasing the useful life of assets increases average debt maturity in that $\frac{\Delta M_a}{\Delta n} \geq 0$.*

The model generates both cross-sectional and time-series predictions for debt maturity. Within a firm, the model predicts that (see Proposition 3)

Prediction 4. *Capital age and debt maturity are negatively related.*

¹³Optimal financing can be implemented by either issuing amortising debt or by issuing multiple debt issues with staggered maturities.

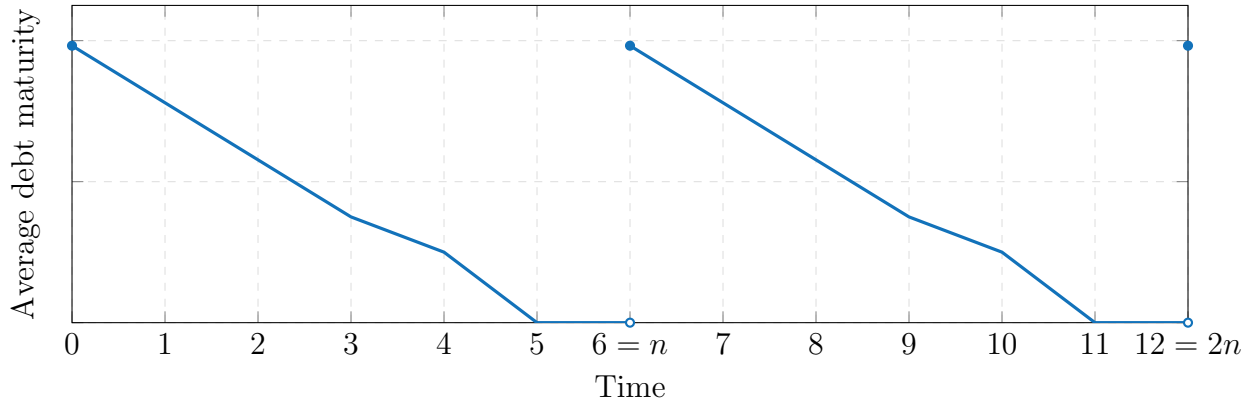


Figure 5: **Average debt maturity.** This figure shows the average debt maturity of a firm with assets that have a useful life of 6 years given the optimal debt maturity structure at issuance.

While cross-sectionally, the model predicts that (see Theorem 3)

Prediction 5. *Average debt maturity is positively related to the useful life of assets.*

III Empirical Analysis

This section tests the model predictions, with a main focus on the time-series Predictions 1, 3, and 4 relating capital age to leverage and debt maturity.

A Data and Variables

Our empirical analysis is based on a sample of listed U.S. firms from annual Compustat over the period of 1975–2018. We use a sample selection procedure similar to that in Peters and Taylor (2017) and Lin, Palazzo, and Yang (2020). In particular, we exclude firms whose SIC code is between 4900 and 4999 (utility or regulated firms), between 6000 and 6999 (financial firms), or greater than 9000 (government agencies etc.). We exclude firms operating in R&D-intensive sectors (SIC codes 737, 384, 382, 367, 366, 357, and 283).¹⁴ We winsorize all variables at 1% and 99% levels to mitigate the impact of outliers. We drop all observations

¹⁴Our empirical results are robust to including R&D-intensive industries; see Subsection III.D.

with missing values on one or more variables of interest. We then remove observations with a market-to-book ratio larger than 20, negative book equity or negative EBITDA. Our final sample consists of 69,054 firm-year observations with 5,984 unique firms.

Our model predicts that debt levels and maturity should decrease with capital age (a), while the length of debt cycles and average debt maturity should increase with the useful life of assets (n). To test these predictions, we need measures of a firm’s capital age and the useful life of its assets. We follow prior research to construct these measures. We construct our measure of capital age as in [Salvanes and Tveteras \(2004\)](#) and [Lin et al. \(2020\)](#). In particular, we first calculate net and gross investment for firm i at time t , respectively, as:

$$I_{i,t}^{net} = ppent_{i,t+1} - ppent_{i,t} \quad \text{and} \quad I_{i,t}^{gross} = \delta_{i,t+1}ppent_{i,t} + I_{i,t}^{net},$$

where $ppent_{i,t}$ refers to net PP&E and $\delta_{i,t}$ is the BEA industry economic depreciation rate assigned to firm i at time t .¹⁵ Capital age $CA_{i,t}$ is then defined as:

$$CA_{i,t} = \begin{cases} (CA_{i,t-1} + 1) \times \frac{(1-\delta_{i,t})ppent_{i,t-1}}{ppent_{i,t}} + \frac{I_{i,t-1}^{gross}}{ppent_{i,t}} & \text{if } I_{i,t-1}^{gross} > 0, \\ CA_{i,t-1} + 1 & \text{otherwise.} \end{cases}$$

When the firm has positive gross investment in the previous period, capital age is a weighted average of the old capital, which ages one year, and new capital, which is one year old. The respective weights of old and new capital, $(1 - \delta_{i,t})ppent_{i,t-1}/ppent_{i,t}$ and $I_{i,t-1}^{gross}/ppent_{i,t}$, reflect the corresponding shares of the old and new capital in this period’s total capital. When gross investment is negative, we assume that all capital vintages are disposed of in an equal way so that capital ages by one year. We initialize the firm–level measure of capital age by calculating the ratio of accumulated depreciation and amortization ($dpact_{i,0}$) to current depreciation and amortization ($dpc_{i,0}$) from Compustat. Subsection [III.D](#) shows that our main results are robust to using alternative measures of capital age.

¹⁵We match this variable to Compustat using the linking table provided by the BEA, which exploits the NAICS industry classification. In robustness tests, we recompute our measure using the accounting depreciation from Compustat, i.e. $\delta_{i,t} = dpc_{i,t}/ppent_{i,t}$ and obtain similar results. See Subsection [III.D](#).

Panel A: Summary statistics								
	Capital age	Useful life	ND/EBITDA	Net book leverage	Net mkt. leverage	% debt mat.> 3y	% debt mat.> 5y	Debt mat. (yr.)
Mean	6.807	13.109	2.244	0.190	0.224	0.521	0.328	6.233
Standard deviation	3.208	5.666	4.194	0.226	0.263	0.328	0.302	4.706
Q1	4.418	9.000	0.318	0.051	0.041	0.230	0.006	3.227
Median	6.374	13.000	1.445	0.201	0.200	0.585	0.294	5.079
Q3	8.704	17.000	3.045	0.341	0.397	0.796	0.570	7.669
N	69054	63413	69054	69054	69054	69054	69054	16689

Panel B: Within-firm pairwise correlations								
	Capital age	Useful life	ND/EBITDA	Net book leverage	Net mkt. leverage	% debt mat.> 3y	% debt mat.> 5y	Debt mat. (yr.)
Capital age	1							
Useful life	0.247	1						
ND/EBITDA	-0.042	-0.0020	1					
Net book lev.	-0.143	-0.084	0.507	1				
Net mkt. lev.	-0.120	-0.063	0.519	0.843	1			
% debt mat.> 3y	-0.099	0.0015	0.033	0.139	0.078	1		
% debt mat.> 5y	-0.122	0.010	0.016	0.086	0.049	0.639	1	
Debt mat. (yr.)	-0.073	-0.004	0.0023	0.016	-0.001	0.178	0.222	1

Table 1: **Summary statistics: capital age and financing.** The table contains the summary statistics of capital age, the useful life of assets, and the financing variables. These include three measures of net leverage: net debt to EBITDA, net book leverage, net market leverage and three measures of debt maturity: the ratios of debt maturing in more than 3 or 5 years to total debt as well as the debt maturity from Capital IQ. Panel A contains the summary statistics and Panel B contains the within-firm pairwise correlations between the respective variables. All variables are defined in Table [A.1](#).

To measure of the useful life of assets, we follow the empirical literature which relies on deflating gross PP&E by current depreciation (Stohs and Mauer, 1996; Custódio et al., 2013; Livdan and Nezlobin, 2021). We proxy for the useful life of firm i 's assets at time t by

$$UL_{i,t} = \left\| \frac{ppeg_{i,t} + ppeg_{i,t-1}}{2dpc_{i,t}} \right\|,$$

where $\| \cdot \|$ rounds to the nearest integer, $ppeg_{i,t}$ refers to gross PP&E, and $dpc_{i,t}$ is current depreciation and amortization. The measure is justified by the observation that firms largely use straight-line depreciation rule for their fixed assets and reflects the number of years needed to fully depreciate the capital stock, which is time invariant in the model. As in Livdan and Nezlobin (2021), we cap the measure at 25 years.¹⁶ We also show that our results are robust to using alternative measures of useful life.

We test the model predictions on financing using three measures of leverage: net debt to EBITDA, net book leverage, and net market leverage. Net debt to EBITDA is the main variable of interest as our model generates specific predictions with respect to this measure of indebtedness, which is also the most commonly used measure in practice (Lian and Ma, 2021; Graham, 2022). We additionally present results using net book leverage and net market leverage as dependent variables as this allows us to verify that our mechanism also applies to measures of leverage commonly used in the academic literature. We test the predictions on debt maturity using the ratios of debt maturing in more than 3 and 5 years to total debt (as in Custódio et al., 2013) and debt maturity from Capital IQ (as in Choi et al., 2018), which we refer to as debt maturity in our analysis. Summary statistics for our measures of capital age and useful life of assets and for the dependent variables are presented in Table 1. Appendix C provides the definitions and summary statistics of all the variables.

Panel A of Table 1 shows that average capital age in our sample equals 6.81 years, which is close to the value of 5.7 years in Lin et al. (2020). Moreover, capital age exhibits substantial

¹⁶Note that the measure of useful life is calculated using a different variable for depreciation than that used in the measure of capital age. This is because we want to be as close as possible to the definitions proposed in existing literature. Moreover, BEA reports geometric depreciation rates, which cannot be easily used to impute the useful life of the asset relative to the straight-line depreciation assumptions from Compustat.

variation across firms, with a standard deviation of 3.2 years. The average useful life of assets is 13.1 years, similar to the value of 12.6 years in [Livdan and Nezlobin \(2021\)](#), which suggests that average capital age equals half of the useful life of assets, as in the model. Sample firms have an average net debt to EBITDA ratio of 2.2, net book leverage ratio of 19% and, net market leverage ratio of 22.4%. On average, 52.1% (32.8%) of their debt is maturing in more than 3 (5) years. The average debt maturity from Capital IQ is 6.2 years, in line with prior studies (e.g., [Choi et al., 2018](#)) and close to average capital age.

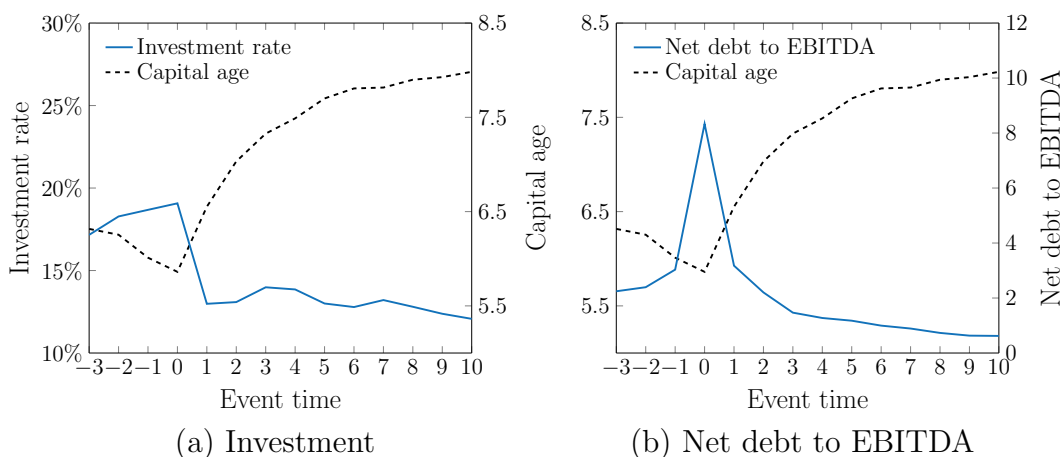


Figure 6: Debt cycles: Peak to through. The figure presents the dynamics of average capital age, investment, and net debt to EBITDA around a net debt to EBITDA peak, defined for each firm as the year in which net debt to EBITDA reaches its maximum value. Event time $t = 0$ indicates the net debt to EBITDA peak. We only include debt cycles with at least 3 years from peak to trough, defined as the year in which net debt to EBITDA is at its minimum value for each firm. All variables are defined in [Table A.1](#).

Panel B of [Table 1](#) shows the within-firm correlations between the variables of interest. As hinted by [Figure 1](#), net leverage and debt maturity are negatively correlated with capital age while debt maturity is positively correlated with the useful life of assets.

Before formally testing the model predictions, we illustrate our mechanism with [Figure 6](#), which shows the evolution of capital age, net debt to EBITDA, and investment around leverage peaks. Event time $t = 0$ indicates the peak of the debt cycle, i.e. the time when each firm attains its highest net debt to EBITDA ([DeAngelo et al., 2018](#)). [Figure 6](#) shows

that capital age is the lowest after a peak in leverage, indicating that firms have replaced old capital. Over time, capital age increases while net debt to EBITDA decreases. Leverage peaks occur after investment peaks have led to the replacement of old capital.

