

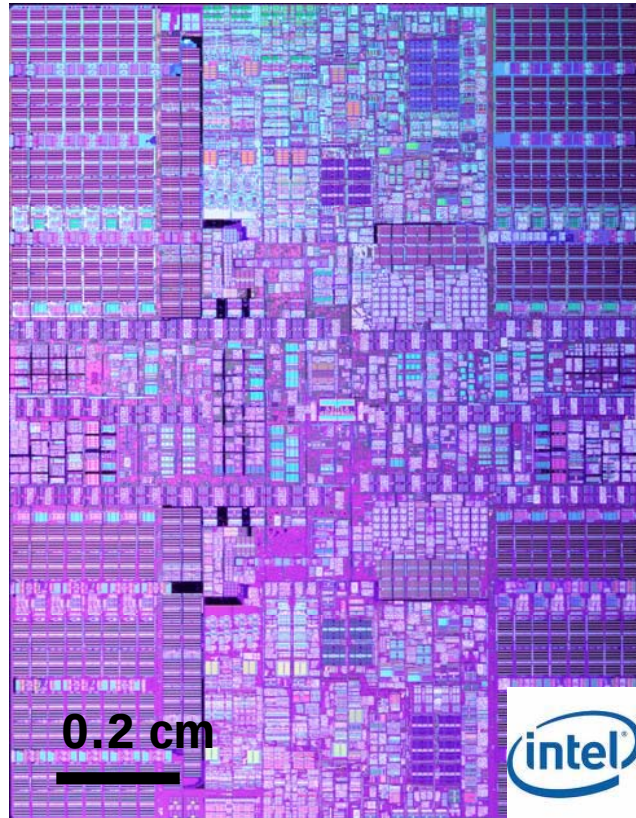
Frontiers in Nanoscale Science I

Incredibly Shrinking Transistor
Semiconductor Nanostructures
Quantum Transport
Molecular Electronics

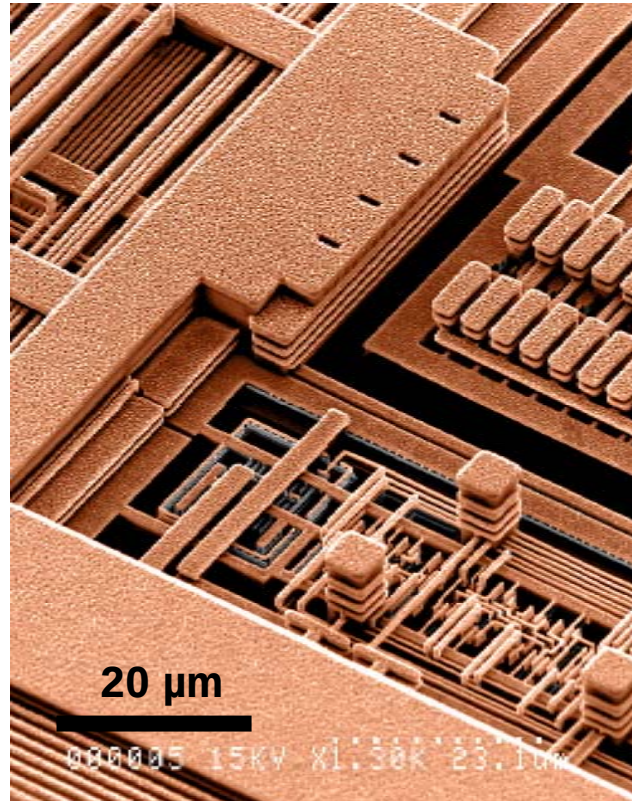
Frontiers in Nanoscale Science I

Incredibly Shrinking Transistor

Integrated Circuits



CPU as of 2008
~ 800 million transistors



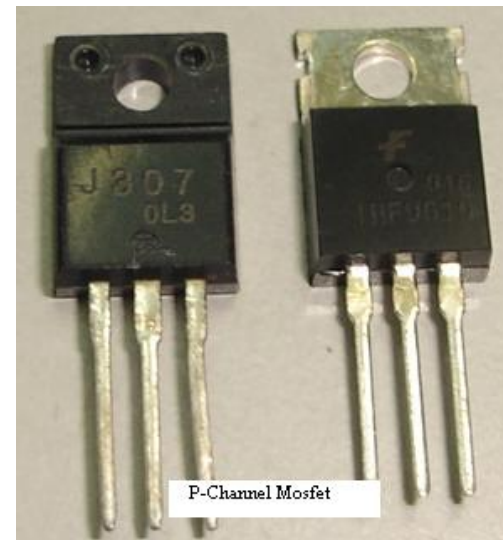
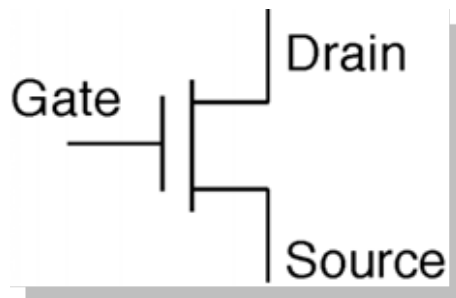
metal lines in a CPU

Transistor

- fundamental active electronic component of digital circuits
- *three* terminal device
- does 2 functions:
 1. *switch* – 0 / 1 → perform logic
 2. *gain* – amplifies digital signals

common form – field-effect transistor (FET)

