

Three-dimensional disk-based optical correlator

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Abstract. A total of 300 templates were stored as angularly multiplexed transmission holograms at multiple spots on a photopolymer disk. A novel correlator architecture is described and demonstrated that correlates all the templates against an input image within one disk rotation (≈ 20 ms). The projected performance of the system is 150,000 templates per disk and a processing rate of approximately 6000 correlations per second.

Subject terms: correlator; holographic correlator; photopolymer; holographic memories; optical processor.

Optical Engineering 33(12), 4051–4054 (December 1994).

1 Introduction

In recent years we have seen the implementation of several pattern recognition systems that use arrays of optical correlators to realize a variety of algorithms (e.g., template matching, radial basis functions, and neural networks). An array of correlators can be implemented by spatially multiplexing different filters on a two-dimensional (2-D) medium, frequently in a disk configuration.^{1–4} Alternatively, 3-D holographic storage can be used by superimposing multiple holograms utilizing either wavelength⁵ or angular^{6,7} multiplexing to form the correlation between the input and any stored reference. Finally, spectral and time domains can be used to store multiple filters in 2-D spectral hole-burning media.⁸ In this paper we present a method that combines angularly multiplexed storage in 3-D media with spatial multiplexing to form a 3-D disk.⁹ The 3-D disk allows us to store a very large number of gray-scale templates, whereas the disk rotation proves convenient for implementing the necessary shift in one of the two dimensions for the calculation of the image correlation function. The architecture we describe can be implemented with any holographic storage medium that can be fabricated into a thick slab (to allow volume holography) with sufficient area (to make a sizable disk). For instance, photorefractive crystals can be used.⁹ The 3-D disk used in the experimental demonstration in this paper is constructed out of HRF-150 DuPont photopolymer.¹⁰ In a previous publication¹¹ we have reported the storage of 10 angularly multiplexed holograms in this material.

2 Theory of Operation

When a thick hologram is used to store the Fourier-transform filter in a VanderLugt correlator, the shift invariance is destroyed in one of the two dimensions.¹² As a result, the output of such a system is simply one line of the 2-D correlation function. We can use angularly multiplexed holograms in a volume to store multiple templates and use the second dimension of the output plane to display in parallel one line of each of the 2-D correlation patterns between the input and the stored templates. By translating the input image, the 2-D correlation patterns are generated sequentially, one line at a time.^{2,6,7} In this paper we describe an alternative solution in which we translate the holographic medium instead. The reference holograms are stored by Fourier transforming in one direction and imaging in the other. Since the input is imaged onto the hologram in one dimension, translating the hologram produces the desired relative shift between input and reference that is necessary to compute the correlation function in two dimensions. Since the holographic medium is a 3-D disk, this translation is provided by the disk rotation. Moreover, in this architecture, we increase the number of templates by storing multiple angularly multiplexed holograms at multiple locations on the disk. Disk rotation is also conveniently used to access the different locations in sequence.

The optical setup is shown in Fig. 1. The image f to be stored is presented to the system on a spatial light modulator (SLM—an Epson LCTV in the experiment). The first lens takes the Fourier transform of the image presented on the SLM. At the Fourier plane of the first lens, the image is filtered to edge-enhance it and also to remove the diffraction orders of the SLM. The second lens transforms this filtered signal back into an image that is demagnified by 1/5. Using three cylindrical lenses, the image is imaged in the along-“track” (x) direction and Fourier transformed in the radial (y) direction. The two spherical lenses, following the cylindrical

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Paper 39034 received Mar. 24, 1994; revised manuscript received June 18, 1994; accepted for publication June 20, 1994.
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lenses, demagnify the 1-D Fourier transform and 1-D image by a factor of 1/4.