B Financing Cycles: Within-Firm Evidence

To formally test Prediction 1 on the relation between leverage ratios and capital age, we estimate fixed-effect leverage regression models while controlling for standard determinants of leverage. Notably, we run regressions of the form

$$Lev_{i,j,t+1} = \phi CA_{i,t} + \beta X_{i,t} + \eta_i + \gamma_{t+1} + \kappa_{j,t+1} + \varepsilon_{i,t+1},$$

where $Lev_{i,j,t+1}$ is the net leverage of firm i in industry j , and the vector of controls $X_{i,t}$ includes profitability, size, market-to-book, tangibility, cash flow volatility, R&D, and firm age (Lemmon et al., 2008). All specifications include firm fixed effects η_i and year fixed effects γ_t to account for time-invariant firm heterogeneity and time-varying factors common to all firms, respectively. Some specifications additionally include industry-year fixed effects $\kappa_{j,t}$ to control for industry-level shocks that can drive investment and leverage, where we use the Hoberg-Phillips fixed industry classification with 100 industries (Hoberg and Phillips, 2010, 2016). We cluster standard errors at the firm level.

The main parameter of interest in these tests is the parameter ϕ , which we expect ϕ to be negative according to Prediction 1. Table 2 presents the estimates for net debt to EBITDA (columns 1 to 3), net book leverage (columns 4 to 6) and net market leverage (columns 7 to 9). The results confirm the sign of the univariate correlations from Table 1: capital age and leverage are negatively related, even when including standard explanatory variables and controlling for fixed effects. In particular, a one standard deviation increase in capital age is associated with a 0.404 drop in net debt to EBITDA ratio, corresponding to a 18% reduction relative to the mean. Columns 6 and 9 shows that it is also associated with a 3.3 percentage point lower net book leverage ratio and a 3.4 percentage point lower net market leverage ratio, corresponding to a reduction of 17.4% and 15.2% relative to their mean. In

unreported results, we find that capital age provides economically meaningful incremental explanatory power for leverage even when taking into account its standard determinants, as the adjusted within R^2 increases by 10%, 26% and 10% for net debt to EBITDA, net book leverage, and net market leverage, respectively, when including capital age in the specification.¹⁷ Additionally, in Panel A of Table IA.1 in the Internet Appendix we carry out an analysis of the importance of different determinants of leverage similar to that in Frank and Goyal (2009). Capital age is by and large the most important leverage factor in terms of explanatory power.

To investigate the relation between debt maturity and capital age, we follow the approach of Custódio et al. (2013) and Choi et al. (2018) and estimate maturity regressions of the form

$$Mat_{i,j,t+1} = \phi CA_{i,t} + \beta X_{i,t} + \eta_i + \gamma_{t+1} + \kappa_{j,t+1} + \varepsilon_{i,t+1},$$

where $Mat_{i,j,t+1}$ is maturity of debt of firm i in industry j , $X_{i,t}$ is the vector of controls, and η_i , γ_t , $\kappa_{j,t}$ are firm, year, and industry-year fixed effects. Here again, the main parameter of interest is the parameter ϕ , which we expect to be negative according to Prediction 4.

Table 3 presents the resulting estimates for the share of debt maturing in more than 3 years (columns 1 to 3), the share of debt maturing in more than 5 years (columns 4 to 6), and debt maturity from Capital IQ (columns 7 to 9). In line with Prediction 4, capital age and debt maturity are negatively related. A one standard deviation increase in capital age is associated with a 0.441 year lower debt maturity and with a 2.9 (respectively 2.0) percentage point lower share of debt maturing in 3 (respectively 5) years. The negative correlation is robust to controlling for typical determinants of debt maturity. Furthermore, the economic effect is significant, as capital age also provides additional explanatory power: the adjusted within R^2 respectively increases by 33%, 49%, and 39% for debt maturing in more than 3 years, 5 years, and for debt maturity.¹⁸ Finally, the fact that capital age is significant while asset maturity is not, is consistent with our model prediction that asset maturity is mainly a time-invariant firm characteristic while capital age can predict financing decisions.

¹⁷We compare the adjusted R^2 when adding capital age to the models in columns 2, 5, and 8 in Table 2.

¹⁸We compare the adjusted R^2 when adding capital age to the models in columns 2, 5, and 8 in Table 3.

	ND/EBITDA			Net book leverage			Net market leverage		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Capital age	-0.431*** (-11.67)	-0.371*** (-8.51)	-0.404*** (-7.14)	-0.041*** (-17.15)	-0.034*** (-11.65)	-0.033*** (-9.37)	-0.042*** (-14.87)	-0.033*** (-10.23)	-0.034*** (-8.83)
Profitability		-0.825*** (-21.96)	-0.740*** (-16.14)		-0.034*** (-17.82)	-0.029*** (-12.40)		-0.050*** (-23.55)	-0.046*** (-17.96)
Size		0.491*** (4.19)	0.557*** (3.40)		0.051*** (6.28)	0.062*** (6.53)		0.085*** (10.06)	0.101*** (9.73)
Market-to-book		-0.062* (-1.91)	-0.043 (-1.16)		-0.009*** (-4.02)	-0.011*** (-4.35)		-0.027*** (-12.20)	-0.024*** (-9.84)
Tangibility		0.366*** (4.83)	0.377*** (3.75)		0.037*** (7.06)	0.037*** (6.16)		0.046*** (8.20)	0.042*** (6.32)
Cash flow volatility		-0.023 (-0.71)	-0.032 (-0.90)		-0.003* (-1.73)	-0.001 (-0.60)		-0.003* (-1.83)	-0.000 (-0.05)
R&D		-0.108* (-1.84)	0.009 (0.13)		-0.006 (-1.51)	0.000 (0.02)		-0.008** (-1.97)	0.001 (0.26)
Firm age		0.133 (0.28)	0.729 (1.52)		-0.024 (-0.64)	0.031 (0.92)		-0.019 (-0.52)	0.014 (0.39)
Year FE	Yes	Yes	No	Yes	Yes	No	Yes	Yes	No
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Ind.-Year FE	No	No	Yes	No	No	Yes	No	No	Yes
Observations	56933	44335	29957	56933	44335	29957	56933	44335	29957
Adj. within R^2	0.0066	0.0459	0.0400	0.0303	0.0867	0.0815	0.0205	0.1199	0.1172

Table 2: **Capital age and leverage – within-firm regressions.** This table presents estimates from regressions of net debt to EBITDA and net leverage ratios on lagged capital age. The dependent variable is *Net debt to EBITDA* in columns 1 to 3; *Net book leverage* in columns 4 to 6 and *Net market leverage* in columns 7 to 9. Each explanatory variable is standardized by its full-sample standard deviation. The models in columns 3, 6 and 9 include industry-year fixed effects created using Hoberg-Phillips fixed industry classification with 100 industries. All variables are defined in Table A.1. t -statistics are reported in parentheses. Standard errors are clustered at the firm level. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p-values.

	% debt maturing > 3y			% debt maturing > 5y			Debt maturity (yr.)		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Capital age	-0.039*** (-13.52)	-0.030*** (-8.43)	-0.029*** (-6.04)	-0.032*** (-10.34)	-0.025*** (-6.55)	-0.020*** (-4.12)	-0.301** (-2.36)	-0.390*** (-2.81)	-0.441*** (-2.76)
Size		0.100*** (3.44)	0.175*** (4.56)		0.019 (0.69)	0.059* (1.73)		3.165*** (2.85)	4.360*** (3.06)
Size squared		-0.048* (-1.80)	-0.115*** (-3.29)		0.024 (0.92)	-0.001 (-0.02)		-2.544** (-2.17)	-3.487** (-2.41)
Market-to-book		0.006** (2.09)	0.006 (1.48)		0.005* (1.71)	0.001 (0.18)		0.070 (0.66)	0.054 (0.44)
Asset maturity		0.005 (1.12)	0.002 (0.32)		0.006 (1.40)	0.002 (0.31)		0.164 (1.31)	0.182 (1.25)
Abnormal earnings		0.003** (2.55)	0.002 (1.27)		0.003*** (3.46)	0.004*** (3.32)		0.016 (0.52)	0.037 (0.92)
Cash flow volatility		0.000 (0.12)	0.003 (0.85)		-0.001 (-0.58)	0.003 (0.81)		-0.098 (-1.42)	-0.015 (-0.18)
R&D		-0.005 (-0.91)	-0.008 (-1.09)		-0.005 (-0.88)	-0.006 (-0.77)		0.096 (0.51)	0.025 (0.11)
Net book leverage		0.030*** (8.12)	0.038*** (7.96)		0.015*** (4.14)	0.016*** (3.49)		0.054 (0.55)	0.080 (0.74)
Firm age		-0.041 (-0.89)	-0.009 (-0.19)		-0.077 (-1.42)	-0.022 (-0.35)		3.245** (1.96)	2.732 (1.51)
Year FE	Yes	Yes	No	Yes	Yes	No	Yes	Yes	No
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Ind.-Year FE	No	No	Yes	No	No	Yes	No	No	Yes
Observations	56933	43253	29030	56933	43253	29030	13870	11542	10295
Adj. within R^2	0.0090	0.0173	0.0179	0.0067	0.0103	0.0082	0.0015	0.0068	0.0077

Table 3: **Capital age and debt maturity – within-firm regressions.** The table presents estimates from regressions of debt maturity on lagged capital age. The dependent variable is *% of debt maturing in > 3 years* in columns 1 to 3; *% of debt maturing in > 5 years* in columns 4 to 6; and *Debt maturity (yr.)* in columns 7 to 9. Each explanatory variable is standardized by its full-sample standard deviation. Models in columns 3, 6 and 9 include industry-year fixed effects created using Hoberg-Phillips fixed industry classification with 100 industries. All variables are defined in Table A.1. t -statistics are reported in parentheses. Standard errors are clustered at the firm level. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.

In Panel B of Table IA.1 in the Internet Appendix, we carry out an analysis of the importance of the factors that we use in our debt maturity regressions, following the approach of Frank and Goyal (2009). We find that capital age carries the second most explanatory power after net book leverage.

C Financing Cycles: Exploring the Mechanism

Having established that capital age plays an important role in explaining within-firm variation in net leverage and debt maturity (Predictions 1 and 4), we further analyze the mechanism by investigating the effects of the lumpiness of investment, the return on investment and firm size on our results.

We first analyze the role of investment lumpiness. According to Prediction 3, we expect that financing is more sensitive to capital age when investment is lumpier. To test the hypothesis, we split firms into terciles based on two proxies of investment lumpiness—the firm-level skewness and kurtosis of investment. We then run regressions of net leverage and debt maturity on lagged capital age interacted with indicators for each tercile.¹⁹ Panel A and B of Table 4 present the resulting estimates and confirm the negative relations between capital age and both leverage and debt maturity documented in Tables 2 and 3. In addition, they confirm the implications of Prediction 3 by showing that the effects become monotonically stronger as investment lumpiness increases. In fact, Panels A and B show that the effects are more than doubled when moving from the lowest to the highest tercile and that this difference is statistically significant. For example, when measuring lumpiness with skewness, a one standard deviation increase in capital age is associated with a 0.548 drop in net debt to EBITDA when investment is more lumpy, but only a 0.209 drop in net debt to EBITDA when investment is less lumpy.

We next turn to analyzing the role of the return on investment. We expect that financing is less sensitive to capital age in firms with a higher return on investment (Prediction 3). We

¹⁹We do not run these interactive tests on average maturity because we only have observations for this variable for a substantially smaller subset of firms and thus the tests would not be comparable when doing the tercile splits across the different specifications.