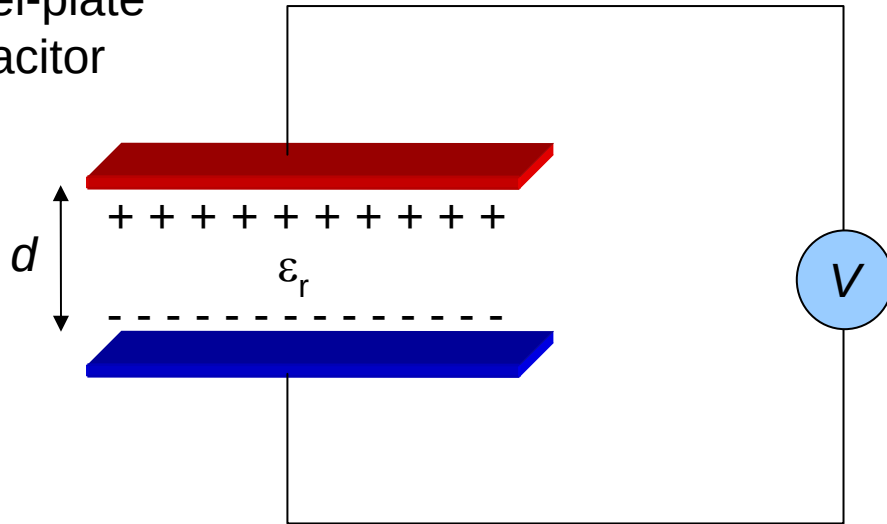
FET - symbol



P-Channel Mosfet

Concept of Capacitance

parallel-plate
capacitor



$$\Delta Q = C \Delta V$$

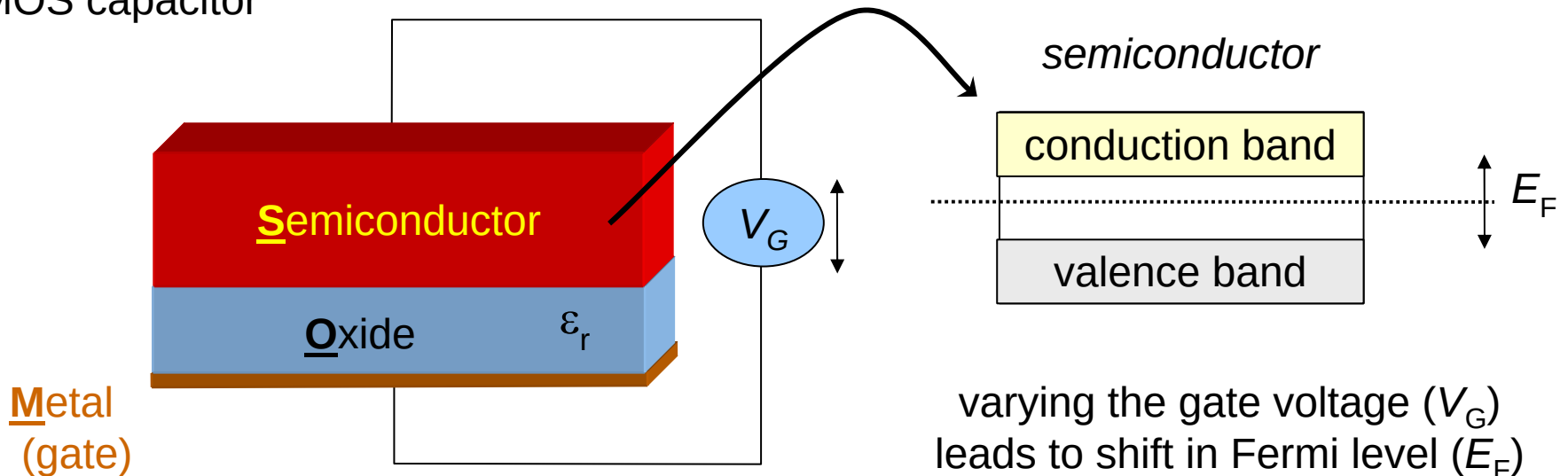
$$C = \epsilon_0 \epsilon_r A / d$$

A – cross-sectional area
of the plates

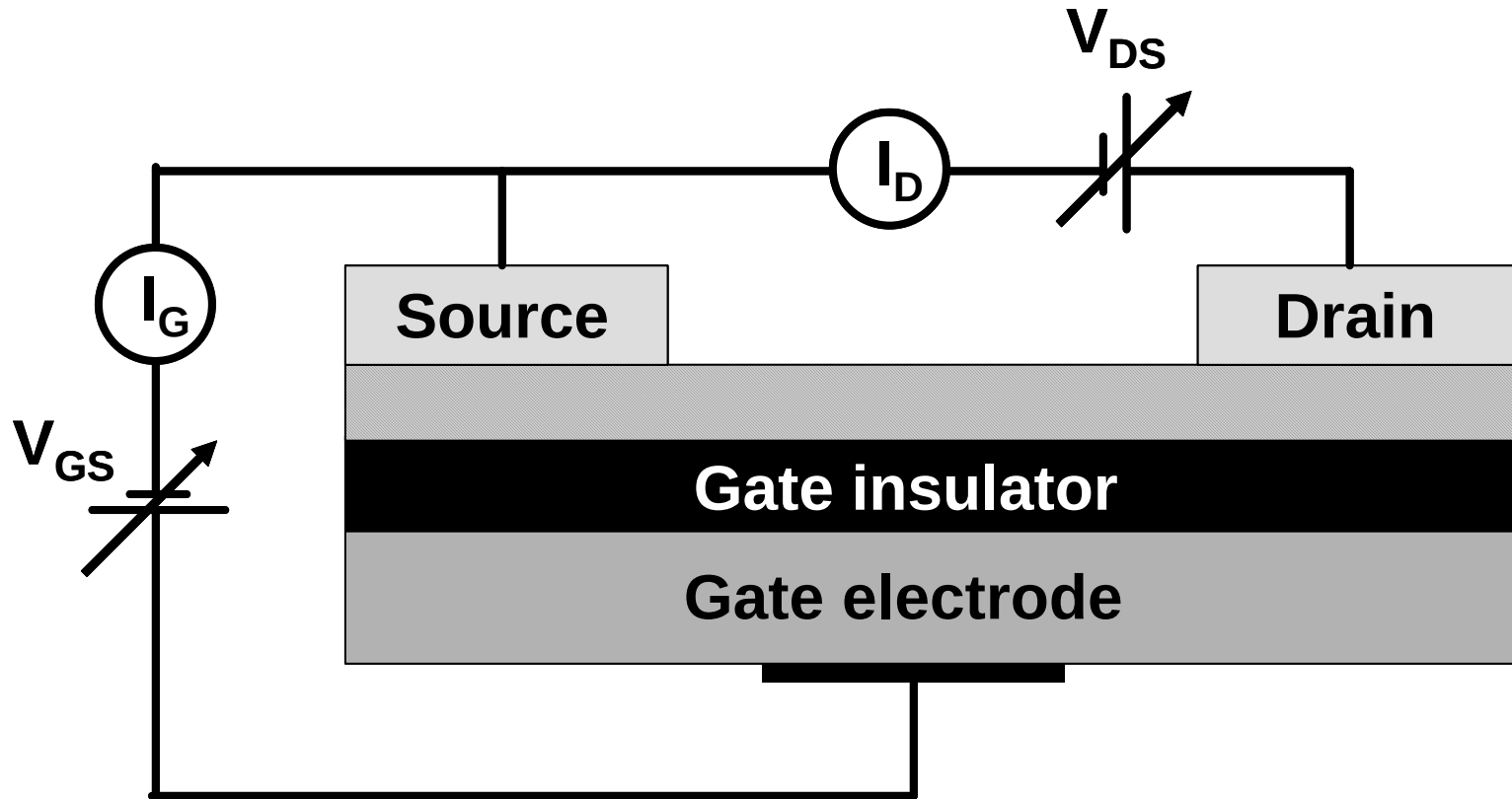
Q – Charge

ϵ – dielectric constant

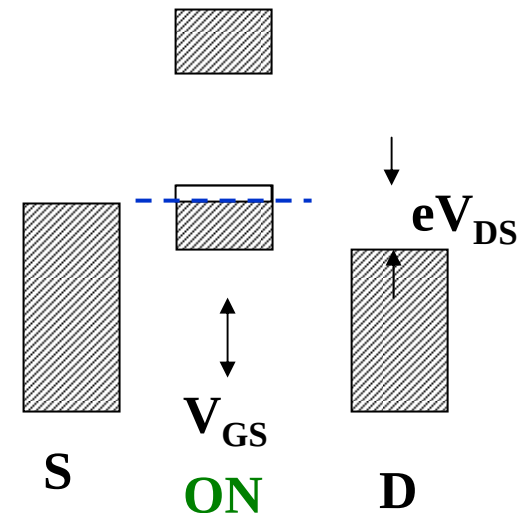
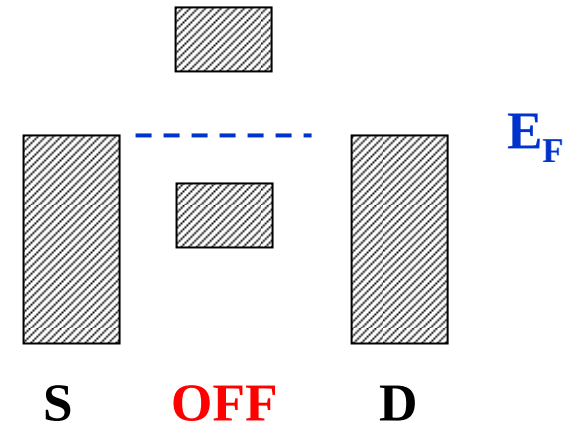
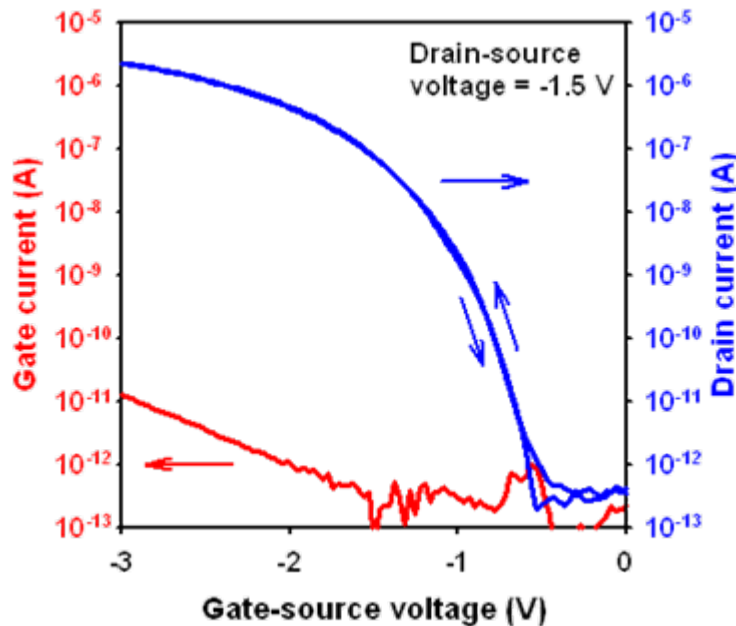
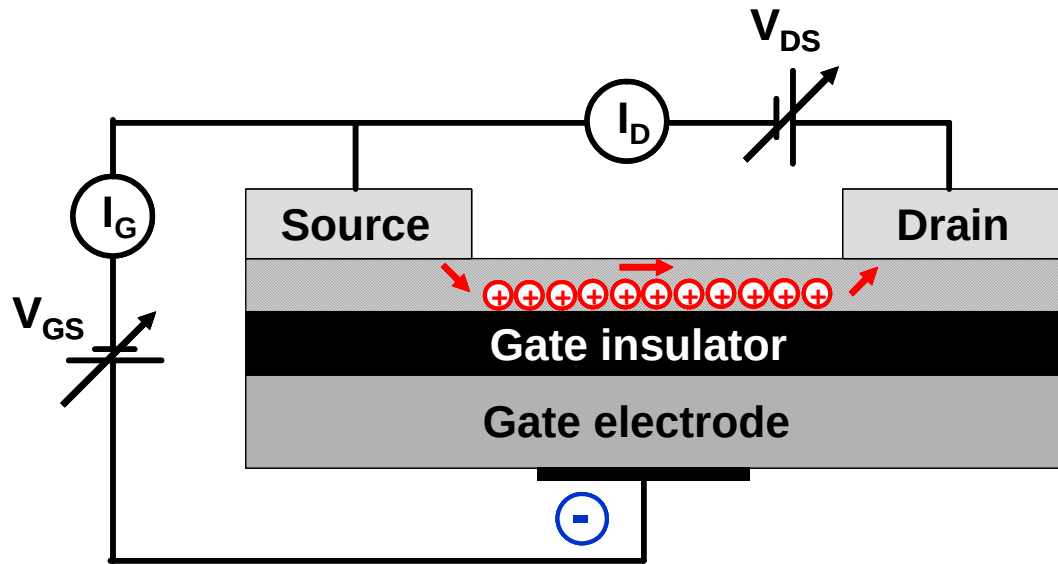
MOS capacitor