This pattern is then interfered with a plane wave with spatial frequency μ and stored in the thick photopolymer film laminated on a blank glass optical disk. Thus the pattern f imaged in the x direction and Fourier transformed in y is holographically stored on the disk. Additional holograms are multiplexed at the same disk location by changing the angle of the reference beam using a rotating mirror. A 4F system of lenses is used in the reference arm, as shown in Fig. 1, to change the incident angle of the reference beam without changing its location on the disk. The effective transmittance of the hologram can be written as $T(x,y) \approx \tilde{f}^*(x,y/\lambda F) \exp(j2\pi\mu x)$, where \tilde{f} is the 1-D Fourier transform of f .

To generate the correlation function between a recorded function f and an input function g , we present g on the SLM. The function g is mapped into the pattern $\tilde{g}(x,y/\lambda F)$ after going through the optical system that transfers it to the plane of the disk. The signal after the disk is given by $\tilde{g}(x,y/\lambda F) \tilde{f}^*(x,y/\lambda F) \exp(j2\pi\mu x)$. The lens placed between the disk and the detector array in Fig. 1 takes the 2-D Fourier transform of this signal. The result on the detector plane is given by¹²

$$S(x_d, y_d) \approx \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \tilde{g}\left(\frac{x,y}{\lambda F}\right) \tilde{f}^*\left(\frac{x,y}{\lambda F}\right) \times \exp\left\{-j\frac{2\pi}{\lambda F}[x(x_d - \mu\lambda F) + yy_d]\right\} dx dy \times \text{sinc}\left(\frac{L\mu}{F}(x_d - \mu\lambda F)\right), \quad (1)$$

where L is the thickness of the disk. The different plane-wave references (μ 's) used to record each angularly multiplexed hologram result in the reconstructions being uniquely shifted on the detector plane to $x_d = \mu\lambda F$. In addition, the sinc function in Eq. (1) places a window in the x_d direction, which has the benefit that it reduces the crosstalk between different correlations. Specifically, the line detectors are spaced in the x_d direction by $\Delta x_d = nF/L\mu$, where n is a small integer. This places each of the adjacent line detectors in the n 'th nulls of its neighbors, thereby minimizing crosstalk. Writing the product of Fourier transforms in the y direction as a correlation function and observing the light amplitude at $x_d = \mu\lambda F$, we obtain from Eq. (1)

$$S(\mu\lambda F, y_d) \approx \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x,y)f(x,y-y_d) dx dy. \quad (2)$$

This is an inner product in the x direction and correlation in y . In other words, it is one line of the full 2-D correlation function between f and g .

Using disk rotation as approximately a linear shift $\theta(t)$ in the x direction generates the full 2-D correlation function with time:

$$S'(\mu\lambda F, y_d, t) \approx \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x,y)f[x+\theta(t),y-y_d] dx dy. \quad (3)$$

The intensity at the detector is $I(\mu\lambda F, y_d, t) = S' S'^*$, and therefore the detected signal is the square of the correlation

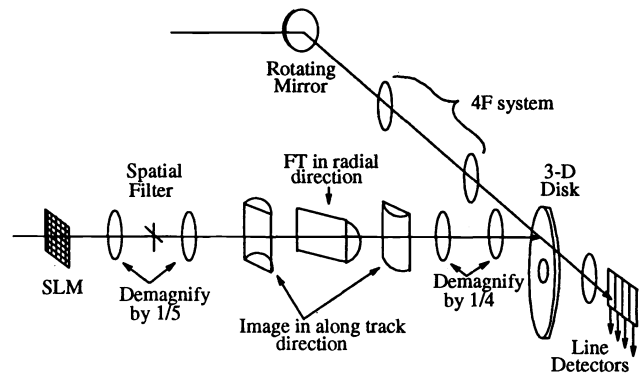


Fig. 1 3-D disk-based optical correlator setup.

function. With a thick medium, multiple holograms can be recorded at a single spot on the disk, using angle multiplexing. Therefore, different 2-D correlation functions for each multiplexed hologram can be generated one line at a time and detected in parallel.