	ND/EBITDA		Net book leverage		% debt mat. > 3y		% debt mat. > 5y	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Panel A: Investment lumpiness – Skewness								
Capital age	-0.302***	-0.209**	-0.035***	-0.023***	-0.032***	-0.019**	-0.020***	-0.008
	(-4.16)	(-2.55)	(-7.31)	(-4.60)	(-4.67)	(-2.49)	(-2.68)	(-0.97)
Capital age x Middle	-0.186**	-0.176*	-0.007	-0.006	-0.013	-0.009	-0.012	-0.012
	(-2.02)	(-1.80)	(-1.05)	(-0.93)	(-1.45)	(-1.02)	(-1.23)	(-1.15)
Capital age x High	-0.370***	-0.339***	-0.015**	-0.018***	-0.017*	-0.016*	-0.017*	-0.021**
	(-3.62)	(-3.11)	(-2.31)	(-2.68)	(-1.96)	(-1.68)	(-1.91)	(-2.02)
Controls	No	Yes	No	Yes	No	Yes	No	Yes
Observations	34213	29718	34213	29718	34213	28805	34213	28805
Adj. within R^2	0.0102	0.0415	0.0319	0.0831	0.0083	0.0183	0.0050	0.0087
Panel B: Investment lumpiness – Kurtosis								
Capital age	-0.250***	-0.207**	-0.033***	-0.026***	-0.040***	-0.030***	-0.025***	-0.015*
	(-3.14)	(-2.21)	(-6.84)	(-4.85)	(-5.73)	(-3.53)	(-3.46)	(-1.74)
Capital age x Middle	-0.252***	-0.136	-0.007	0.001	0.001	0.004	-0.006	-0.008
	(-2.64)	(-1.29)	(-1.12)	(0.20)	(0.16)	(0.36)	(-0.63)	(-0.74)
Capital age x High	-0.432***	-0.354***	-0.018***	-0.017**	-0.007	-0.001	-0.007	-0.006
	(-4.12)	(-3.07)	(-2.77)	(-2.53)	(-0.74)	(-0.05)	(-0.76)	(-0.55)
Controls	No	Yes	No	Yes	No	Yes	No	Yes
Observations	34213	29718	34213	29718	34213	28805	34213	28805
Adj. within R^2	0.0105	0.0416	0.0322	0.0834	0.0079	0.0182	0.0047	0.0086

test this prediction in the same manner as for investment lumpiness by running regressions of net leverage and debt maturity on lagged capital age interacted with indicators for firms split into terciles based on their return on investment. The resulting estimates are presented in Panel C of Table 4 and show that the effects of capital age on firm financing are monotonically decreasing in the return on investment, in line with Prediction 3. For example, specifications (1) and (2) of Panel C show that roughly two-thirds of the effect is removed when moving from the lowest to the highest tercile and that the difference is statistically significant. In particular, a one standard deviation increase in capital age is associated with a 0.643 drop in net debt to EBITDA when the return on investment is low, but only a 0.191 drop in net debt to EBITDA when the return on investment is high.

Lastly, we investigate the effects of firm size, with the expectation that larger firms are more likely to have more divisible capital (e.g., multiple factories built at different times) and weaker financing cycles as illustrated by Figure 4. In line with this intuition, Panel D

	ND/EBITDA		Net book leverage		% debt mat. > 3y		% debt mat. > 5y	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Panel C: Return on investment								
Capital age	-0.697***	-0.643***	-0.046***	-0.038***	-0.042***	-0.032***	-0.034***	-0.029***
	(-9.75)	(-7.55)	(-12.73)	(-9.31)	(-8.65)	(-5.72)	(-6.66)	(-5.00)
Capital age x Middle	0.289***	0.322***	0.002	0.003	-0.002	0.005	0.002	0.009*
	(4.88)	(4.85)	(0.62)	(1.22)	(-0.54)	(0.92)	(0.44)	(1.70)
Capital age x High	0.408***	0.452***	0.013***	0.014***	0.002	0.009	0.010*	0.020***
	(5.88)	(5.73)	(3.38)	(3.44)	(0.34)	(1.38)	(1.89)	(3.20)
Controls	No	Yes	No	Yes	No	Yes	No	Yes
Observations	34915	29957	34915	29957	34915	29030	34915	29030
Adj. within R^2	0.1128	0.1168	0.0609	0.0968	0.0093	0.0195	0.0056	0.0096
Panel D: Firm size								
Capital age	-0.593***	-0.612***	-0.050***	-0.049***	-0.042***	-0.040***	-0.031***	-0.031***
	(-7.28)	(-6.52)	(-10.08)	(-8.83)	(-6.41)	(-5.09)	(-5.09)	(-4.38)
Capital age x Middle	0.214**	0.273***	0.017***	0.020***	0.010	0.016*	0.007	0.010
	(2.49)	(2.85)	(3.15)	(3.46)	(1.28)	(1.76)	(1.02)	(1.17)
Capital age x High	0.211**	0.364***	0.021***	0.031***	0.017**	0.026***	0.022**	0.030***
	(2.28)	(3.61)	(3.55)	(4.76)	(2.02)	(2.74)	(2.57)	(3.26)
Controls	No	Yes	No	Yes	No	Yes	No	Yes
Observations	34915	29957	34915	29957	34915	29030	34915	29030
Adj. within R^2	0.0126	0.0421	0.0485	0.0946	0.0182	0.0238	0.0157	0.0162

Table 4: **Exploring the mechanism.** This table presents estimates from regressions of net leverage variables and debt maturity on lagged capital age interacted with indicators for firms split into terciles by the proxies of investment lumpiness (the firm-level investment skewness, Panel A; and firm-level investment kurtosis, Panel B), the return on investment (EBITDA divided by book assets, Panel C), and firm size (book assets, Panel D). The lowest tercile is the baseline group. *Middle* and *High* indicate the middle and highest terciles of each splitting variable. The dependent variables are *Net debt to EBITDA*, *Net Book Leverage*, *% of debt maturing in > 3 years*, and *% of debt maturing in > 5 years*. Each explanatory variable is standardized by its full-sample standard deviation. Specifications 2, 4, 6 and 8 control for all independent variables from Tables 2 for net leverage and 3 for debt maturity. All specifications include indicators for the middle and high terciles. All models include firm and industry-year fixed effects created using the Hoberg-Phillips fixed industry classification with 100 industries. t -statistics are reported in parentheses. Standard errors are clustered at the firm level. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p-values.

shows that the effects of capital age on leverage and debt maturity are indeed the strongest among the smallest firms. As firm size increases, the effects become monotonically weaker (except in specification (1)) with magnitudes that are halved between the lowest and the highest tercile of firm size.

D Robustness

We next conduct robustness tests by examining the effects of the sample composition, the definition of depreciation, and the measure of capital age on our results. In each robustness test, we replicate the regression models from Subsection III.B while controlling for all the determinants of net leverage and debt maturity as well as firm and industry-year fixed effects (i.e., the comparable results can be found in columns 3, 6 and 9 in Tables 2 and 3).

First, in Panel A of Table 5, we show that the effect of capital age on net leverage and debt maturity remains quantitatively similar when including in the sample firms that operate in R&D-intensive sectors (SIC codes 737, 384, 382, 367, 366, 357, and 283).

Second, in Panels B and C of in Table and 5 we document that the effect of capital age on net leverage and debt maturity remains quantitatively similar when changing the definition of the depreciation rate. We do so by calculating capital age using the accounting depreciation rate implied by Compustat instead of the BEA industry economic depreciation rate. In Panel B we compute the depreciation rate as $\delta_{i,t}^1 = dpc_{i,t}/ppent_{i,t}$, that is the depreciation expense over net property, plant and equipment. In Panel C, we calculate the depreciation rate as $\delta_{i,t}^2 = (dpc_{i,t} - am_{i,t})/ppent_{i,t}$, i.e. the depreciation expense minus amortization of intangibles over net property, plant and equipment. The results presented in Panels B and C of Table 5 indicate that using the accounting depreciation rate from Compustat rather than the economic depreciation rate from BEA does not materially affect our results, neither statistically nor economically.

Third, we show in Table 6 that the results are robust to using different measures of capital age. We consider three alternative measures. In Panel A, we modify our baseline measure by assuming that the firm first disposes of the oldest capital vintages when disinvesting. In contrast, our baseline measure assumes that *all* vintages are equally affected (Lin et al., 2020). In Panel B, we proxy capital age by the ratio of accumulated ($dpact$) to current depreciation (dpc). In Panel C, we follow Ai, Croce, and Li (2012) and use the weighted average age of firms' capital vintages over the past $T = 7$ years to measure capital age. As suggested by the summary statistics in Table A.2, all alternative measures of capital age have means and standard deviations comparable to those of our original measure. Moreover, the

pairwise correlation coefficient between the baseline and alternative measures ranges from 0.44 to 0.79.²⁰ Overall, the results in Table 6 illustrate that changing capital age proxy does not materially affect the economic and statistical significance of the results.

Lastly, in Table IA.2 of the [Internet Appendix](#), we show that our results are robust to changing the industry definition, by using the Hoberg-Phillips fixed industry classification with 50 industries and the Fama-French industry classification with 49 industries.

E Financing Cycles: Cross-Sectional Evidence

We next turn to the cross-sectional predictions of the model that firms with longer-lived assets should follow longer debt cycles (Prediction 2) and have a higher average debt maturity (Prediction 5). We proxy for the useful life of assets using the ratio of the book value of its physical assets to its depreciation costs. This measure is a proxy for the economic life of the firm’s assets and does not directly depend on capital adjustment costs. Indeed, the measure captures the number of years to fully depreciate the capital stock and does not rely on when the firm actively chooses to replace it. For robustness, we also use alternative measures of asset life including the average of the capital age, the asset maturity (calculated as in [Stohs and Mauer \(1996\)](#) and [Custódio et al. \(2013\)](#)), and the asset maturity capped at 25 years.

To test the first prediction, we need to obtain a measure of the length of a firm’s financing cycle. To do so, we define a leverage spike as an instance in which the firm’s net debt to EBITDA ratio exceeds its firm-specific median by one standard deviation. The length of the cycle is then the number of years between the first observation and the first spike, between consecutive leverage spikes, or between the last spike and the end of the sample period for the given firm, conditional on a minimum of three years between spikes and three years of observations around the spike (in Table IA.4 of the [Internet Appendix](#) we show that the results are robust to using a 5-year filter.). Firms that do not have at least one spike are excluded. We then average the useful life of assets and the length of the cycles for each

²⁰The measure of [Ai et al. \(2012\)](#) differs the most as it requires at least 7 years of continuous investment data to calculate capital age. This reduces the overall sample size. While calculating this measure with $T = 10$ or $T = 15$ yields a capital age proxy with a mean closer to that of the remaining measures, it results in having substantially fewer observations, which affects the statistical power of our tests.

firm in our sample. To test the second prediction, we examine the relationship between the average debt maturity and the average useful life of assets. The bottom panels in Figure 1 show that both the debt cycle length and the average debt maturity are increasing in the firm’s average useful life.

To formally test the model predictions, we run cross-sectional regressions of the form

$$Cycle_i = \alpha + \phi UL_i + \beta X_i + \varepsilon_i,$$

where $Cycle_i$ is either the maximum or the average length of the cycle of firm i , UL_i is the average useful life of firm i ’s asset, and X_i is a vector of average firm-level controls analogous to the controls in the within-firm tests in Table 2. We cluster standard errors at the industry level using the Hoberg-Phillips fixed industry classification with 100 industries. The main parameter of interest is the parameter ϕ , which we expect to be positive.

Table 7 presents the resulting estimates for the maximum debt cycle lengths (columns 1 to 2) and the average debt cycle length (columns 3 to 4). The results suggest a strong positive association between the cycle length and the firm’s average asset life, consistent with Prediction 2, and are robust to controlling for common determinants of leverage. A one-year increase in asset life is associated with a roughly one-month increase in the average debt cycle length, depending on the specification. Moreover, the results are similar and robust to using other alternative measures of asset life (Panels B to D). Thus, consistent with Prediction 2, firms with longer-lived assets have longer debt cycles.

To test Prediction 5, namely that the average useful life is positively associated with the average debt maturity, we regress the firm-level averages of the debt maturity measures on the average useful life of the assets. Formally, we run cross-sectional regressions of the form

$$Mat_i = \alpha + \phi UL_i + \beta X_i + \varepsilon_i,$$

where Mat_i is the average of the debt maturity for firm i , and X_i is a vector of average firm-level controls analogous to the controls in the within-firm tests in Table 3. Here again, the main parameter of interest is the parameter ϕ , which we expect to be positive.

Panel A: Including R&D-intensive industries						
	ND/EBITDA	Net book lev.	Net market lev.	% debt mat. > 3y	% debt mat. > 5y	Debt mat. (yr.)
Capital age	-0.412*** (-8.10)	-0.034*** (-10.54)	-0.034*** (-9.88)	-0.029*** (-6.59)	-0.020*** (-4.57)	-0.476*** (-3.31)
Observations	38256	38256	38256	37211	37211	13109
Adj. within R^2	0.0353	0.0857	0.1007	0.0162	0.0078	0.0066

Panel B: Capital age calculated using Compustat depreciation rate						
	ND/EBITDA	Net book lev.	Net market lev.	% debt mat. > 3y	% debt mat. > 5y	Debt mat. (yr.)
Capital age	-0.339*** (-5.86)	-0.029*** (-7.96)	-0.029*** (-7.54)	-0.025*** (-5.31)	-0.017*** (-3.42)	-0.362** (-2.41)
Observations	29848	29848	29848	28954	28954	10192
Adj. within R^2	0.0389	0.0767	0.1134	0.0170	0.0075	0.0071

Panel C: Capital age calculated using Compustat depreciation rate excluding amortization						
	ND/EBITDA	Net book lev.	Net market lev.	% debt mat. > 3y	% debt mat. > 5y	Debt mat. (yr.)
Capital age	-0.341*** (-5.81)	-0.029*** (-7.91)	-0.029*** (-7.48)	-0.028*** (-5.72)	-0.018*** (-3.56)	-0.379** (-2.47)
Observations	29848	29848	29848	28954	28954	10192
Adj. within R^2	0.0390	0.0767	0.1133	0.0175	0.0076	0.0072

Table 5: **Capital age and financing – alternative sample and different definition of depreciation rates.** This table presents estimates from regressions of net debt to EBITDA, net leverage ratios and debt maturity on lagged capital age when changing the sample construction by keeping R&D-intensive firms (Panel A) and when capital age is calculated using alternative definitions of the depreciation rate (depreciation expense over net property, plant and equipment in Panel B and depreciation expense minus amortization of intangibles over net property, plant and equipment in Panel C). We control for all independent variables from Table 2 in leverage regressions and from Table 3 in debt maturity regressions. Each explanatory variable is standardized by its full-sample standard deviation. All specifications include firm, and industry-year fixed effects, created using Hoberg-Phillips fixed industry classification with 100 industries. All variables are defined in Table A.1. t -statistics are reported in parentheses. Standard errors are clustered at the firm level. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.