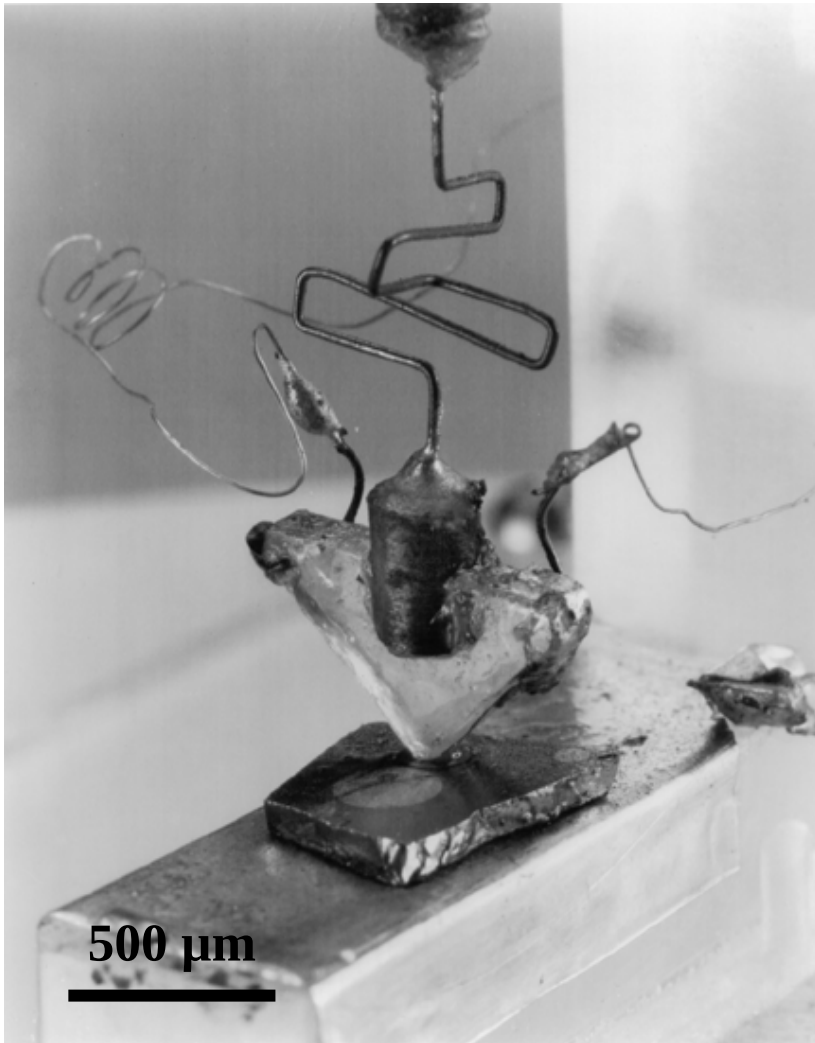
How does a modern field-effect transistor work ?



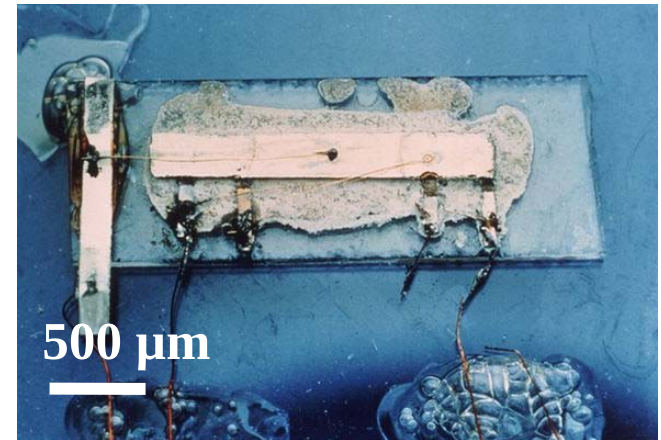
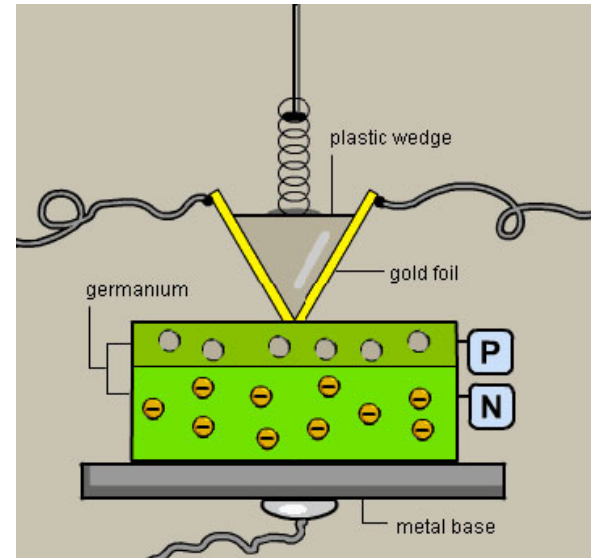
How does a modern field-effect transistor work ?



The beginning....

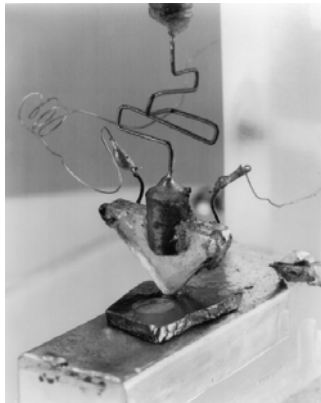


W.B. Shockley, J. Bardeen and W.
H. Brattain, Bell Labs 1947

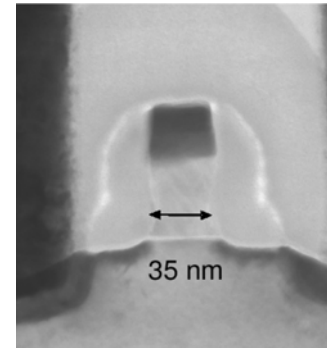
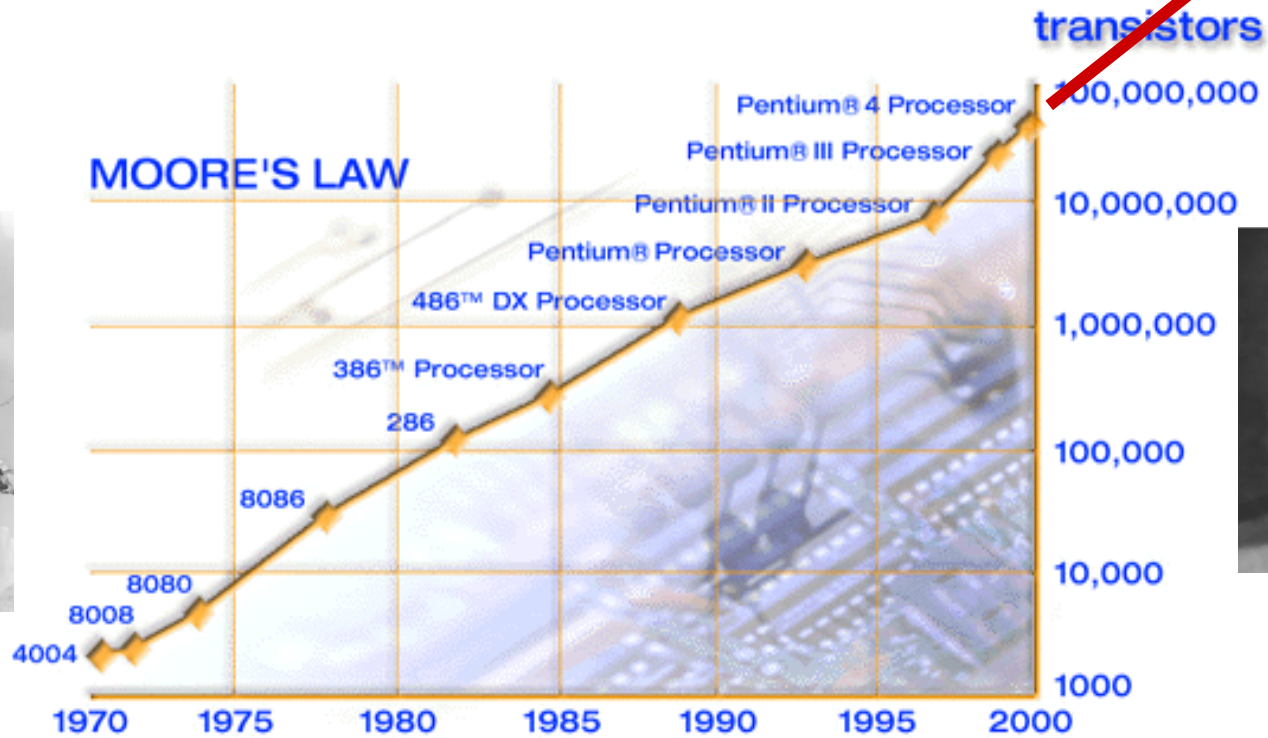