3 Disk Rotation Effects

In this architecture we make use of disk rotation during reconstruction to shift the stored images with respect to the input in one dimension (x) and thus form the complete correlation. Disk rotation, however, is only approximately equivalent to a shift. In this section we analyze the effects due to rotation of the image. We analyze this effect ignoring the effects due to the finite thickness of the hologram, since the observed rotation effects are identical for 2-D and 3-D holograms. We calculate the effects of rotation by considering the correlation between an individual pixel at the input image and a pixel of one of the images stored in the hologram. The signal at the plane of the disk is focused in the x direction and a plane wave in the y direction, and therefore can be written as $S \approx \exp(-j2\pi\beta y) \text{rect}(x/\delta)$, where β is the spatial frequency in the y direction and δ is the pixel size. This signal is stored with a plane-wave reference $R = \exp(-j2\pi\mu x)$ with spatial frequency μ in the x direction. The recorded hologram can be written as

$$RS^* = \exp(-j2\pi\mu x) \exp(j2\pi\beta y) \text{rect}(x/\delta). \quad (4)$$

The hologram is then rotated by $d\theta$ about a center of rotation in the x - y plane a distance r away from the center of the x,y coordinates. This rotation results in the coordinates being transformed according to $x' \approx x - (y+r)d\theta$ and $y' \approx y + xd\theta$. Substituting these into Eq. (4), the hologram can be expressed in terms of the unrotated coordinates (x,y) as

$$RS^* = \exp\{j2\pi\mu[x - (y+r)d\theta]\} \exp(j2\pi\beta y) \times \exp(j2\pi\beta d\theta x) \text{rect}\left[\frac{x - (y+r)d\theta}{\delta}\right]. \quad (5)$$

We multiply the above expression by S to generate the 1-D inner product and 1-D correlation. After we expand and simplify the exponents, we obtain

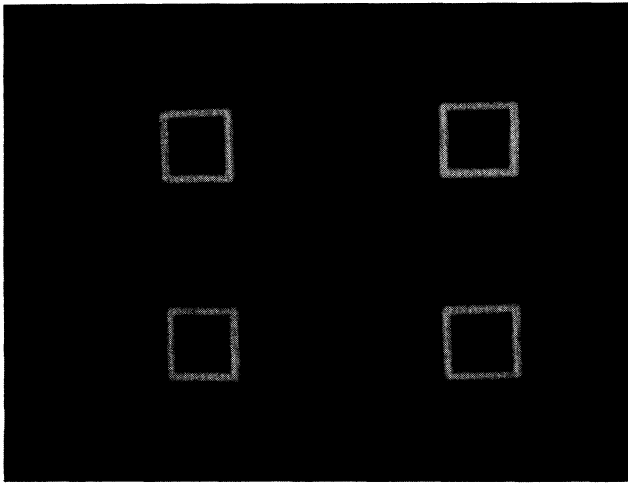


Fig. 2 Image used to test correlator.

$$\begin{aligned}
 SRS^* &= \exp(j2\pi\mu x) \exp(-j2\pi\mu d\theta y) \\
 &\times \exp(j2\pi\beta d\theta x) \operatorname{rect}\left[\frac{x - (y+r)d\theta}{\delta}\right] \\
 &\times \operatorname{rect}\left(\frac{x}{\delta}\right). \quad (6)
 \end{aligned}$$

After the Fourier-transforming lens, the terms in Eq. (6) correspond to the desired signal and shifts of this signal on the detector plane, depending on the amount of rotation $d\theta$. The terms and their effects are listed below:

- $\exp(j2\pi\mu x)$ is the reconstructed plane wave without rotation—the desired signal.
- $\exp(-j2\pi\mu d\theta y)$ corresponds to a shift in the y direction on the detector plane, and it can be compensated by simply reinterpreting the detected signal.
- $\exp(j2\pi\beta d\theta x)$ corresponds to a shift in the x direction on the detector plane, and it can be neglected if $N^2\delta/r < 1$, where N is the number of pixels in one dimension.
- $\operatorname{rect}[(x - (y+r)d\theta)/\delta] \operatorname{rect}(x/\delta)$ is due to the finite pixel size. The relative rotation between the two rect functions is negligible if $y < r/N$.