Panel A: Capital age calculated by disposing of oldest capital vintages first						
	ND/EBITDA	Net book lev.	Net market lev.	% debt mat. > 3y	% debt mat. > 5y	Debt mat. (yr.)
Capital age	-0.290*** (-6.36)	-0.025*** (-8.52)	-0.027*** (-8.75)	-0.021*** (-4.55)	-0.018*** (-3.97)	-0.125 (-0.76)
Observations	28750	28750	28750	27871	27871	9822
Adj. within R^2	0.0396	0.0767	0.1170	0.0162	0.0083	0.0061

Panel B: Capital age calculated as accumulated to current depreciation						
	ND/EBITDA	Net book lev.	Net market lev.	% debt mat. > 3y	% debt mat. > 5y	Debt mat. (yr.)
Capital age	-0.300*** (-6.08)	-0.028*** (-9.07)	-0.029*** (-8.46)	-0.015*** (-2.61)	-0.012** (-2.05)	-0.074 (-0.44)
Observations	29686	29686	29686	28792	28792	10203
Adj. within R^2	0.0389	0.0797	0.1162	0.0155	0.0070	0.0053

Panel C: Capital age proxy based on Ai et al. (2012) with $T = 7$						
	ND/EBITDA	Net book lev.	Net market lev.	% debt mat. > 3y	% debt mat. > 5y	Debt mat. (yr.)
Capital age	-0.126*** (-3.32)	-0.007*** (-3.29)	-0.007*** (-3.08)	-0.007** (-2.09)	-0.005 (-1.42)	-0.196** (-2.10)
Observations	25774	25774	25774	25020	25020	9200
Adj. within R^2	0.0347	0.0646	0.1043	0.0152	0.0062	0.0055

Table 6: **Capital age and financing – alternative measures of capital age.** This table presents estimates from regressions of net debt to EBITDA, net leverage ratios and debt maturity on alternative measures of lagged capital age (by assuming that firms dispose of oldest capital vintages first in Panel A, by proxying capital age as the ratio of accumulated (*dpact*) to current depreciation (*dpc*) in Panel B and by calculating capital age as the weighted average age of firms’ capital vintages as in [Ai et al. \(2012\)](#) over the past $T = 7$ years in Panel C). We control for all independent variables from Table 2 in leverage regressions and from Table 3 in debt maturity regressions. Each explanatory variable is standardized by its full-sample standard deviation. All specifications include firm, and industry-year fixed effects, created using Hoberg-Phillips fixed industry classification with 100 industries. All variables are defined in Table A.1. t -statistics are reported in parentheses. Standard errors are clustered at the firm level. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.

	Max debt cycle		Avg. debt cycle	
	(1)	(2)	(3)	(4)
Panel A: Useful life				
Useful life	0.183*** (5.93)	0.110*** (4.31)	0.114*** (4.91)	0.085*** (4.30)
Controls	No	Yes	No	Yes
Observations	2405	2376	2405	2376
Adj. R^2	0.026	0.237	0.016	0.161
Panel B: Average capital age				
Capital age	0.685*** (10.95)	0.205*** (5.29)	0.433*** (10.97)	0.145*** (4.67)
Controls	No	Yes	No	Yes
Observations	2407	2378	2407	2378
Adj. R^2	0.089	0.238	0.058	0.160
Panel C: Asset maturity				
Asset maturity	0.050 (1.46)	0.047* (1.89)	0.027 (1.16)	0.036* (1.75)
Controls	No	Yes	No	Yes
Observations	2367	2339	2367	2339
Adj. R^2	0.004	0.232	0.002	0.156
Panel D: Asset maturity (capped at 25 years)				
Asset maturity (cap.)	0.086** (2.49)	0.107*** (3.26)	0.048** (2.05)	0.067*** (2.88)
Controls	No	Yes	No	Yes
Observations	2367	2339	2367	2339
Adj. R^2	0.009	0.234	0.004	0.157

Table 7: **Asset life and debt cycles – cross-sectional regressions.** The dependent variable is *Maximum debt cycle length* in columns 1 and 2, and *Average debt cycle length* in columns 3 and 4. Firms with no leverage spike have a cycle length that is undefined and are dropped from the sample. We require a minimum of three years between subsequent spikes. In specifications 2 and 4 we control for all independent variables from Table 2. t -statistics are reported in parentheses. Standard errors are clustered at the industry level using Hoberg-Phillips fixed industry classification with 100 industries. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.

	% debt mat. > 3y		% debt mat. > 5y		Debt maturity (yr.)	
	(1)	(2)	(3)	(4)	(5)	(6)
Panel A: Useful life						
Useful life	0.015*** (9.88)	0.010*** (8.67)	0.013*** (8.34)	0.009*** (8.65)	0.133*** (4.68)	0.092*** (3.80)
Controls	No	Yes	No	Yes	No	Yes
Observations	4272	3992	4272	3992	2415	2316
Adj. R^2	0.084	0.421	0.095	0.358	0.036	0.167
Panel B: Average capital age						
Capital age	0.021*** (6.86)	0.008*** (3.10)	0.022*** (9.62)	0.008*** (3.31)	0.239*** (5.85)	0.035 (0.82)
Controls	No	Yes	No	Yes	No	Yes
Observations	4364	3999	4364	3999	2442	2320
Adj. R^2	0.042	0.389	0.060	0.323	0.026	0.153
Panel C: Asset maturity						
Asset maturity	0.008*** (4.59)	0.007*** (13.43)	0.006*** (3.32)	0.006*** (7.89)	0.067** (2.26)	0.065*** (3.51)
Controls	No	Yes	No	Yes	No	Yes
Observations	4290	3936	4290	3936	2398	2278
Adj. R^2	0.062	0.436	0.054	0.359	0.024	0.174
Panel D: Asset maturity (capped at 25 years)						
Asset maturity (cap.)	0.012*** (8.02)	0.010*** (10.25)	0.010*** (5.54)	0.008*** (11.19)	0.102*** (3.63)	0.093*** (5.33)
Controls	No	Yes	No	Yes	No	Yes
Observations	4290	3936	4290	3936	2398	2278
Adj. R^2	0.084	0.441	0.076	0.367	0.035	0.179

Table 8: **Asset life and debt maturity – cross-sectional regressions.** The dependent variable is the average of each firm’s % of debt maturing in > 3 years in columns 1 to 2; % of debt maturing in > 5 years in columns 3 to 4; and Debt maturity (yr.) in columns 5 to 6. In specifications 2, 4 and 6 we control for all independent variables from Table 3, except for asset maturity. t -statistics are reported in parentheses. Standard errors are clustered at the industry level using the Hoberg-Phillips fixed industry classification with 100 industries. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.

Table 8 presents the resulting estimates for average % debt maturing in more than 3 years (columns 1 and 2) and 5 years (columns 3 and 4), and average debt maturity (columns 5 and 6). The results document a positive and significant relationship between the average debt maturity and the average useful life in all specifications. Moreover, the results are generally robust to using alternative measures of asset life (Panels B to D). The results are consistent with Prediction 5 that firms with longer-lived assets have longer debt maturities.

As a robustness test, we show in Table IA.3 in the Internet Appendix that our cross-sectional results for debt cycles are robust to defining them using net book leverage rather than net debt to EBITDA. Additionally, in Table IA.4 in the Internet Appendix we show that our cross-sectional results for debt cycles are robust to having a minimum of five years between subsequent spikes.

IV Conclusion

Capital ages and must eventually be replaced. This paper develops a dynamic investment and financing model to study how ageing capital generates variation in financing decisions. In this model, firms issue debt to finance investment. As capital ages, they deleverage to free up debt capacity, which allows them to replace old capital by issuing new debt. To achieve these dynamics, firms issue debt with a maturity that matches the useful life of new assets and an amortization schedule that reflects the need to free up debt capacity as capital ages. These debt dynamics lead to debt cycles and to a maturity matching theory of debt. They also imply that both leverage and debt maturity should be negatively related to capital age while both the duration of debt cycles and debt maturity should be positively related to the useful life of assets. We take the model predictions to the data and find that all our measures of leverage and debt maturity are negatively related to capital age while all measures of the duration of debt cycles or debt maturity are positively related to the useful life of assets, as predicted by the model. In addition, we find that the effects of capital age on leverage and maturity are stronger in smaller firms, firms with more lumpy investment, and with a lower return on investment, in line with the model predictions.

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Appendix

The first part of the appendix derives the results for the baseline model. The second part derives the debt maturity results. The third part defines the variables used in the empirical analysis.

A Baseline Model

We impose the following parameter restrictions. First we assume that

$$\pi > rK \left(1 + \frac{1}{r} \frac{\rho_C}{(1 + \rho_C)^n - 1} \right), \quad (\text{A.1})$$

which ensures that investing is positive NPV for an unlevered firm. Second, we assume that

$$\begin{aligned} \phi &\geq \underline{\phi} = \frac{\max\{K - C_0, 0\}}{\pi}, & (\text{A.2}) \\ \phi &< \bar{\phi} = \min \left\{ \frac{1}{r} - \frac{K}{\pi} \left(1 + \frac{1}{r} \frac{\rho_C}{(1 + \rho_C)^n - 1} \right), \frac{1}{\rho_D} \left(1 - \frac{K}{\pi} \frac{\rho_C(1 + r)^n + r(1 + \rho_C)^n - r}{(1 + \rho_C)^n - 1} \right) \right\}. & (\text{A.3}) \end{aligned}$$

As we show below, the upper bound on ϕ ensures that debt is risk-free. The lower bound on ϕ ensures that the firm can initially purchase the asset.

The results are organized as follows. First, we show that investing is positive NPV when investment is internally financed (Lemma 1). Second, we show that this is also true when the firm can issue debt and that the firm has no incentive to default (Proposition 1). Having established that the firm invests and does not default, we derive the firm's optimal financing policy (Theorem 1). We then establish that the firm pays dividends in period $t + 1$ only if the borrowing constraint binds in period t (Lemma 2) and that the borrowing constraints binds when the firm invests (Lemma 3).

Lemma 1 (Benchmark Firm Value). *The value of a firm that retains profits to finance investment internally is given by*

$$C_0 + \frac{\pi}{r} - K \left(1 + \frac{1}{r} \frac{\rho_C}{(1 + \rho_C)^n - 1} \right).$$

Proof. If the firm saves s today and for the next $n - 1$ periods and earns a rate ρ_C on its cash balances, then the future value of its savings in $n - 1$ periods is

$$\sum_{i=0}^{n-1} s(1 + \rho_C)^i = s \frac{(\rho_C + 1)^n - 1}{\rho_C}.$$

As a result, the firm has enough savings to finance investment after n periods if

$$s = K \frac{\rho_C}{(\rho_C + 1)^n - 1}.$$

The firm earns enough to save for investment if

$$\pi - s = \pi - K \frac{\rho_C}{(\rho_C + 1)^n - 1} \geq 0,$$

This is guaranteed by restriction (A.1). The value of a firm that saves to finance investment is then given by

$$C_0 - K + \sum_{t=1}^{\infty} \frac{\pi - s}{(1+r)^t} = C_0 + \frac{\pi}{r} - K \left(1 + \frac{1}{r} \frac{\rho_C}{(1+\rho_C)^n - 1} \right),$$

which is bigger than C_0 given the restriction on K . □

Proof of Propostion 1. We want to show that the firm always invests when assets reach the end of their useful life and has no incentive to default. To do so, we assume that creditors always believe that the firm will not default and therefore charge an interest rate ρ_D on debt. We then show that, given this belief, the firm has no incentive to default and always invests so that the belief is consistent and constitutes an equilibrium.

Since the firm holds cash $C_0 > 0$ and there is no debt payment due, the firm never defaults at time $t = 0$. Furthermore, the firm never defaults when it holds a positive amount of cash as net debt is negative. Therefore, we assume in this lemma that net debt is positive, in that $ND_t > 0$. Assume now that the firm does not invest at time $t = 0$ and defaults at $t = 1$. This is suboptimal since

$$\underbrace{C_0 + D_0}_{\text{Value of firm that defaults at } t = 1} \leq C_0 + \phi\pi < \underbrace{C_0 + \frac{\pi}{r} - K \left(1 + \frac{1}{r} \frac{\rho_C}{(1+\rho_C)^n - 1} \right)}_{\text{Value of an internally financed firm}} \leq E_0$$

where the first inequality follows from the borrowing constraint and the second inequality follows from the restrictions on ϕ ; see equations (A.2) and (A.3).²¹ As a result, default can only happen for $t > 1$.