J. Kilby The first working
integrated circuit

The incredible shrinking of the transistor



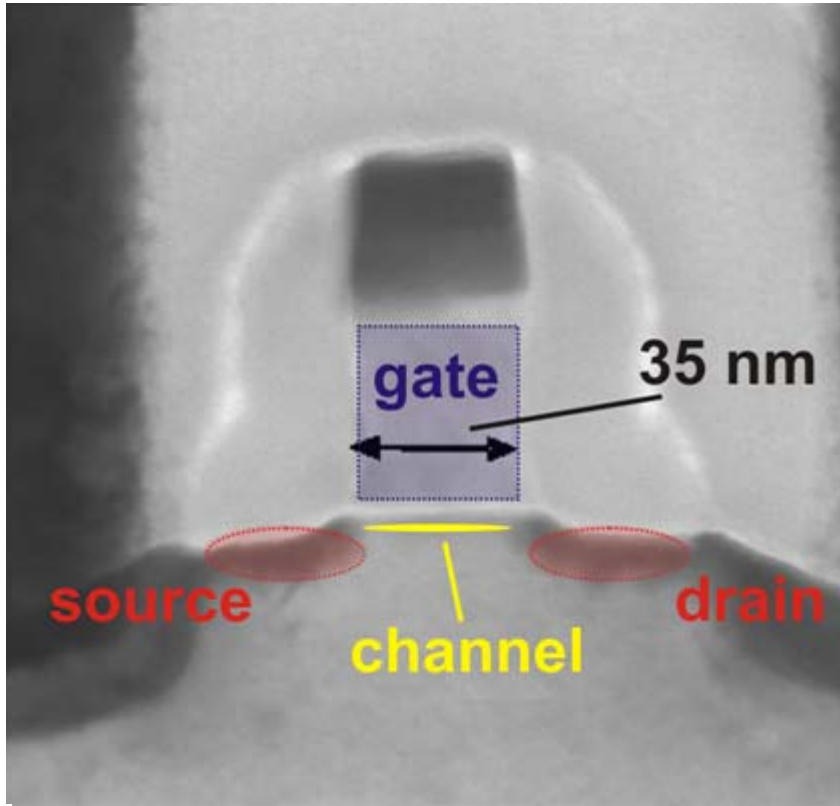
transistor
1947



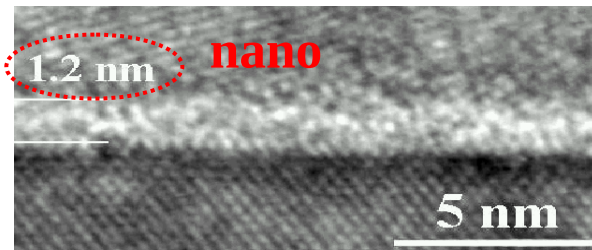
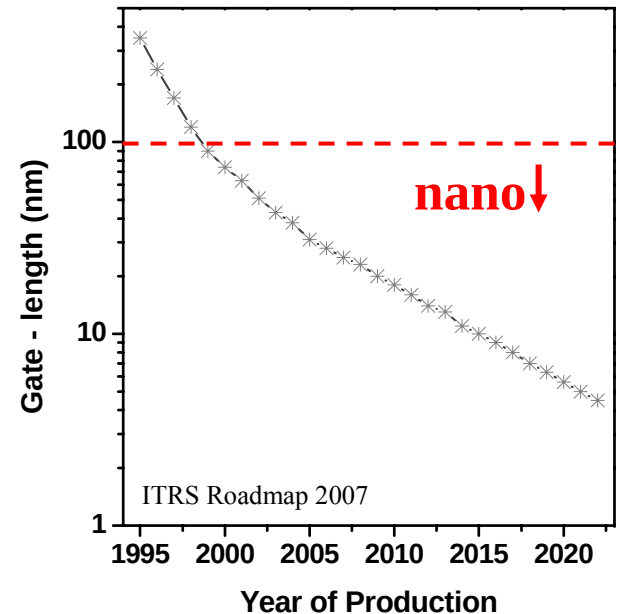
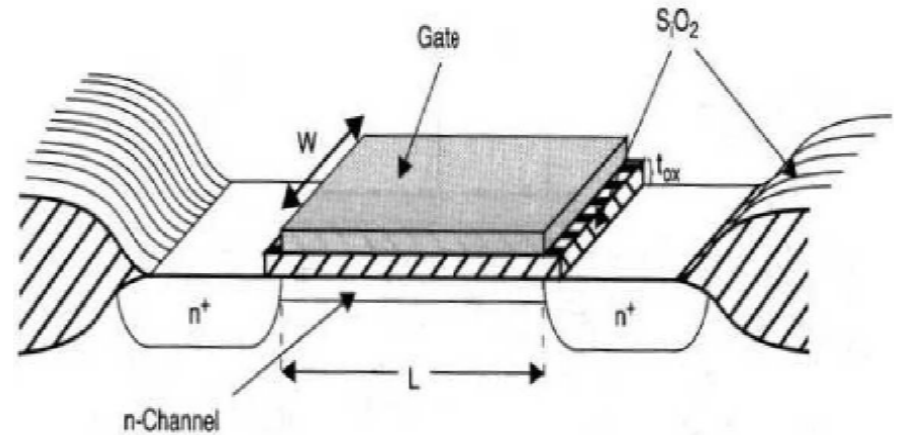
transistor
2005

→ Shrinking of parts of the transistor to atomic dimensions

The incredible shrinking of the transistor

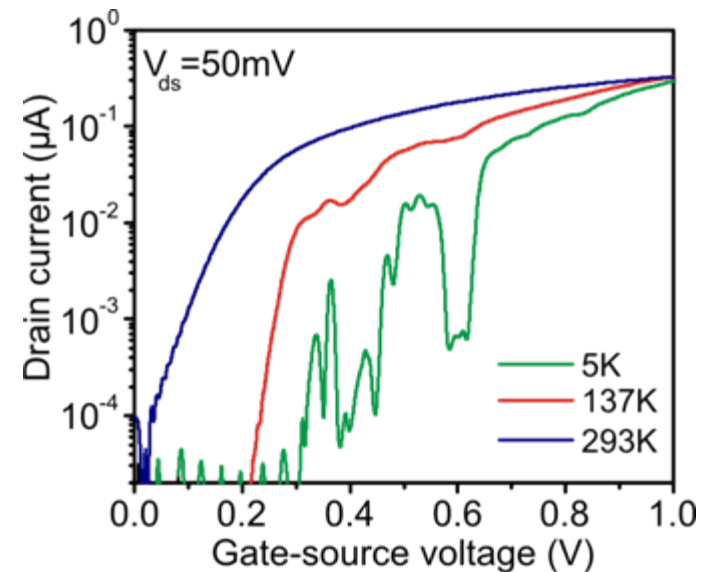
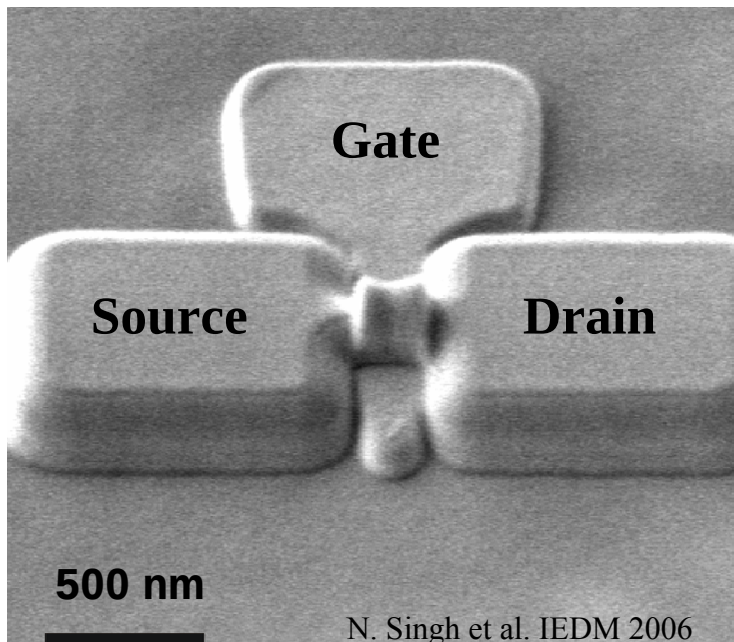
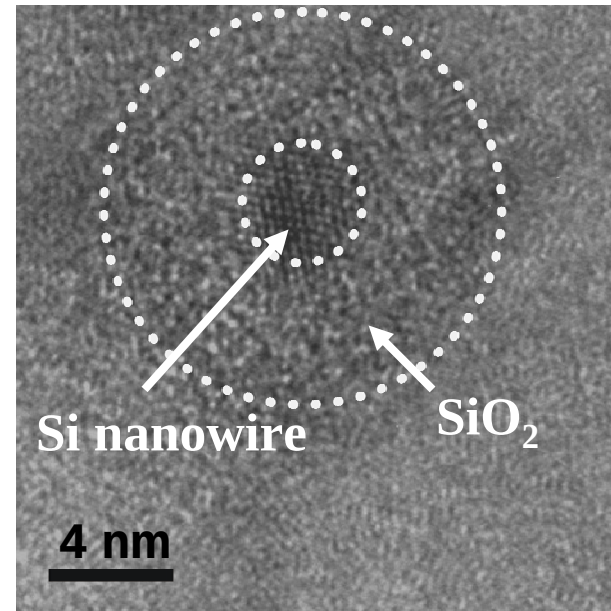
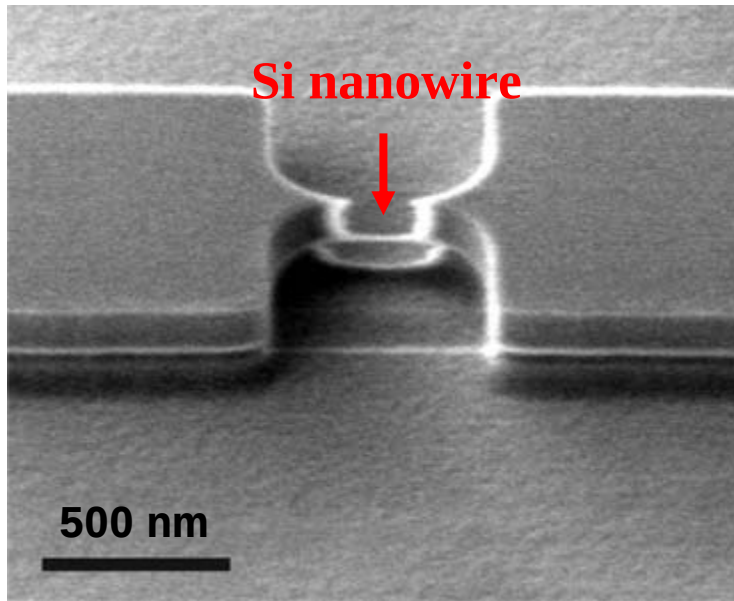