In our experimental setup, the shift of the correlation pattern was almost entirely in the y direction. If the above conditions for neglecting the rotation effects are not satisfied, the result is a reduction in the shift invariance of the correlator in the x direction.

4 Experimental Correlation

Using the system shown in Fig. 1, 300 transmission holograms were stored at a radius of 5 cm along a “ring” around the disk. Using DuPont’s HRF-150 film and exposing with 488-nm light, three holograms were angularly multiplexed at each spot on the disk. The disk was then rotated to expose a total of 100 different spots; since at each spot three holograms were recorded, a total of 300 holograms were stored. The size of the illuminated region was approximately

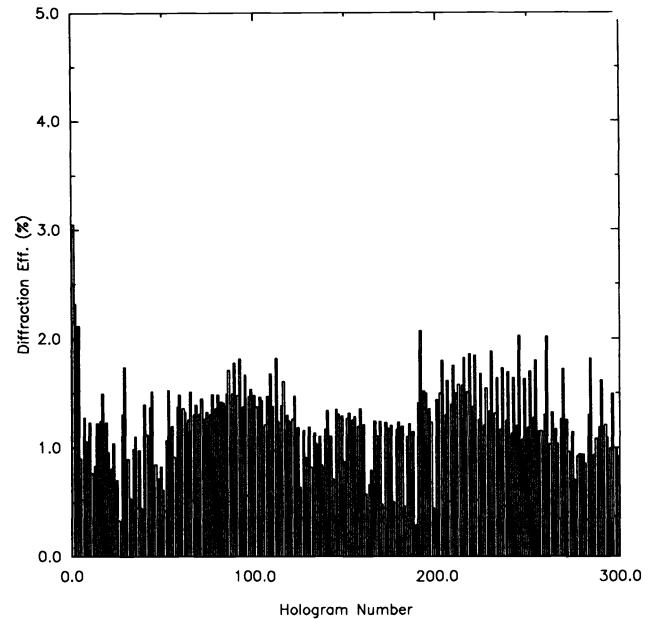


Fig. 3 Diffraction efficiency of 300 holograms—three holograms at a spot with 100 spots on a ring of a 3-D disk.

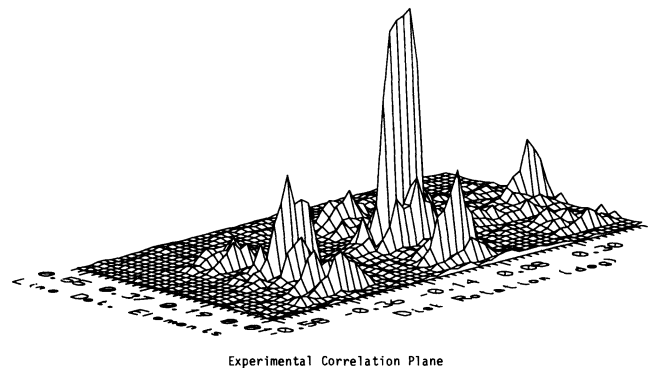


Fig. 4 Experimental autocorrelation squared of the pattern shown in Fig. 2 and produced using the optical disk-based correlator.

0.9×0.6 mm with a signal intensity of 2.4 mW/cm^2 and a reference-beam intensity of 2.0 mW/cm^2 . After each spot was sensitized with preillumination¹¹ using the reference beam for 25 s, each hologram was exposed for 10 s. The disk rotation between spots was 3.5 deg, and the angular separation of the three multiplexed holograms was 1.5 deg. The holograms were made with the image of four boxes shown in Fig. 2. The diffraction efficiency for the 300 holograms is shown in Fig. 3. The 3-D disk was made by pressing (laminating) the 38- μm -thick photopolymer film onto the glass disk.