Assume that the firm has net debt $ND_t > 0$ at time $t > 0$ and defaults at time $t + 1 > 1$. If the firm has capital installed at time t and therefore produces the final good at time $t + 1$, we have that $\rho_D ND_t \leq \rho_D \phi\pi < \pi$ (see equation (A.3)). Therefore, the firm can make the

²¹We need (A.2) to hold since it ensures that the firm has enough resources to invest at time zero.

interest payment $\rho_D ND_t$ and a positive dividend payment

$$Div_{t+1} \geq \pi - \rho_D \phi \pi > 0$$

if it chooses $ND_{t+1} = ND_t$ and defaults at $t + 2$. As a result, the firm will not default if it produces the good at $t + 1$.

Assume next that the firm has no (more) installed capital at time t and does not invest so that it does not produce the good at $t + 1 > 1$ and therefore defaults at $t + 1$. Clearly, each period since the last time it invested $t' \geq t - n$ it must be that leverage is $ND_{t'} = \phi \pi$. Otherwise, the firm would benefit from increasing leverage and bringing dividend payments forward in time since $\rho_C < \rho_D < r$ and $\rho_D \phi \pi < \pi$. This also implies that the firm pays a dividend of $Div_{t'} = \pi - \rho_D \phi \pi$ for the n -periods $t' \in [t - n + 1, t]$.

Our objective is now to show that there is a profitable deviation for the firm's shareholders, namely to save for the n -periods $t' \in [t - n + 1, t]$ and invest at time t and thereby avoid default at $t + 1$. If instead of paying dividends, the firm saves $s < \pi - \rho_D \phi \pi$ each period after the last time it invested ($t' \in [t - n + 1, t]$) and puts this money in a savings account, then its savings at time t amount to:

$$\sum_{a=0}^{n-1} s(1 + \rho_C)^{n-1-a} = s \frac{(1 + \rho_C)^n - 1}{\rho_C}.$$

Instead, paying out s each period generates a value at time t of

$$\sum_{a=0}^{n-1} s(1 + r)^{(n-1-a)} = s \frac{(1 + r)^n - 1}{r}.$$

The firm saves enough to finance investment if

$$s = K \frac{\rho_C}{(1 + \rho_C)^n - 1}$$

We need that the firm generates enough profits to save this amount. That is, we need

$$\pi(1 - \rho_D \phi) > K \frac{\rho_C}{(1 + \rho_C)^n - 1}, \tag{A.4}$$

which holds under restriction (A.3). The firm prefers saving over paying dividends if

$$\underbrace{s \frac{(1 + r)^n - 1}{r}}_{\text{Pay dividends}} = K \frac{\rho_C}{(1 + \rho_C)^n - 1} \frac{(1 + r)^n - 1}{r} < \underbrace{\frac{\pi - \rho_D \phi \pi}{r} - K \left(1 + \frac{1}{r} \frac{\rho_C}{(1 + \rho_C)^n - 1} \right)}_{\text{Internally financed firm with debt obligations } \phi \pi}.$$

The firm that would save for investment is worth at least as much as the internally financed firm that makes coupon payments on its debt forever.²² This condition can be written as

$$\phi < \frac{1}{\rho_D} \left(1 - \frac{K}{\pi} \frac{\rho_C(1+r)^n + r(1+\rho_C)^n - r}{(1+\rho_C)^n - 1} \right),$$

which holds under restriction (A.3).

A direct implication of the fact that the firm never defaults is that it always replaces capital at the end of its useful life. The firm also never replaces capital early. If it would do so, then it could increase its firm value by delaying replacement and yield a return of $\rho_C K > 0$ on the cost of capital, which could be paid out as a dividend while leaving all other policies and cash flows unchanged. \square

Proof of Theorem 1. We want to show that the firm's net debt is weakly decreasing in capital age. To establish this result, we first need to show that the firm only pays dividends when the borrowing constraint binds in the previous period.

We know from Proposition 1 that the firm always replaces capital when it reaches the end of its useful life and that the debt is risk-free. Assume that for some t , $Div_{t+1} > 0$ while $ND_t < \phi\pi$. Define ΔDiv_t as

$$\Delta Div_t = \min \left\{ \frac{Div_{t+1}}{1 + \rho_D}, \phi\pi - ND_t \right\}.$$

Increasing dividends at time t to $Div'_t = Div_t + \Delta Div_t$ by using debt financing would imply that $Div'_{t+1} \geq Div_{t+1} - (1 + \rho_D)\Delta Div_t$. The inequality follows from the fact that the interest rate is lower if net debt was negative before $ND_t < 0$.²³ This change in policy would increase shareholder value since its effect on equity value (at time t) is at least

$$\Delta Div_t - \frac{(1 + \rho_D)\Delta Div_t}{1 + r} > 0.$$

As a result, if $ND_t < \phi\pi$, then $Div_{t+1} = 0$ and therefore if $Div_{t+1} > 0$ then $ND_t = \phi\pi$.

²²Observe that the value of the internally financed firm is actually a lower bound since some of the savings can be used to temporarily lower net debt, which yields a rate of return $\rho_D > \rho_C$.

²³Indeed, if $ND_t < 0$ and $ND_t + \Delta Div_t \leq 0$ then the discount rate is ρ_C and the change in the amount that needs to be repaid at $t + 1$ is

$$(1 + \rho_C)(ND_t + \Delta Div_t) - (1 + \rho_C)ND_t = (1 + \rho_C)\Delta Div_t < (1 + \rho_D)\Delta Div_t.$$

If $ND_t < 0$ and $ND_t + \Delta Div_t > 0$, this change is

$$(1 + \rho_D)(ND_t + \Delta Div_t) - (1 + \rho_C)ND_t = (1 + \rho_D)\Delta Div_t + ND_t(\rho_D - \rho_C) < (1 + \rho_D)\Delta Div_t.$$

Instead, if $ND_t > 0$ this change is $(1 + \rho_D)\Delta Div_t$.

Assume $a > 0$ and $ND_{a-1} < ND_a \leq \phi\pi$. If $ND_{a-1} > 0$ then

$$Div_a = \pi + ND_a - ND_{a-1}(1 + \rho_D) > \rho_D\phi\pi - \rho_D ND_{a-1} + (ND_a - ND_{a-1}) > 0$$

because $\phi < \frac{1}{\rho_D}$, see equation (A.3). While if $ND_{a-1} < 0$

$$Div_a = \pi + ND_a - ND_{a-1}(1 + \rho_C) > 0.$$

But this contradicts the previous result and therefore $ND_{a-1} \geq ND_a$. □

Lemma 2. *If $Div_{t+1} > 0$ then $ND_t = \phi\pi$.*

Proof. This result follows directly from the proof of Theorem 1. □

Lemma 3. $ND_{a=0} = \phi\pi$.

Proof. We want to show that $ND_{a=0} = \phi\pi$. We do so by showing that $ND_{a=0} < \phi\pi$ can never occur. Assume that for some $t' \geq 0$ with $a = 0$ we have $ND_{t'} < \phi\pi$. Let $t'' > t'$ be the next time that $ND_{t''} = \phi\pi$ and $a = 0$. Assume that t'' does not exist. In this case, and owing to Theorem 1 and Lemma 2, the firm never pays dividends for $t > t'$ since $ND_t < \phi\pi$. Therefore, equity value is zero. But this cannot be the optimal strategy since investment is positive NPV (Proposition 1) and therefore generates a surplus that can be distributed to shareholders, which would yield a positive equity value. As a result, t'' must exist. We know that $ND_{t''-n} < \phi\pi$ since $t' \leq t'' - n < t''$. Given that Theorem 1 implies that net debt is weakly decreasing within a cycle and $ND_{t''-n} < \phi\pi$, we have that $ND_t < \phi\pi$ for $t \in [t'' - n, t'' - 1]$ because of the definition of t' and t'' . From Lemma 2, it then follows that the firm does not pay any dividends over the interval $t \in [t'' - n + 1, t'']$ where $t'' - n + 1 > 0$.

Each period t , the firm has a cash flow of π but needs to pay interest. The firm can save at least $s = K \frac{\rho_C}{(1+\rho_C)^{n-1}}$ since equation (A.4) holds. Therefore, the firm lowers net debt by at least s each period over this time interval and as a result net debt decreases by at least

$$\sum_{a=0}^{n-1} s(1 + \rho_C)^a = s \frac{(1 + \rho_C)^n - 1}{\rho_C} = K.$$

As a result, we have that

$$\pi - \left(1 + \rho_D \mathbb{I}_{\{ND_{t''-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{t''-1} < 0\}}\right) ND_{t''-1} > \pi - \rho_D \phi\pi - ND_{t''-1} > K - ND_{t''-n+1}.$$

This implies that the dividend at time t'' , which follows from the budget constraint, is

$$\begin{aligned} Div_{t''} &= \pi - K + ND_{t''} - \left(1 + \rho_D \mathbb{I}_{\{ND_{t''-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{t''-1} < 0\}}\right) ND_{t''-1} \\ &> K - K + ND_{t''} - ND_{t''-n+1} = \phi\pi - ND_{t''-n+1} \\ &> 0. \end{aligned}$$

This makes it impossible that $ND_{t''-1} < \phi\pi$ owing to Lemma 2. This result in combination with Theorem 1 then implies that $ND_{t''-n} = \phi\pi$ but this contradicts the fact that $ND_t < \phi\pi$ for $t \in [t''-n, t-1'']$. This rules out that $ND_{a=0} < \phi\pi$ so that we must have $ND_{a=0} = \phi\pi$. \square

Proof of Proposition 2. We show using backward induction that higher investment costs $K' > K$ lead to stronger leverage cycles.

Assume $K \leq \pi - \rho_D \phi\pi$. In that case, the firm always keep its net debt at $\phi\pi$ and invests using retained earnings. As a consequence,

$$|ND_a - ND_{a-1}| = 0 \leq |ND'_a - ND'_{a-1}|.$$

Assume next that $K > \pi - \rho_D \phi\pi$ so that $K' > \pi - \rho_D \phi\pi$. In that case, the firm needs debt capacity $ND_{a=n-1} < \phi\pi$ to finance investment and we know from Lemma 2 that $Div_{a=0} = 0$. Furthermore, Lemma 3 implies that $ND_{a=0} = \phi\pi$. From the budget constraint it then follows that

$$0 = \pi - K + \phi\pi - \left(1 + \rho_D \mathbb{I}_{\{ND_{a=n-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a=n-1} < 0\}}\right) ND_{a=n-1}.$$

There is a unique $ND_{a=n-1}$ that solves this equation. Furthermore, this $ND_{a=n-1}$ is decreasing in K . These results also hold true for $ND'_{a=n-1}$ and imply that

$$0 \leq ND_{a=0} - ND_{a=n-1} = \phi\pi - ND_{a=n-1} < \phi\pi - ND'_{a=n-1} = ND'_{a=0} - ND'_{a=n-1}$$

and therefore

$$|ND_{a=0} - ND_{a=n-1}| \leq |ND'_{a=0} - ND'_{a=n-1}|.$$

We are going to show the result for $a > 0$ using backwards induction. We have just shown that $ND_{a=n-1} \geq ND'_{a=n-1}$. Assume now that $ND_a \geq ND'_a$ and $a > 0$. We want to show that $ND_{a-1} \geq ND'_{a-1}$ and the proposition's result. There are three cases.

1. Assume $ND_{a-1} < \phi\pi$ and $ND'_{a-1} < \phi\pi$ then we have that $Div_a = Div'_a = 0$, see

Lemma 2. Assume $ND_{a-1} < ND'_{a-1}$ then the budget constraint implies that

$$\begin{aligned}
0 &= \pi + ND_a - \left(1 + \rho_D \mathbb{I}_{\{ND_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a-1} < 0\}}\right) ND_{a-1} \\
&= \pi + ND'_a - \left(1 + \rho_D \mathbb{I}_{\{ND'_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND'_{a-1} < 0\}}\right) ND'_{a-1}, \\
ND_a - ND'_a &= \left(1 + \rho_D \mathbb{I}_{\{ND_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a-1} < 0\}}\right) ND_{a-1} \\
&\quad - \left(1 + \rho_D \mathbb{I}_{\{ND'_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND'_{a-1} < 0\}}\right) ND'_{a-1} \\
&< 0,
\end{aligned}$$

This contradicts the fact that $ND_a \geq ND'_a$. Thus, we must have $ND_{a-1} \geq ND'_{a-1}$. We still need to show the proposition's result. We know that the budget constraint

$$0 = \pi + ND_a - \left(1 + \rho_D \mathbb{I}_{\{ND_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a-1} < 0\}}\right) ND_{a-1}$$

holds. From this budget constraint it directly follows that

$$\begin{aligned}
0 \leq ND_{a-1} - ND_a &= \pi - \left(\rho_D \mathbb{I}_{\{ND_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a-1} < 0\}}\right) ND_{a-1} \\
&\leq \pi - \left(\rho_D \mathbb{I}_{\{ND'_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND'_{a-1} < 0\}}\right) ND'_{a-1} \\
&= ND'_{a-1} - ND'_a.
\end{aligned}$$

The inequality follows from the fact that $ND_{a-1} \geq ND'_{a-1}$. Therefore

$$|ND_{a-1} - ND_a| \leq |ND'_{a-1} - ND'_a|.$$

2. Assume $ND_{a-1} < \phi\pi$ and $ND'_{a-1} = \phi\pi$ then we have that $Div_a = 0$ from Lemma 2. The budget constraint then implies that

$$\begin{aligned}
0 &= -Div_a + \pi + ND_a - \left(1 + \rho_D \mathbb{I}_{\{ND_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a-1} < 0\}}\right) ND_{a-1} \\
&= -Div'_a + \pi + ND'_a - (1 + \rho_D)ND'_{a-1} \\
&\leq \pi + ND'_a - (1 + \rho_D)ND'_{a-1}.
\end{aligned}$$

As a consequence,

$$Div_a \geq (ND_a - ND'_a) - \left(1 + \rho_D \mathbb{I}_{\{ND_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND_{a-1} < 0\}}\right) ND_{a-1} + (1 + \rho_D)ND'_{a-1} > 0,$$

which is a contradiction. Therefore, this case cannot arise.