TEM image of a contemporary FET

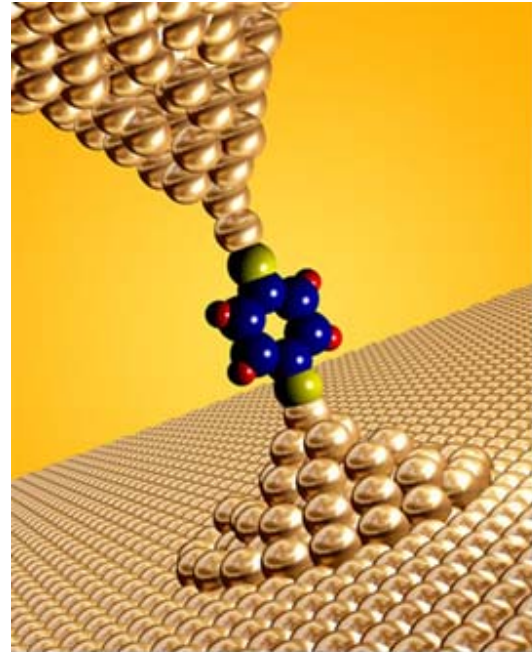
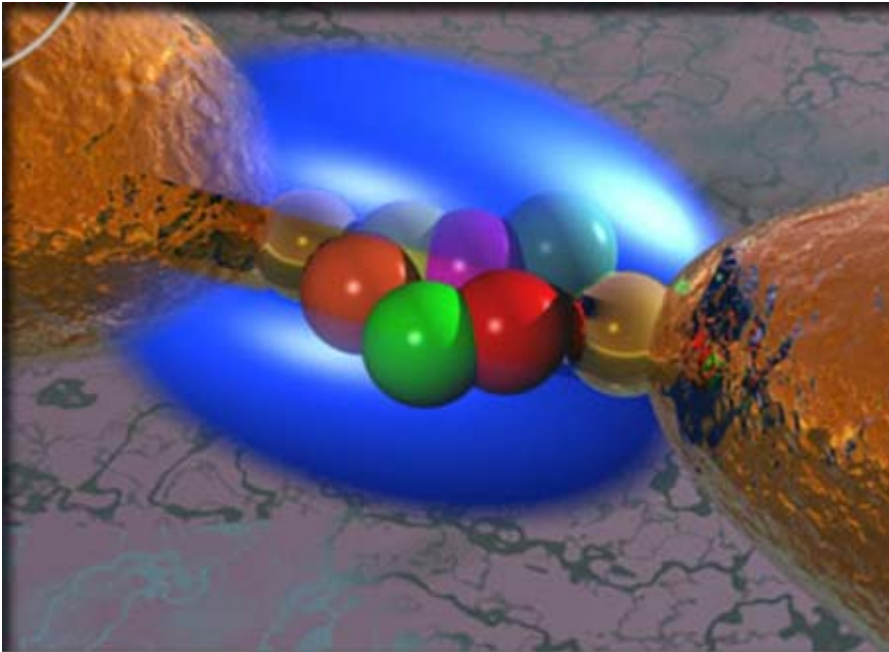