Figure 4 is an experimental plot of the autocorrelation function squared of the four-box image in Fig. 2. It agrees reasonably well with the expected autocorrelation of this image. Figure 4 was generated by storing the image on the disk as explained above, and then presenting the same image as input to the system. The correlation plane was sampled by a linear CCD detector array. In this experiment the disk was not continuously rotated. Instead, the detector was read out, the disk was rotated by 0.02 deg, and the process repeated

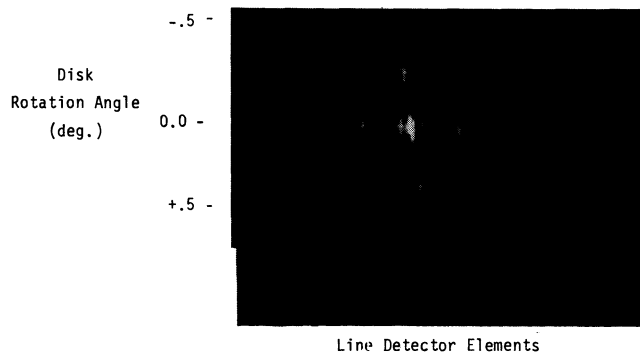


Fig. 5 2-D gray-scale depiction of the pattern in Fig. 4, showing the slant of the correlation pattern due to disk rotation.

60 times to obtain 60 lines of the 2-D correlation pattern. Since the boxes occupy a large portion of the input plane (SLM), Fig. 4 demonstrates that the correlation ability exists across most of the input plane. Figure 5 is the gray-scale image representation of the correlation function in Fig. 4. Notice the slant in the correlation pattern that is due to disk rotation. The shift produced by the experimental setup was mostly in the y direction (labeled line detector elements in Fig. 5), as predicted.

5 Discussion

We have demonstrated a multichannel disk-based optical correlator using both angular and spatial multiplexing of volume holograms. The full 2-D correlation function of an input image against stored templates is generated by using disk rotation to shift one image over the other, thus reading out one line of each correlation function in parallel. A total of 300 holograms, in the required 1-D image and 1-D Fourier-transformed format, were stored on a single ring of an optical disk. The correlation generation was experimentally verified and compared with theory.

The thickness of the material was about 38 μm . Using the spin-coating technique, we have made a photopolymer film thick enough ($\approx 300 \mu\text{m}$) to store more than 50 holograms in one spot. Using the whole area of the disk and leaving enough blank space between spots, approximately 3000 spots can be stored on a 5-cm-radius disk. Therefore, if polymer film of approximately 300- μm thickness can be manufactured, then this results in a storage capacity of $\approx 150,000$ holograms or templates. The correlator described above can achieve very high correlation rates without the need of fast SLM. However, the processing bottleneck is shifted to the detectors. The speed of the current correlator is limited by the speed of the linear CCD detector arrays. A linear detector array is needed for each angular multiplexed hologram position. For example, if 50 holograms are multiplexed at each spot, then 50 linear detector arrays are employed, each with several hundred pixels. With the 50 holograms per spot and linear CCD detector arrays with 500 elements each running at 30 MHz, the correlation rate is about 6000 correlations per second. Less than 10 mW of light incident on the film is sufficient to realize this correlation rate, assuming a measured diffraction efficiency of 2×10^{-3} when 50 holograms were multiplexed in a 38- μm -thick film.¹³ The correlation rate

could be significantly increased using custom detector arrays that perform a winner-take-all operation on the pixels and report the location and magnitude of the largest correlation peak off chip. Note that the above performance is achievable without the need to develop new components.

Acknowledgments

This work was supported by AFOSR and Northrop. The photopolymer was graciously made available to use by DuPont; in particular, the authors wish to thank Jay Calio of DuPont. In addition, we appreciate the many helpful discussions with Dr. Sidney Li.

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