3. Assume $ND_{a-1} = \phi\pi$ and $ND'_{a-1} \leq \phi\pi$. This case directly implies that $ND_{a-1} \geq$

ND'_{a-1} . If $ND'_{a-1} = \phi\pi$ then

$$0 \leq ND_{a-1} - ND_a = \phi\pi - ND_a \leq \phi\pi - ND'_a = ND'_{a-1} - ND'_a.$$

If $ND'_{a-1} < \phi\pi$ then $Div'_a = 0$ by Lemma 2. From the budget constraint it then follows that

$$\begin{aligned} 0 \leq ND_{a-1} - ND_a &= -Div_a + \pi - \rho_D ND_{a-1} \\ &\leq \pi - \left(\rho_D \mathbb{I}_{\{ND'_{a-1} \geq 0\}} + \rho_C \mathbb{I}_{\{ND'_{a-1} < 0\}} \right) ND'_{a-1} = ND'_{a-1} - ND'_a. \end{aligned}$$

Therefore,

$$|ND_{a-1} - ND_a| \leq |ND'_{a-1} - ND'_a|.$$

These steps recursively establish our result. □

B Debt Maturity

We first establish the optimal debt issuance strategy (Theorem 2). We then show that average debt maturity is decreasing in capital age (Proposition 3) and increasing in asset maturity (Theorem 3).

Proof of Theorem 2. We first show that the net debt dynamics are the same when $\epsilon \rightarrow 0$ as when debt issuance is frictionless. These net debt dynamics allow us to show the absence of permanent debt and derive the optimal debt issuance strategy.

Let $E_0(\epsilon)$ be the equity value given issuance costs ϵ . Without issuance costs, debt maturity is irrelevant as any long-term debt contract can be implemented by a sequence of short-term contracts. Furthermore, $E_0(0) \geq E_0(\epsilon)$ since issuance cost depress firm value. As a result, the net debt and investment dynamics are the same as in the baseline model when $\epsilon \rightarrow 0$. If this was not the case, then we would have $\lim_{\epsilon \downarrow 0} E_0(\epsilon) < E_0(0)$ and using the one-period debt implementation from the baseline model would dominate for sufficiently small issuance costs $\epsilon \rightarrow 0$.

Given these net debt dynamics, the firm wants to issue debt that minimizes issuance costs. Observe that cash generates a lower return than debt $\rho_C < \rho_D$ and given that debt issuance costs are small $\epsilon \rightarrow 0$, the firm only has debt outstanding when $ND_t > 0$ and only cash in hand when $ND_t < 0$.

Because the firm always invests when assets reach the end of their useful life (Proposition 1), we have that $ND_{a=n-1} < 0$ since it needs both cash and debt to finance investment; see equation (2). As a result, the firm does not issue debt with a maturity longer than n -periods.

To minimize issuance costs the firm only issues debt when it invests with a maturity that matches the net debt dynamics during the capital's lifetime. \square

Proof of Proposition 3. We first establish that average debt maturity has a recursive structure that depends on the ratio of this and next period's net debt. We then establish that the ratio of this and next period's net debt can be ordered, which allows us to show that average debt maturity declines as capital ages.

Define \hat{a} as the largest capital age such that debt is positive

$$\hat{a} = \sup\{a | ND_a > 0\}.$$

Given that $K > \phi\pi + \pi$ (see equation (2)), we know that $ND_{n-1} < 0$ and therefore that $\hat{a} < n - 1$. Furthermore, from Theorem 1 we have that $ND_a \leq 0$ for $a > \hat{a}$. Therefore average debt maturity is $M_a = 0$ for $a > \hat{a}$.

We can write the average debt maturity as

$$\begin{aligned} M_a &= \sum_{i=a}^{n-1} \mathbb{I}_{\{ND_i > 0\}} (i+1-a) \frac{ND_i - \max\{ND_{i+1}, 0\}}{ND_a} \\ &= \sum_{i=a}^{\hat{a}} (i+1-a) \frac{ND_i - \max\{ND_{i+1}, 0\}}{ND_a} \\ &= \frac{1 * ND_a - 1 * ND_{a+1} + 2 * ND_{a+1} - \dots - (\hat{a} - a) ND_{\hat{a}} + (\hat{a} + 1 - a) ND_{\hat{a}}}{ND_a} \\ &= \frac{ND_a + \dots + ND_{\hat{a}}}{ND_a} = 1 + \frac{ND_{a+1} + \dots + ND_{\hat{a}}}{ND_a} \\ &= 1 + \frac{ND_{a+1}}{ND_a} M_{a+1}. \end{aligned}$$

Define $B_a = \frac{ND_{a+1}}{ND_a}$ for $a < \hat{a}$. The above equation can be rewritten as

$$M_a = 1 + B_a M_{a+1}.$$

From Theorem 1 and the definition of \hat{a} it follows that $B_a \in (0, 1]$.

We want to show that $B_{a+1} \leq B_a$ for $a < \hat{a} - 1$. Assume first that $ND_{a+1} = \phi\pi$. In this case, we have $B_{a+1} \leq 1 = \phi\pi/\phi\pi = ND_{a+1}/ND_a = B_a$ (Theorem 1). Assume next that $ND_{a+1} < \phi\pi$. Then we also have $ND_{a+2} \leq ND_{a+1} < \phi\pi$ (Theorem 1). From the budget constraint in equation (1), the fact that $ND_{a+2} \geq ND_{\hat{a}} > 0$ (Theorem 1), and the fact that the firm pays no dividends at $a+2$ since $ND_{a+1} < \phi\pi$ (Lemma 2), it then follows that

$$ND_{a+2} = ND_{a+1}(1 + \rho_D) - \pi$$

and therefore

$$B_{a+1} = (1 + \rho_D) - \frac{\pi}{ND_{a+1}}.$$

If $ND_a < \phi\pi$ then the same argument implies that

$$B_a = (1 + \rho_D) - \frac{\pi}{ND_a}.$$

Since ND_a is weakly decreasing in a (Theorem 1), we then have that $B_{a+1} \leq B_a$.

If $ND_a = \phi\pi$ the same argument implies that

$$ND_{a+1} = Div_{a+1} + ND_a(1 + \rho_D) - \pi \geq ND_a(1 + \rho_D) - \pi$$

and therefore

$$B_a \geq (1 + \rho_D) - \frac{\pi}{ND_a}.$$

and we get that $B_{a+1} \leq B_a$

As a consequence

$$1 \geq B_0 \geq B_1 \geq \dots \geq B_{\hat{a}-1} > 0.$$

It is easy to see that $M_{\hat{a}} = 1$ and therefore

$$M_{\hat{a}-1} = 1 + B_{\hat{a}-1}M_{\hat{a}} \geq 1 = M_{\hat{a}}.$$

We can now establish our result using backward induction. Assume that $M_{\hat{a}-i-1} \geq M_{\hat{a}-i} \geq 0$. We then know that

$$M_{\hat{a}-i-2} = 1 + B_{\hat{a}-i-2}M_{\hat{a}-i-1} \geq 1 + B_{\hat{a}-i-1}M_{\hat{a}-i-1} \geq 1 + B_{\hat{a}-i-1}M_{\hat{a}-i} = M_{\hat{a}-i-1} \geq 0,$$

which recursively establishes that the debt maturity is decreasing in a . \square

Proof of Theorem 3. We first show that increasing asset life by a year yields the same net debt dynamics just one year lagged. This result in combination with Proposition 3 allows us to show that average debt maturity weakly increases with asset life.

Define the function

$$d(ND_{a-1}, ND_a) = \pi - K\mathbb{I}_{\{a=0\}} + ND_a - (1 + \mathbb{I}_{\{ND_{a-1} \geq 0\}}\rho_D + \mathbb{I}_{\{ND_{a-1} < 0\}}\rho_C) ND_{a-1},$$

which is the “*dividend*” the firm would pay when capital has age a and debt levels are ND_{a-1}

and ND_a , see equation (1). Observe that

$$\frac{\partial d(ND_{a-1}, ND_a)}{\partial ND_{a-1}} < 0. \quad (\text{A.5})$$

Given ND_a , if the firm pays no dividends then the net debt from the previous period ND_{a-1} solves

$$d(ND_{a-1}, ND_a) = 0,$$

which has a unique solution that we call $\hat{N}D(ND_a)$. Given ND_a , if the firm pays dividends $Div_a > 0$, then the net debt from the previous period ND_{a-1} solves

$$d(ND_{a-1}, ND_a) = Div_a,$$

which has a unique solution that we call $\tilde{N}D(ND_a, Div_a)$. Equation (A.5) implies that

$$\tilde{N}D(ND_a, Div_a) < \hat{N}D(ND_a). \quad (\text{A.6})$$

Let $ND_a(n)$ be the net debt of a firm with asset maturity n and capital age a with other quantities made dependent on n in a similar way. We first want to establish that $ND_a(n) = ND_{a+1}(n+1)$ for $a \geq 0$. We do so using backward induction. Lemma 3 implies that $ND_0(n) = ND_0(n+1) = \phi\pi$. We additionally know that $ND_{a=n-1}(n) < 0 < \phi\pi$ and similarly that $ND_{a=n}(n+1) < 0 < \phi\pi$ as otherwise the firm cannot finance investment; see equation (2). This together with Lemma 2 implies that $Div_0(n) = Div_0(n+1) = 0$. Therefore,

$$ND_{a=n-1}(n) = ND_{a=n}(n+1) = \hat{N}D(\phi\pi).$$

We can now establish recursively that $ND_a(n) = ND_{a+1}(n+1)$. Indeed assume that $ND_a(n) = ND_{a+1}(n+1)$. There are two cases to consider.

Case 1: If $\phi\pi \geq \hat{N}D(ND_a(n))$ then $\phi\pi \geq \hat{N}D(ND_a(n)) > \tilde{N}D(ND_a(n), Div_a)$ for any $Div_a > 0$, see equation (A.6), and it cannot be the case that the firm pays dividends at time a because in that case the debt level at $a-1$ would have been $\phi\pi > \tilde{N}D(ND_a(n), Div_a)$, which violates Lemma 2. As a result, when $\phi\pi \geq \hat{N}D(ND_a(n))$ then $ND_{a-1}(n) = \hat{N}D(ND_a(n))$ and via the same reasoning $ND_a(n+1) = \hat{N}D(ND_{a+1}(n+1)) = \hat{N}D(ND_a(n))$. Therefore,

$$ND_{a-1}(n) = ND_a(n+1) = \hat{N}D(ND_a(n)).$$

Case 2: If $\phi\pi < \hat{N}D(ND_a(n))$ then it must be that the firm pays dividends since otherwise the debt level in the previous period would violate the borrowing constraint. Given

that the firm pays dividends and Lemma 2, we must have that

$$ND_{a-1}(n) = ND_a(n+1) = \phi\pi.$$

This recursively establishes that $ND_a(n) = ND_{a+1}(n+1)$ for $a \geq 0$. Furthermore, we have $ND_0(n+1) = \phi\pi = ND_0(n) = ND_1(n+1)$; see Lemma 3.

A firm with assets that have a useful life of $n+1$ periods that issues debt with a maturity that is one year longer than a firm with assets that have a useful life of n , has net debt dynamics $ND_{a+1}(n+1) = ND_a(n)$ for $a \geq 0$ with $ND_0(n+1) = ND_1(n+1) = \phi\pi$, which we just showed is the optimal net debt level when the useful life of assets is $n+1$. This in turn implies that $M_{a+1}(n+1) = M_a(n)$ and, in combination Proposition 3, leads to the desired result. \square

C Data Definitions and Summary Statistics

I Capital IQ Maturity Data

We supplement the firm-level debt maturity proxy derived from Compustat with a more detailed measure from Capital IQ security issuance data, which covers the period of 2002 to 2018. To merge the security- and firm-level data, we use the most recent filing dates and remove any observations with the same ID/date, description, maturity, and interest rate. We further remove all securities with missing `gvkey` and drop entries for credit lines that reflect the drawdown limit only, as opposed to actual utilisation. We drop all observations with missing or negative maturity values. We then compute the firm-level maturity as the weighted average of individual-security maturities weighted by their notional amounts. As the final data filter, we drop observations for which the total debt in Capital IQ is greater than Compustat by more than 10%, as in Colla, Ippolito, and Li (2013).