Electronmicroscope image of a SiO_2 gate insulator
LETI, CEA, France

The incredible shrinking of the transistor – **future**



Molecular Electronics



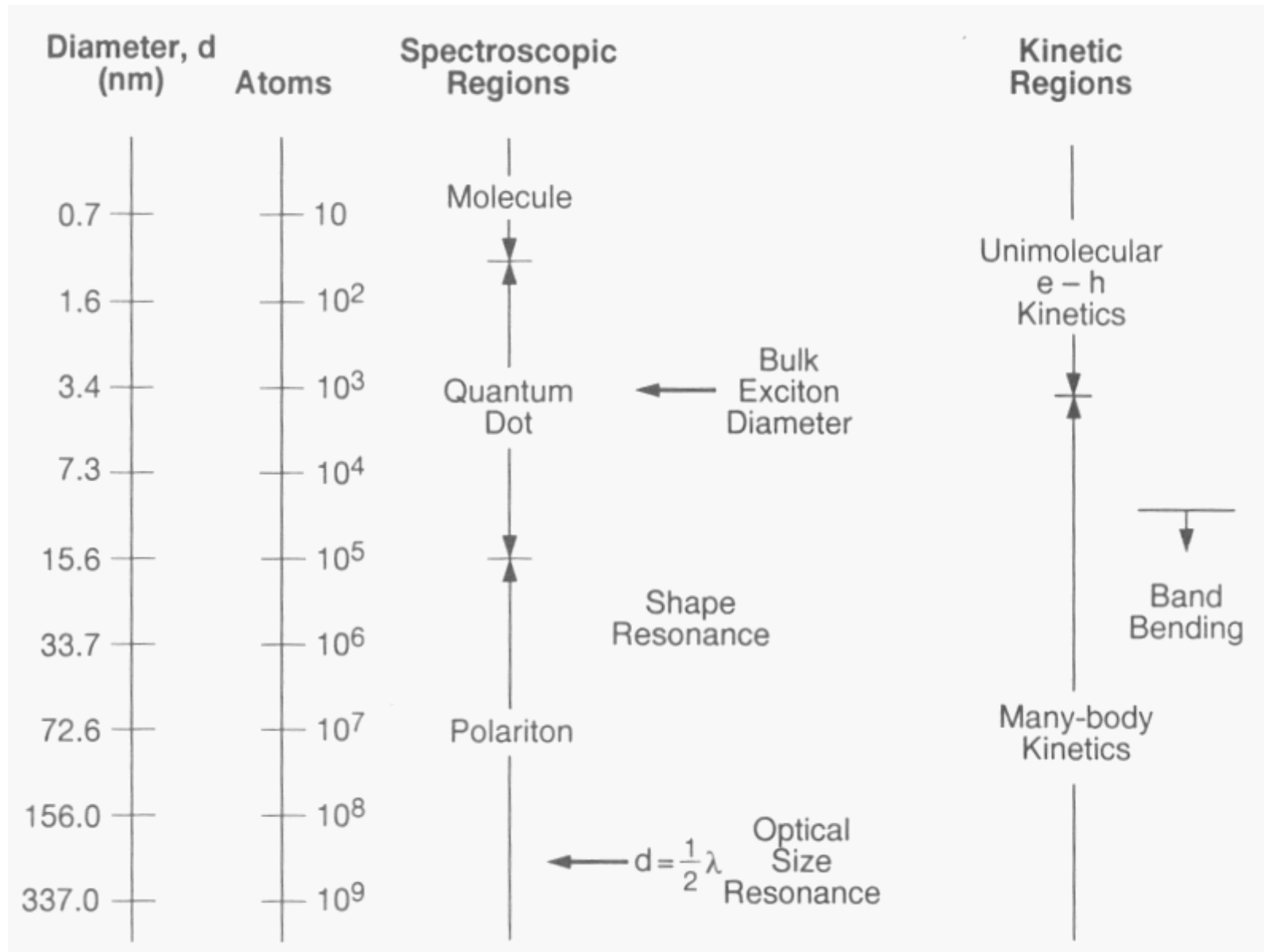
Frontiers in Nanoscale Science I

Semiconductor Nanostructures

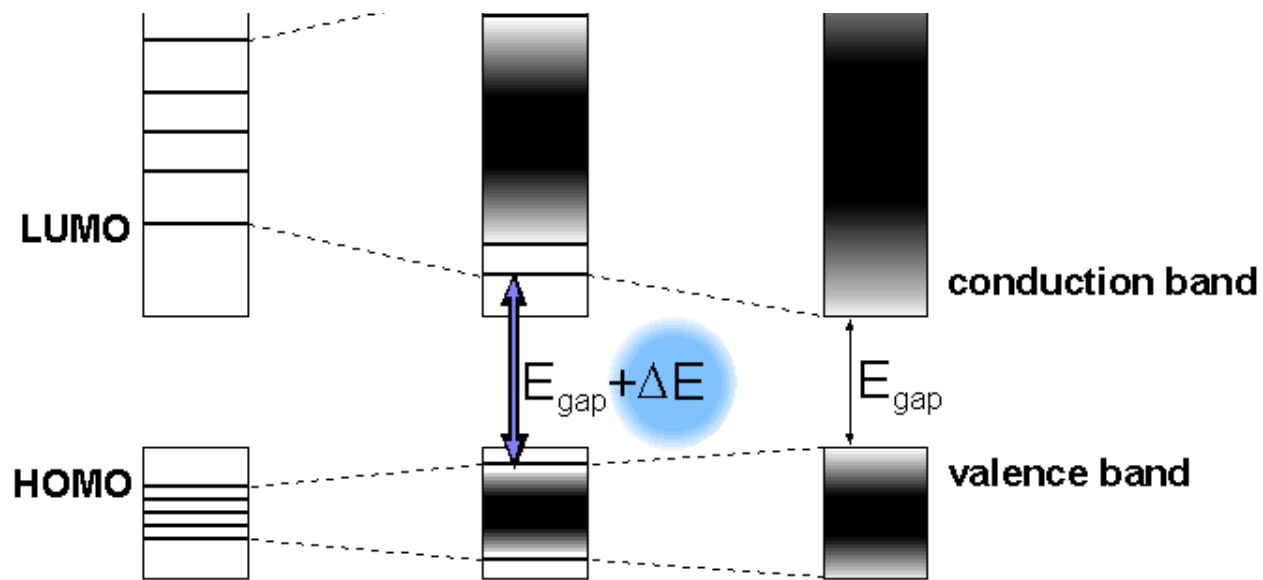
Semiconductor Nanostructures

- basics
- MBE quantum dots
- nanocrystals
- nanowires

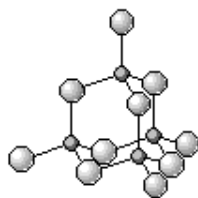
Size regimes



From solid state to molecules

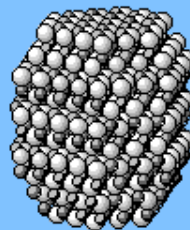


cluster



$\varnothing \approx 1 \text{ nm}$

nanocrystal

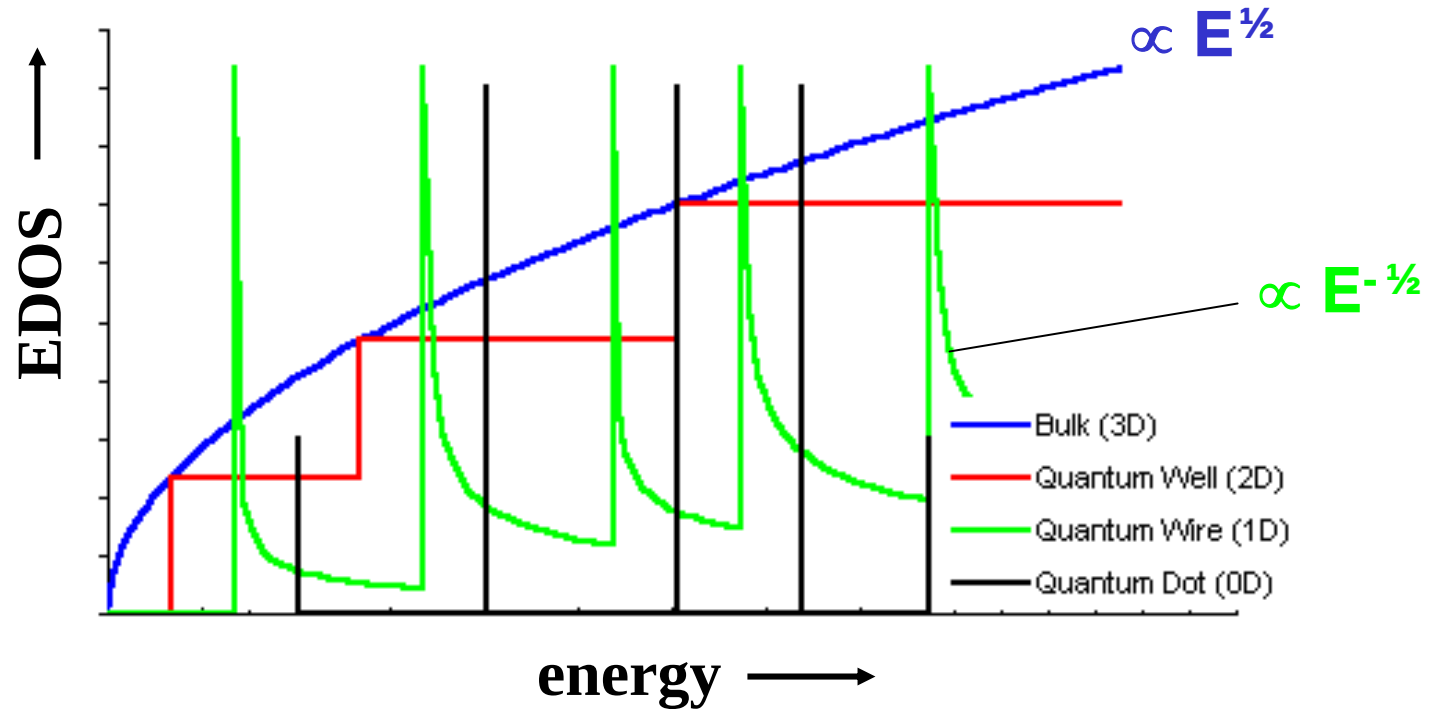


$\varnothing = 2\text{-}10 \text{ nm}$

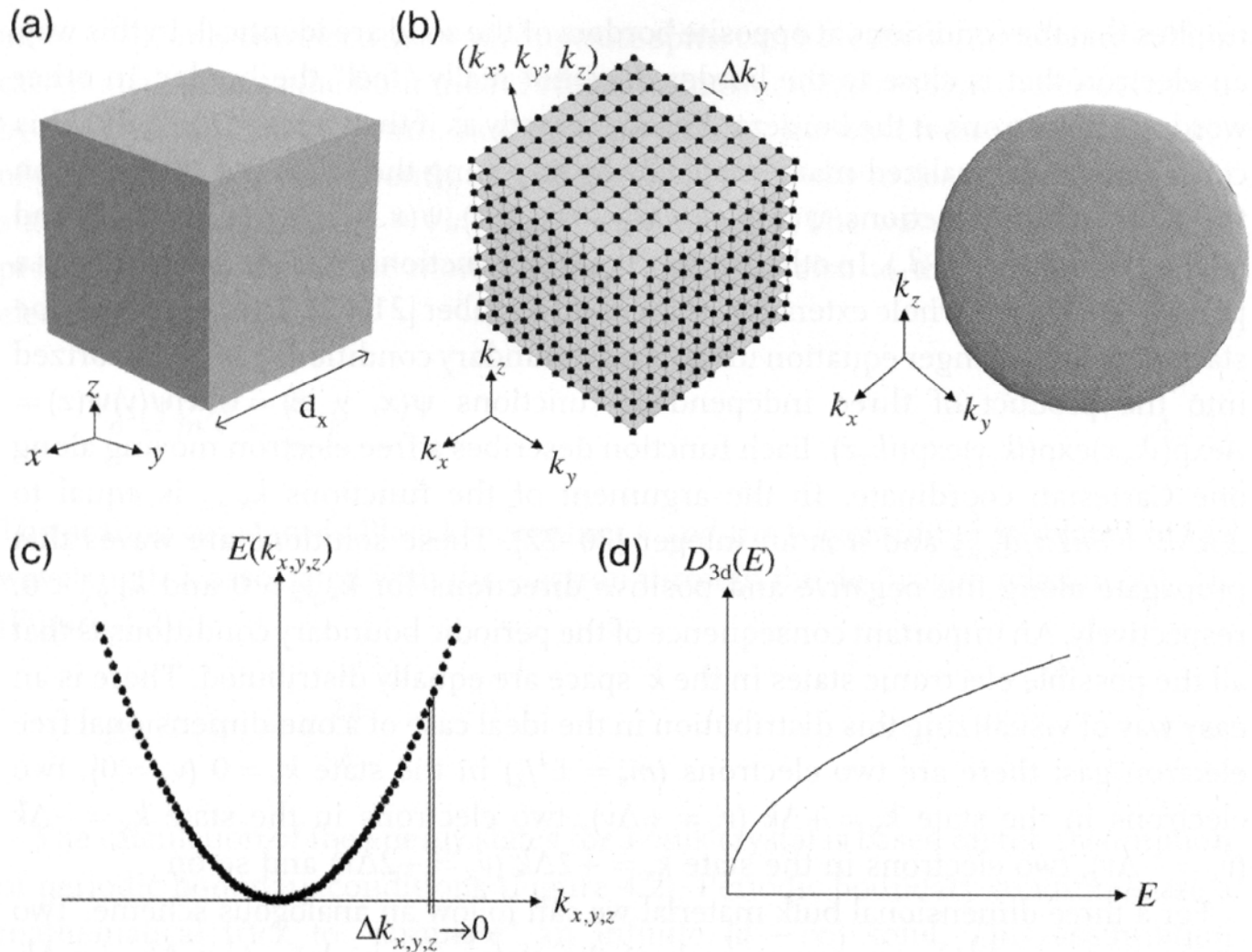
macrocrystal

$\varnothing > 20 \text{ nm}$

Electronic density of states (EDOS)



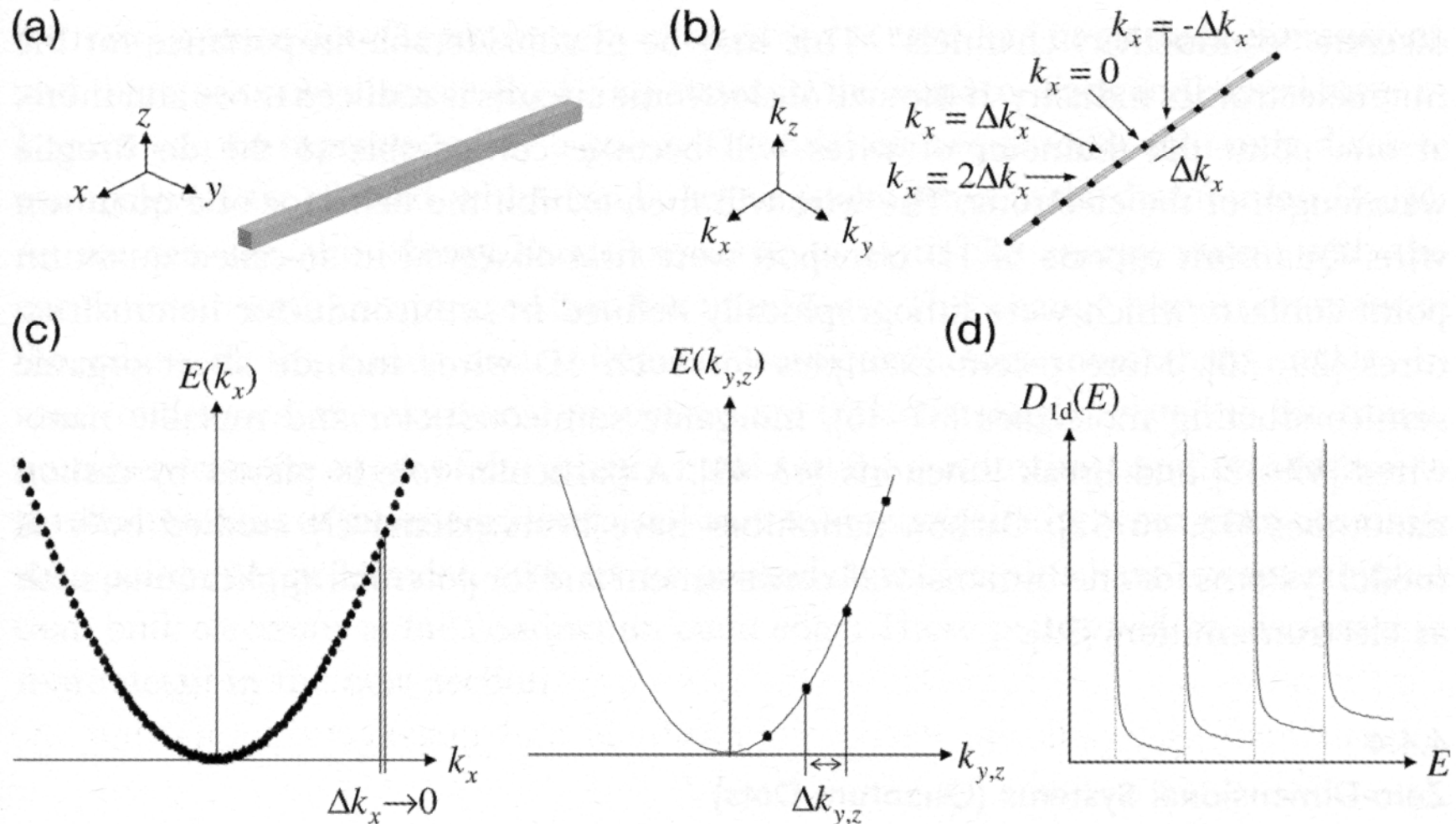
3D systems (bulk material)



$$D_{3D}(k) = \frac{dN(k)}{dk} \propto k^2$$

$$D_{3D}(E) = \frac{dN(E)}{dE} = \frac{dN(k)}{dk} \frac{dk}{dE} \propto E \cdot \frac{1}{\sqrt{E}} \propto \sqrt{E}$$

1D systems (nanowires)

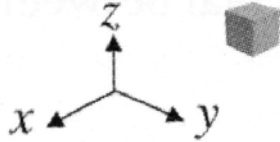


$$D_{1D}(k) = \frac{dN(k)}{dk} \propto 1$$

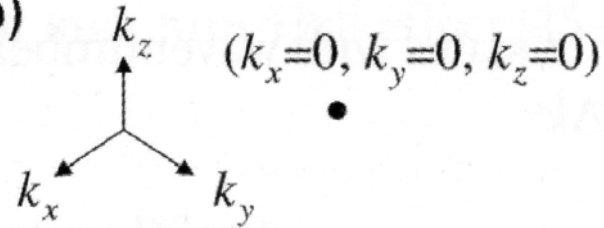
$$D_{1D}(E) = \frac{dN(E)}{dE} = \frac{dN(k)}{dk} \frac{dk}{dE} \propto 1 \cdot \frac{1}{\sqrt{E}} \propto \frac{1}{\sqrt{E}}$$

0D systems (quantum dots)

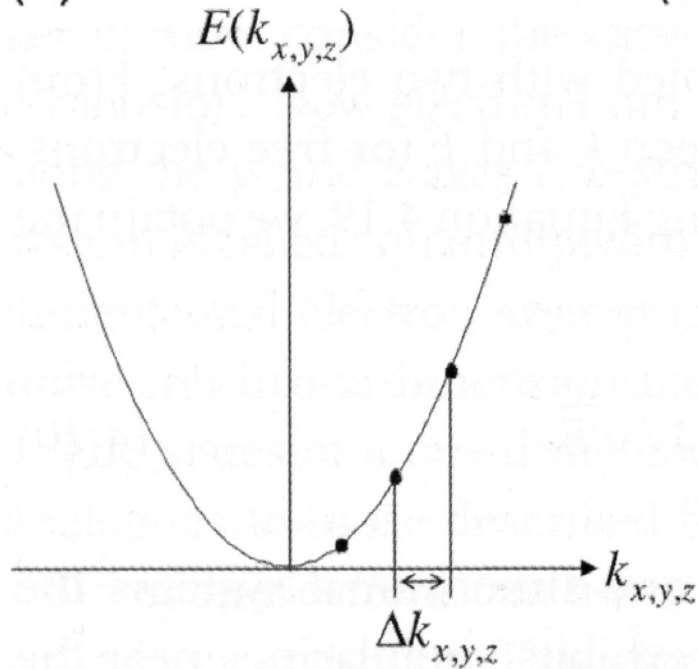
(a)



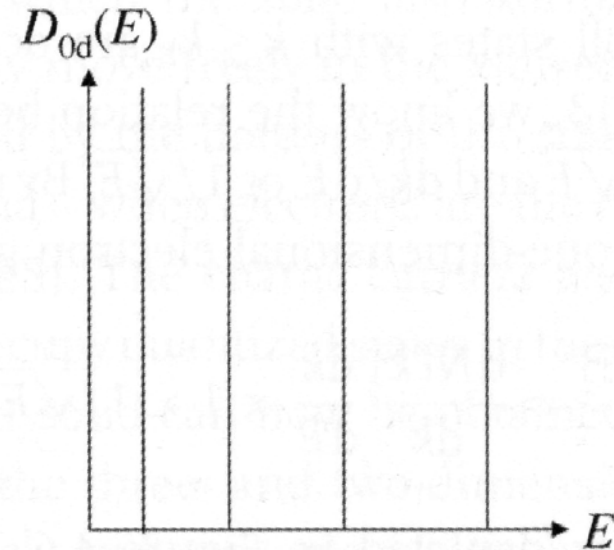
(b)



(c)

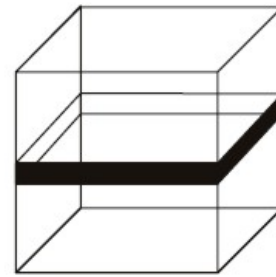
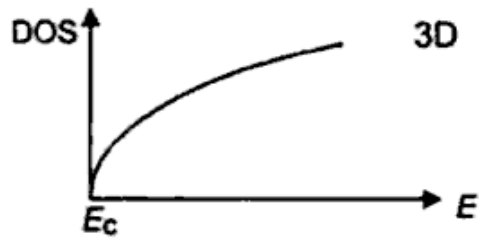
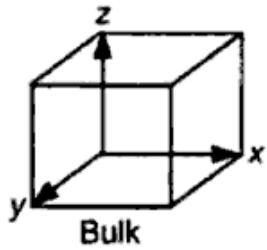


(d)

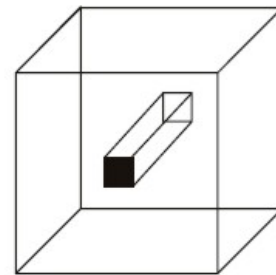
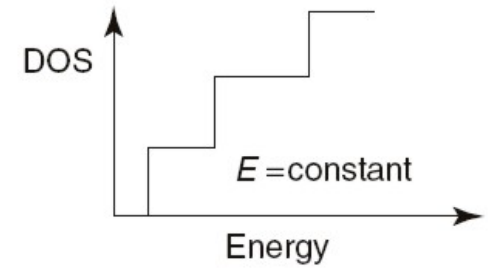


discrete level spectrum

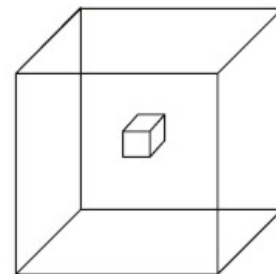
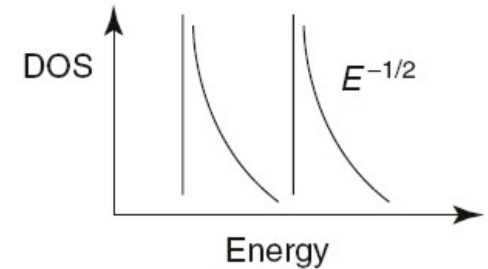
Electronic density of states - Overview



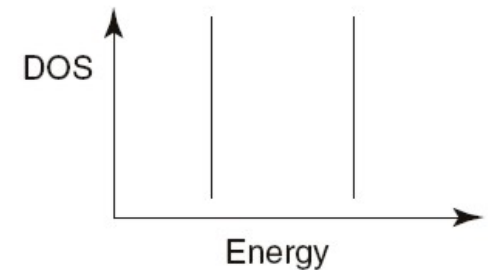
Quantum well (2D)



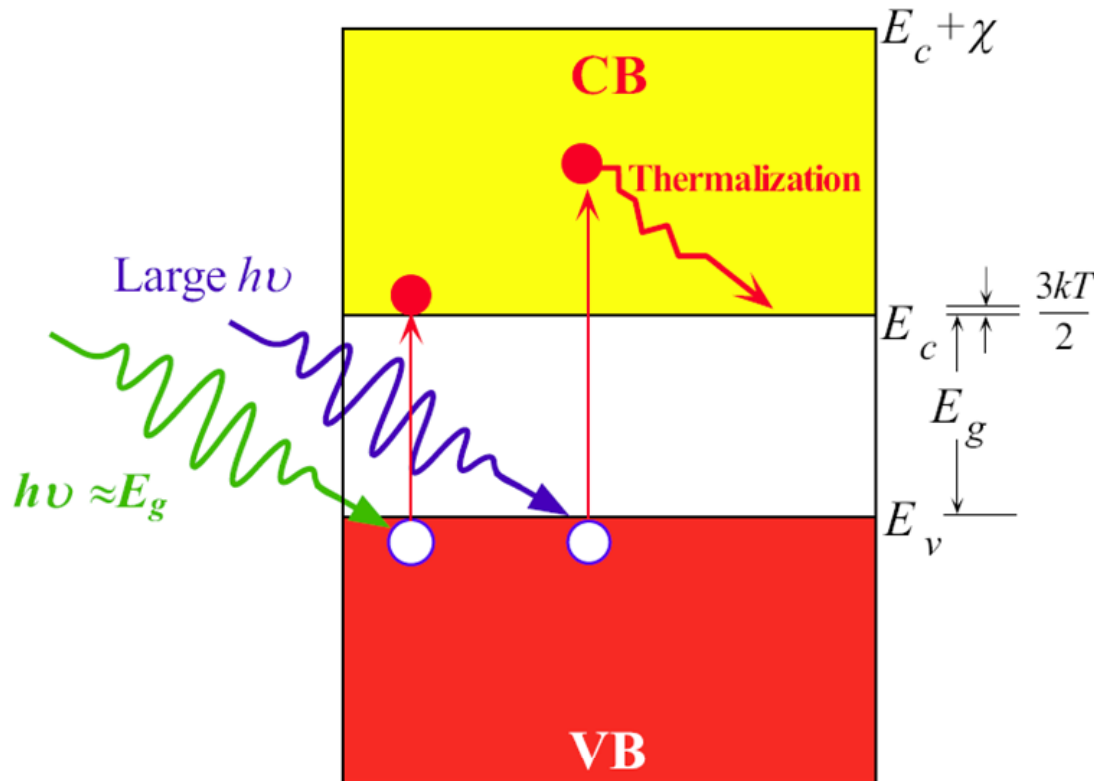
Quantum wire (1D)