II Definitions of Variables

The variables used in the paper are defined in Table A.1.

Variable	Definition
Capital age	See Subsection III.A
Useful life	See Subsection III.A
Net debt to EBITDA	Ratio of total debt (<code>dltt+dlc</code>) less cash (<code>che</code>) over EBITDA (<code>ebitda</code>); set to missing when EBITDA is negative
Net market leverage	Ratio of total debt (<code>dltt+dlc</code>) less cash (<code>che</code>) over total debt plus market value of equity (<code>prcc_f*csho</code>)

Table A.1: **Definitions of variables.** The table contains the definitions of all variables used throughout the paper (in order of appearance).

Variable	Definition
Net book leverage	Ratio of total debt (<code>dltt+dlc</code>) less cash (<code>che</code>) over total assets (<code>at</code>)
% debt maturing > 3y	Ratio of long-term debt (<code>dltt</code>) minus debt maturing in 2- and 3-years (<code>dd2+dd3</code>) over total debt (<code>dlc+dltt</code>)
% debt maturing > 5y	Ratio of long-term debt (<code>dltt</code>) minus debt maturing in 2-, 3-, 4-, and 5-years (<code>dd2+dd3+dd4+dd5</code>) over total debt (<code>dlc+dltt</code>)
Debt maturity (yr.)	Average maturity of outstanding instruments from Capital IQ, weighted by notional
Investment	Capital expenditures (<code>capx</code>) over lagged installed capital (<code>1.ppegt</code>)
Profitability	Operating income (<code>oibdp</code>) over total assets (<code>at</code>)
Size	Natural log of real sales (<code>log(sale/defl)</code>), where <code>defl</code> is the CPI deflator
Tangibility	Ratio of property, plant and equipment (<code>ppent</code>) to total assets (<code>at</code>)
Market-to-book	Ratio of the sum of market value of equity (<code>prcc_f*csho</code>) and book value of debt (<code>at-ceq</code>) to total assets (<code>at</code>)
Cash flow volatility	Moving 3-year standard deviation of profitability
R&D	Ratio of R&D expenditure (<code>xrd</code>) to sales (<code>sale</code>), missing values replaced with zero
Firm age	Time since listing (defined as the first appearance of each firm in CRSP) in years
Asset maturity	Gross property, plant and equipment over depreciation and amortization (<code>ppegt/dp</code>) times the proportion of property, plant and equipment in total assets (<code>ppegt/at</code>), plus current assets over the cost of goods sold (<code>act/cogs</code>) times the proportion of current assets in total assets (<code>act/at</code>)
Abnormal earnings	The difference between the income before extraordinary items, adjusted for common stock equivalents (<code>ibadj-1.ibadj</code>) over the market value of equity used in calculating earnings per share (<code>prcc_f*cshpri</code>)
Investment (firm-level) skewness	The firm-level skewness of investment, measured as the ratio of capital expenditures (<code>capx</code>) over lagged installed capital (<code>1.ppegt</code>); we require at least 5 observations per firm

Table A.1: **Definitions of variables.** The table contains the definitions of all variables used throughout the paper (in order of appearance).

Variable	Definition
Investment kurtosis (firm-level)	The firm-level kurtosis of investment, measured as the ratio of capital expenditures (<code>capx</code>) over lagged installed capital (<code>1.ppegt</code>); we require at least 5 observations per firm
Return on investment	EBITDA (<code>ebitda</code>) over total assets (<code>at</code>)
Debt cycle length	Number of years to the first leverage spike, between subsequent leverage spikes, or after the last spike, conditional on the 3-year window filter and their being at least one spike
Alternative capital age (1)	Capital age calculated as in Subsection III.A, except that, when the firm disinvests, the oldest vintages are disposed of first, rather than all vintages equally
Alternative capital age (2)	Accumulated (<code>dpact</code>) to current (<code>dpc</code>) depreciation expense
Alternative capital age (3)	The weighted average of capital vintages, when averaging over the past T and where more weight is put on younger vintages, following Ai et al. (2012) with $T = 7$
Alternative depreciation rate	Depreciation expense (<code>dpc</code>) over net plant, property and equipment (<code>ppent</code>), winsorized at 1% and 99% levels before calculating capital age
Alternative capital age (4)	Capital age calculated as in Subsection III.A using the depreciation rate from Compustat
Alternative depreciation rate excluding amortization	Depreciation expense (<code>dpc</code>) minus amortization of intangibles (<code>am</code>) over net plant, property and equipment (<code>ppent</code>), missing amortization values replaced with zero, winsorized at 1% and 99% levels before calculating capital age
Alternative capital age (5)	Capital age calculated as in Subsection III.A using the depreciation rate excluding amortization from Compustat

Table A.1: **Definitions of variables.** The table contains the definitions of all variables used throughout the paper (in order of appearance).

III Summary Statistics

Table A.2 contains the summary statistics of all the variables used in the paper which were not provided in Table 1.

	Mean	Std. dev.	Q1	Median	Q3	<i>N</i>
Depreciation rate (BEA)	0.085	0.029	0.068	0.081	0.098	69054
Profitability	0.142	0.073	0.092	0.134	0.183	69054
Size	5.476	1.981	4.097	5.469	6.835	69054
Market-to-book	1.454	0.765	0.982	1.224	1.651	69054
Tangibility	0.361	0.230	0.179	0.316	0.518	69011
Cash flow volatility	0.037	0.033	0.016	0.028	0.047	54770
R&D	0.007	0.017	0.000	0.000	0.007	69054
Firm age	19.213	17.244	6.751	14.085	25.751	66991
Asset maturity	10.806	9.104	4.361	8.380	14.567	67393
Abnormal earnings	0.002	0.178	-0.021	0.009	0.034	63991
Investment skewness (firm-level)	0.930	0.843	0.347	0.857	1.433	4389
Investment kurtosis (firm-level)	3.563	2.540	2.025	2.748	4.119	4389
Return on investment	0.142	0.073	0.092	0.134	0.183	69054
Alternative capital age (1)	5.759	2.929	3.572	5.347	7.513	66438
Alternative capital age (2)	5.777	3.462	3.350	5.169	7.447	68335
Alternative capital age (3)	3.349	0.758	2.907	3.361	3.796	53014
Alternative depreciation rate	0.195	0.257	0.099	0.138	0.201	73817
Alternative capital age (4)	5.511	2.773	3.497	5.118	7.028	73817
Alt. dep. rate excl. amortization	0.170	0.175	0.096	0.132	0.185	73817
Alternative capital age (5)	5.638	2.743	3.631	5.251	7.155	73817

Table A.2: **Summary statistics.** The table contains the summary statistics of the variables used in the regression models of net leverage and debt maturity. The sample period is from 1975 to 2018. All variables are winsorized at 1% and 99% levels and defined in Table A.1.

Internet Appendix to: Financing Cycles

Thomas Geelen[†] Jakub Hajda[‡] Erwan Morellec[§] Adam Winegar[¶]

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This appendix contains:

1. Additional results related to capital depreciation, investment and debt dynamics, and cash-flow versus asset-based borrowing constraints.
2. Additional robustness tests that support the model predictions.

Other Forms of Capital Depreciation

Our model assumes that the efficiency of capital goods follows a one-hoss shay pattern, as in e.g. [Arrow \(1964\)](#), [Rogerson \(2008\)](#), [Rampini \(2019\)](#), or [Livdan and Nezlobin \(2021\)](#). This form of capital efficiency keeps the model tractable since capital age a is a sufficient statistic for the state of the firm when $t > 0$. This in turn allows us to generate crisp empirical predictions on financing decisions and debt maturity choices.

An important question is whether this form of capital efficiency is necessary for our results. *The short answer is no.* Debt cycles are generated by large replacement investments financed with debt. Thus, any form of depreciation that leads to large replacement investments suffices (see [Proposition 4](#)). But what forms of depreciation have this feature?

The U.S. Bureau for Labor Statistics (BLS) estimates the productivity of capital in place relative to the productivity of new capital (or, equivalently, the productivity of capital a years after it has been installed) using the function

$$S(a|\beta) = \mathbb{I}_{\{a \leq n-1\}} \frac{n-a}{n-\beta a},$$

where $\beta \in [0, 1]$; see [Giandrea et al. \(2021\)](#). Our model with capital that has a finite useful life represents the case in which $\beta = 1$. The case $\beta = 0$ corresponds to a linear decrease in asset productivity. [Figure IA.1a](#) shows intermediate cases $\beta \in (0, 1)$. A linear decrease in productivity implies that the replacement investment needed to compensate for the lost productivity of the original capital is constant, in that $S(a-1|0) - S(a|0) = \frac{1}{n} \mathbb{I}_{\{a \leq n\}}$. By

[†]Copenhagen Business School and Danish Finance Institute, Denmark

[‡]HEC Montréal, Canada

[§]EPF Lausanne, Swiss Finance Institute, and CEPR, Switzerland

[¶]BI Norwegian Business School, Norway

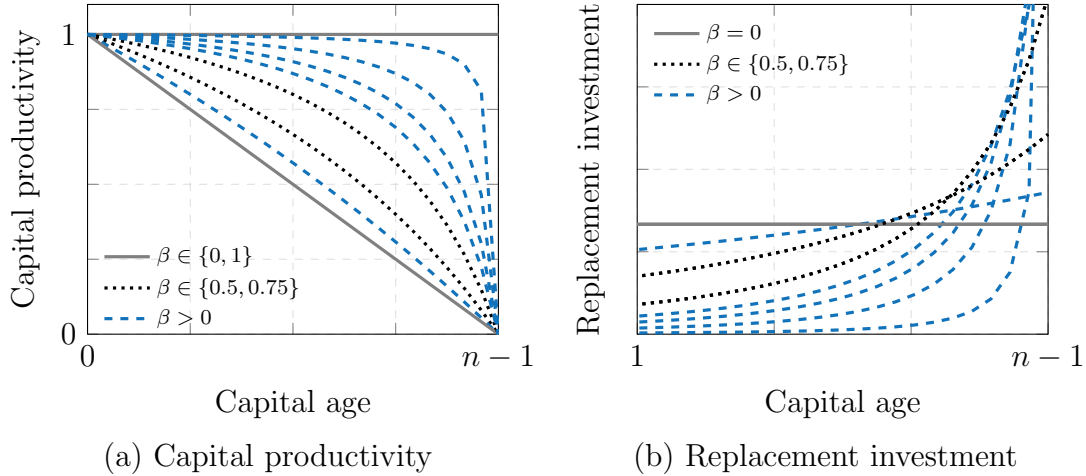


Figure IA.1: **Depreciation and replacement investments.** The figure shows the productivity of capital $S(a|\beta)$ as it ages and the replacement investment $S(a-1|\beta) - S(a|\beta)$ necessary due to the depreciation of the original capital.

contrast, any form of depreciation with $\beta > 0$ back loads the replacement investment leading to large planned replacement investments in capital, as shown by Figure IA.1b. The U.S. Bureau for Labor Statistics uses $\beta = 0.75$ for structures and $\beta = 0.5$ for equipment (see Giandrea et al., 2021). With $\beta = 0.75$ and $n = 4$ (respectively $n = 5$), the firm makes 57.1% (respectively 50%) of its replacement investments in the last useful year of the asset.

We now allow for arbitrary depreciation schedules of capital assuming that capital fully depreciates in n periods, where n can be arbitrarily large. Let π_t be the firm profits at time t . To keep the analysis tractable, we make the following two assumptions:

1. The borrowing constraint is time-invariant

$$D_t \leq \Phi.$$

2. Given the optimal policies, the firm generates enough profits to make interest payments

$$\pi_t > \rho_D \Phi \geq \rho_D D_t.$$

Under these restrictions, we can establish that given an arbitrary form of capital depreciation and an arbitrary distribution of the firm's capital age:

Proposition 4 (Ageing Capital and Leverage with Arbitrary Capital Depreciation). *Let time $T > t$ be the next time that the firm invests. Then for $t' \in \{t, \dots, T-2\}$, capital ages*

while net debt weakly declines

$$ND_{t'+1} \leq ND_{t'}.$$

Proof of Proposition 4. We first establish that the firm never defaults and that the borrowing constraint must bind at time t for the firm to pay dividends at time $t + 1$ (the equivalent of Lemma 2). We then show that once net debt starts decreasing it does so (at least) until the firm invests. As a consequence, during this period, capital ages while net debt declines.

The second condition ensures that the firm never defaults since it can always make interest payments and therefore the rate of return on debt is ρ_D .

We want to show that the firm's net debt is weakly decreasing in capital age at least until the firm invests. To obtain this result, we first need to show that the firm only pays dividends when the borrowing constraint binds in the previous period. We show below that it is suboptimal for the firm to pay dividends at time $t + 1$ if the borrowing constraint does not bind at time t . Therefore, the borrowing constraint must bind at time t if the firm pays dividends at time $t + 1$.

We first establish that if the firm has net debt $ND_t < \Phi$ then $Div_{t+1} = 0$. For this purpose, assume that we have $Div_{t+1} > 0$ while $ND_t < \Phi$ for some t . Define ΔDiv_t as

$$\Delta Div_t = \min \left\{ \frac{Div_{t+1}}{1 + \rho_D}, \Phi - ND_t \right\}.$$

Increasing dividends at time t to $Div'_t = Div_t + \Delta Div_t$ using debt financing implies that $Div'_{t+1} \geq Div_{t+1} - (1 + \rho_D)\Delta Div_t$, where the inequality follows from the fact that the interest rate is lower if net debt is negative (i.e. if $ND_t < 0$); see footnote 23. This change in policy would increase shareholder value since its effect on equity value (at time t) is at least

$$\Delta Div_t - \frac{(1 + \rho_D)\Delta Div_t}{1 + r} > 0,$$

which contradicts optimality of the firm's policies. Therefore, if $Div_{t+1} > 0$ then $ND_t = \Phi$.

Next, we show that net debt weakly decreases over time at least until the firm invests. Let $t' \in \{t, T - 2\}$ where T is the next time the firm invests. There are two cases. First, if $ND_{t'} = \Phi$ then $ND_{t'} \geq ND_{t'+1}$ because of the borrowing constraint. Second, if $ND_{t'} < \Phi$ then the firm does not pay dividends at time $t' + 1$ since $ND_{t'} < \Phi$. Furthermore, $ND_{t'} > ND_{t'+1}$ since $\pi_{t'+1} > \rho_D \Phi > \rho_D ND_{t'}$. Finally, from t' to $t' + 1$ installed capital becomes a year older since there is no investment while net debt weakly decreases. \square

Investment and Debt Dynamics

In the baseline model, the firm can invest in one unit of capital and replaces it every n periods. Assume now that the firm has N units of capital of different vintages, each of which generates a profit π per period for n periods. Furthermore, assume the firm replaces capital when it reaches the end of its useful life. Therefore, the firm invests at times $n * i - a_k^0$, $\forall i \in \mathbb{N}$ and $\forall k \in \{1, \dots, N\}$, where a_0^k is the age of capital unit $k \in \{1, \dots, N\}$ at time zero. We can then show that:

Proposition 5 (Debt Cycles with Multiple Assets). *Let time $T > t$ be the next time that the firm invests. Then for $t' \in \{t, \dots, T - 2\}$, capital ages while net debt weakly declines*

$$ND_{t'+1} \leq ND_{t'}.$$

Proof of Proposition 5. The fact that the firm investment exists of replacing capital that has reach the end of its useful life implies that:

1. The borrowing constraint is time-invariant

$$D_t \leq N\phi\pi.$$

2. Given the optimal policies and the parameter restriction on ϕ , the firm generates enough profits to make interest payments

$$N\pi > \rho_D N\phi\pi \geq \rho_D D_t.$$

The proof is then the same as the proof of Proposition 4. □

Cash-Flow Versus Asset-Based Borrowing Constraints

While in the paper, we rely on a cash-flow based borrowing constraints ([Lian and Ma, 2021](#)). As we now show, debt cycles would mechanically be stronger with an asset-based borrowing constraint ([Rampini and Viswanathan, 2022](#)).

Let V_a be the residual value of capital, which we define as the present value of future cash flows that capital with age a generates:

$$V_a = \frac{\pi}{1+r} + \dots + \frac{\pi}{(1+r)^{n-a}} = \sum_{t=a+1}^n \frac{\pi}{(1+r)^{t-a}}.$$

We assume that the replacement value of capital $\tilde{V}_a = \frac{K}{V_0} V_a$ is proportional to the residual value of capital V_a such that for new capital the replacement value is equal to the purchase price of new capital $\tilde{V}_0 = K$.

Assuming the firm is producing and with a debt repayment due next period of $D_a(1+\rho_D)$, an asset-based borrowing constraint would restrict debt to be less than some fraction $\chi \in \left[0, \frac{1}{1+\rho_D}\right]$ of the capital's residual value

$$D_a < \chi \tilde{V}_a.$$

Since the replacement value of assets \tilde{V}_a decreases with capital age, such a constraint can only strengthen the debt cycles identified in Theorem 1. The reason is that firms are forced to deleverage because the borrowing constraint becomes tighter as capital ages, which does not happen with a cash-flow based borrowing constraint.

Robustness and Additional Results

1. Table [IA.1](#) documents the importance of capital age and all the other factors used in the financing and debt maturity regressions following the approach of [Frank and Goyal \(2009\)](#).
2. Table [IA.2](#) presents estimates from regressions of financing and debt maturity on lagged capital age for different definitions of industries.
3. Table [IA.3](#) presents estimates from regressions of firm-level maximum and average debt cycle lengths based on net book leverage spikes on measures of asset life.
4. Table [IA.4](#) presents estimates from regressions of firm-level maximum and average debt cycle lengths requiring five years between leverage spikes on measures of asset life.

Panel A: Net leverage (net book leverage)

Explanatory variable	Coef.	<i>t</i> -stat.	Adjusted within R^2	
			Individual	Cumulative
Capital age	-0.045***	-13.86	0.036298	0.036298
Profitability	-0.032***	-14.67	0.02662	0.061188
Market-to-book	-0.025***	-10.58	0.016062	0.065402
Size	0.074***	8.46	0.014949	0.073172
Tangibility	0.047***	7.52	0.014257	0.081525
Cash flow	-0.006***	-2.9	0.00092	0.08152
Firm age	0.039	1.03	0.000123	0.081582
R&D	0.002	0.40	-0.000007	0.081545

Panel B: Debt maturity (% of debt maturing in > 3 years)

Explanatory variable	Coef.	<i>t</i> -stat.	Adjusted within R^2	
			Individual	Cumulative
Net book leverage	0.045***	9.92	0.010092	0.010092
Capital age	-0.043***	-9.65	0.007537	0.014722
Size	0.092***	7.15	0.005273	0.016633
Size squared	0.067***	5.47	0.00313	0.017688
Asset maturity	-0.010*	-1.84	0.000278	0.017658
R&D	-0.009	-1.3	0.000099	0.017724
Cash flow volatility	-0.001	-0.34	-0.000032	0.017753
Abnormal earnings	-0.0004	-0.25	-0.000039	0.017896
Firm age	0.009	0.19	-0.00004	0.01792
Market-to-book	0.0002	0.05	-0.000042	0.01788

Table IA.1: **Capital age and financing – importance of individual determinants.** This table presents estimates from regressions of net book leverage (for comparability to Frank and Goyal (2009); Panel A) debt maturity (% of debt maturing in > 3 years; Panel B) on lagged controls from Table 2 in Panel A and from Table 3 in Panel B. We obtain the coefficient estimates, *t*-statistic and the individual adjusted within R^2 by regressing net book leverage or debt maturity on each explanatory variable. We then sort the variables by their individual adjusted within R^2 and regress net book leverage by consecutively adding explanatory variables, which allows to obtain the cumulative adjusted within R^2 . All regressions include firm and industry-year fixed effects, created using the Hoberg-Phillips fixed industry classification with 100 industries, and are run on the same sample as the regression model in column (3) in Table 3. All variables are defined in Table A.1. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate *p*-values.

Panel A: Net leverage

	ND/EBITDA		Net book leverage		Net market leverage	
	(1)	(2)	(3)	(4)	(5)	(6)
Capital age	-0.385*** (-6.90)	-0.408*** (-8.80)	-0.033*** (-9.32)	-0.035*** (-11.66)	-0.033*** (-8.55)	-0.034*** (-10.25)
Ind.-Yr. FE (HP50)	Yes	No	Yes	No	Yes	No
Ind.-Yr. FE (FF49)	No	Yes	No	Yes	No	Yes
Controls	Yes	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes
Observations	30227	44030	30227	44030	30227	44030
Adj. within R^2	0.0408	0.0424	0.0806	0.0866	0.1149	0.1136

Panel B: Debt maturity

	% debt maturing > 3y		% debt maturing > 5y		Debt maturity (yr.)	
	(1)	(2)	(3)	(4)	(5)	(6)
Capital age	-0.028*** (-6.14)	-0.031*** (-7.85)	-0.020*** (-4.21)	-0.024*** (-5.88)	-0.394** (-2.56)	-0.347** (-2.52)
Ind.-Yr. FE (HP50)	Yes	No	Yes	No	Yes	No
Ind.-Yr. FE (FF49)	No	Yes	No	Yes	No	Yes
Controls	Yes	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes
Observations	29317	42948	29317	42948	10480	11323
Adj. within R^2	0.0169	0.0165	0.0076	0.0093	0.0070	0.0058

Table IA.2: **Capital age and financing – alternative industry definitions.** This table presents estimates from regressions of net leverage (Panel A) and debt maturity (Panel B) on lagged capital age for different definitions of industries. The dependent variables in Panel A are *Net debt to EBITDA* in columns 1 and 2, *Net book leverage* in columns 3 and 4 and *Net market leverage* in columns 5 and 6. The dependent variables in Panel B are *% of debt maturing in > 3 years* in columns 1 and 2; *% of debt maturing in > 5 years* in columns 3 and 4; and *Debt maturity (yr.)* in columns 5 and 6. We control for all independent variables from Table 2 in the net leverage regressions and from Table 3 in the debt maturity regressions. Each explanatory variable is standardized by its full-sample standard deviation. All models include industry-year fixed effects created using the Hoberg-Phillips fixed industry classification with 50 industries (*HP50*) and the Fama-French 49 industries (*FF49*). All variables are defined in Table A.1. *t*-statistics are reported in parentheses. Standard errors are clustered at the firm level. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate *p*-values.

	Max debt cycle		Avg. debt cycle	
	(1)	(2)	(3)	(4)
Panel A: Useful life				
Useful life	0.220*** (6.03)	0.101*** (4.26)	0.145*** (5.63)	0.073*** (3.61)
Controls	No	Yes	No	Yes
Observations	2027	2007	2027	2007
Adj. R^2	0.032	0.246	0.021	0.167
Panel B: Average capital age				
Capital age	0.671*** (9.20)	0.138** (2.30)	0.467*** (9.49)	0.121** (2.61)
Controls	No	Yes	No	Yes
Observations	2030	2009	2030	2009
Adj. R^2	0.080	0.245	0.057	0.167
Panel C: Asset maturity				
Asset maturity	0.070* (1.81)	0.041 (1.45)	0.043* (1.66)	0.032 (1.52)
Controls	No	Yes	No	Yes
Observations	2005	1985	2005	1985
Adj. R^2	0.008	0.243	0.004	0.165
Panel D: Asset maturity (capped at 25 years)				
Asset maturity (cap.)	0.117*** (3.06)	0.110*** (3.14)	0.072*** (2.75)	0.070** (2.61)
Controls	No	Yes	No	Yes
Observations	2005	1985	2005	1985
Adj. R^2	0.015	0.246	0.008	0.166

Table IA.3: **Asset life and net book leverage cycles – cross-sectional regressions.** The dependent variable is *Maximum debt cycle length* in columns 1 and 2, and *Average debt cycle length* in columns 3 and 4, where cycle length depends on spikes in net book leverage. Firms with no leverage spike have a cycle length that is undefined and are dropped from the sample. We require a minimum of three years between subsequent spikes. In specifications 2 and 4 we control for all independent variables from Table 2. t -statistics are reported in parentheses. Standard errors are clustered at the industry level using Hoberg-Phillips fixed industry classification with 100 industries. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.

	Max debt cycle		Avg. debt cycle	
	(1)	(2)	(3)	(4)
Panel A: Useful life				
Useful life	0.128*** (4.96)	0.073*** (2.74)	0.082*** (3.56)	0.049** (2.03)
Controls	No	Yes	No	Yes
Observations	1812	1807	1812	1807
Adj. R^2	0.012	0.218	0.006	0.145
Panel B: Average capital age				
Capital age	0.623*** (9.31)	0.197*** (4.41)	0.448*** (7.88)	0.174*** (4.19)
Controls	No	Yes	No	Yes
Observations	1812	1807	1812	1807
Adj. R^2	0.073	0.221	0.050	0.149
Panel C: Asset maturity				
Asset maturity	0.026 (0.94)	0.049** (2.01)	0.015 (0.72)	0.034 (1.40)
Controls	No	Yes	No	Yes
Observations	1784	1779	1784	1779
Adj. R^2	0.001	0.217	0.000	0.143
Panel D: Asset maturity (capped at 25 years)				
Asset maturity (cap.)	0.046 (1.56)	0.073** (2.16)	0.027 (1.19)	0.037 (1.18)
Controls	No	Yes	No	Yes
Observations	1784	1779	1784	1779
Adj. R^2	0.002	0.217	0.001	0.143

Table IA.4: **Asset life and debt cycles – five-year filter.** The dependent variable is *Maximum debt cycle length* in columns 1 and 2, and *Average debt cycle length* in columns 3 and 4. Firms with no leverage spike have a cycle length that is undefined and are dropped from the sample. We require a minimum of five years between spikes. In specifications 2 and 4 we control for all independent variables from Table 2, except for asset maturity. t -statistics are reported in parentheses. Standard errors are clustered at the industry level using Hoberg-Phillips fixed industry classification with 100 industries. We use * $p < 0.10$, ** $p < 0.05$, and *** $p < 0.01$ to indicate p -values.