Quantum dot (0D)



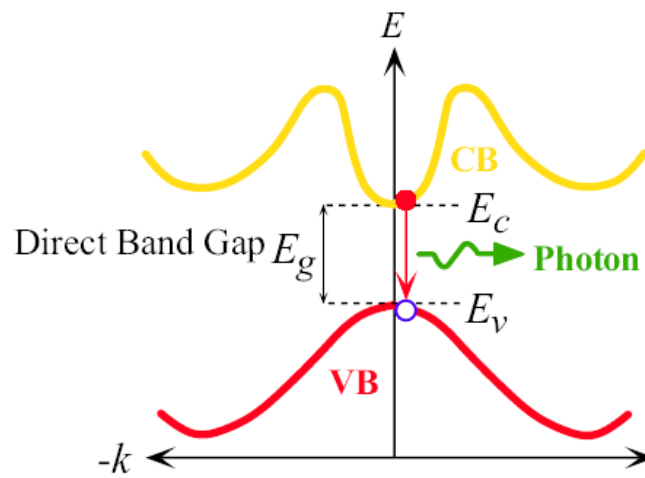
Band-to-band absorption



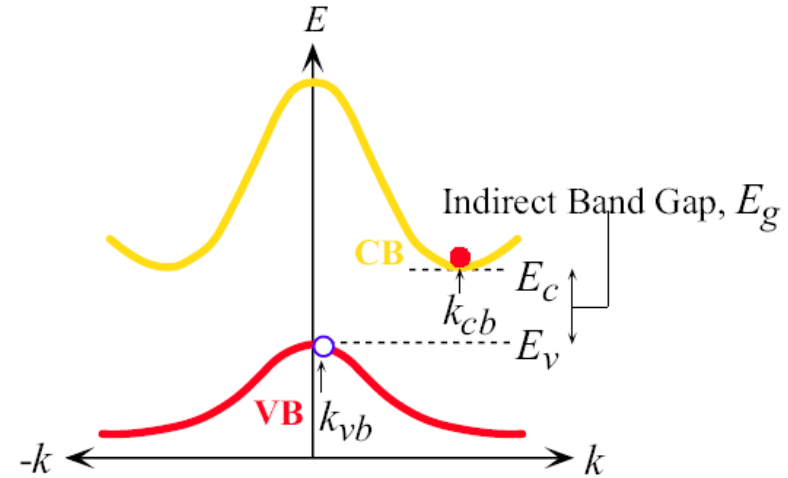
Optical absorption generates electron-hole pairs.

Energetic electrons must lose their excess energy to lattice vibrations until their average energy is $(3/2)kT$ in the CB.

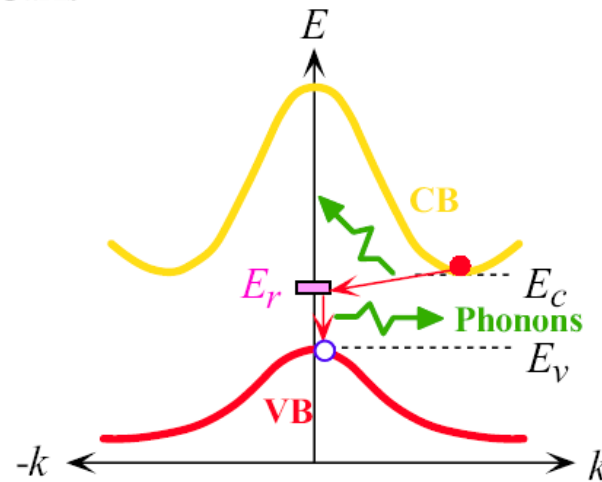
Direct and indirect band gap materials



(a) GaAs



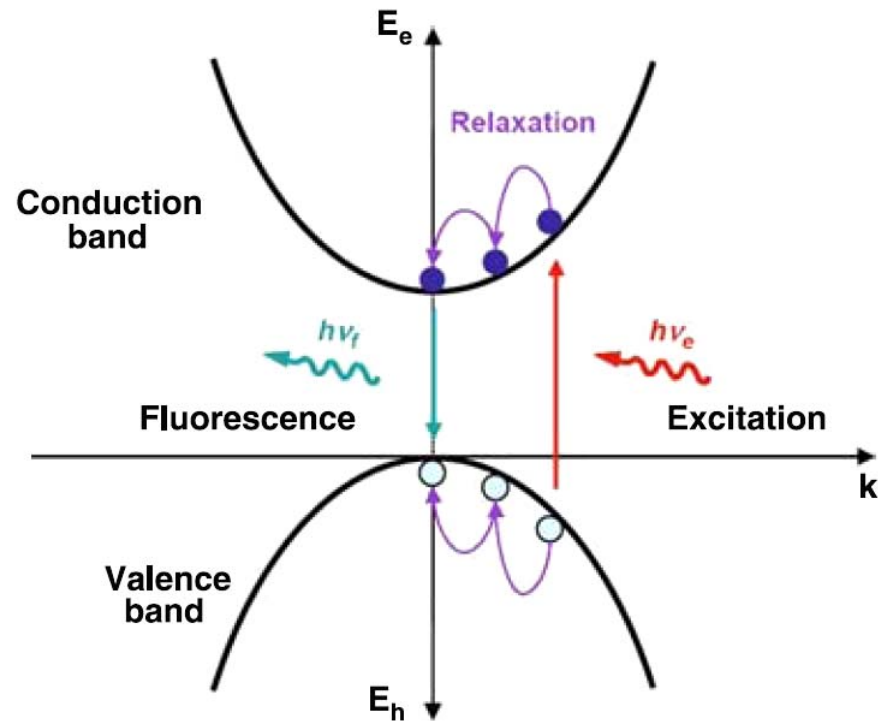
(b) Si



(c) Si with a recombination center

(a) In GaAs the minimum of the CB is directly above the maximum of the VB. GaAs is therefore a direct band gap semiconductor. (b) In Si, the minimum of the CB is displaced from the maximum of the VB and Si is an indirect band gap semiconductor. (c) Recombination of an electron and a hole in Si involves a recombination center.

Fluorescence



time dependence of excess carrier concentration: $\frac{d\Delta n}{dt} = -\frac{\Delta n}{\tau}$

τ ... carrier lifetime

recombination rate $R = -\frac{d\Delta n}{dt} = \frac{\Delta n}{\tau}$

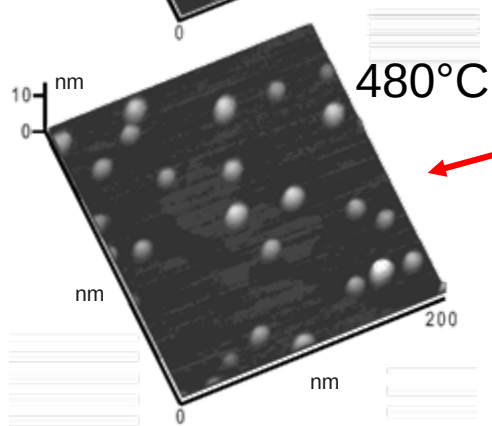
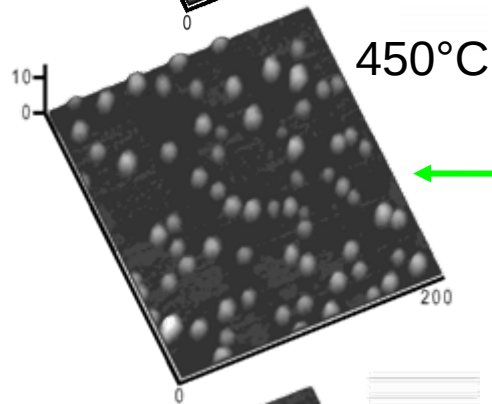
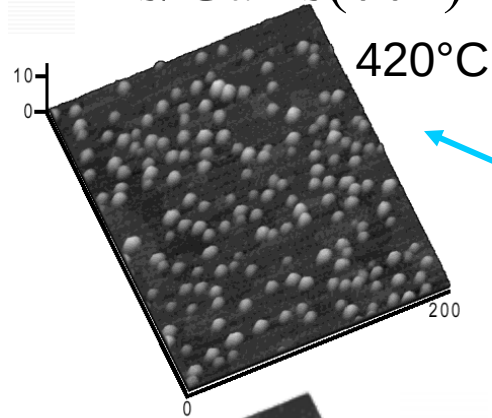
internal quantum efficiency $\eta_i = \frac{R_r}{R_r + R_{nr}}$

'r' ... radiative

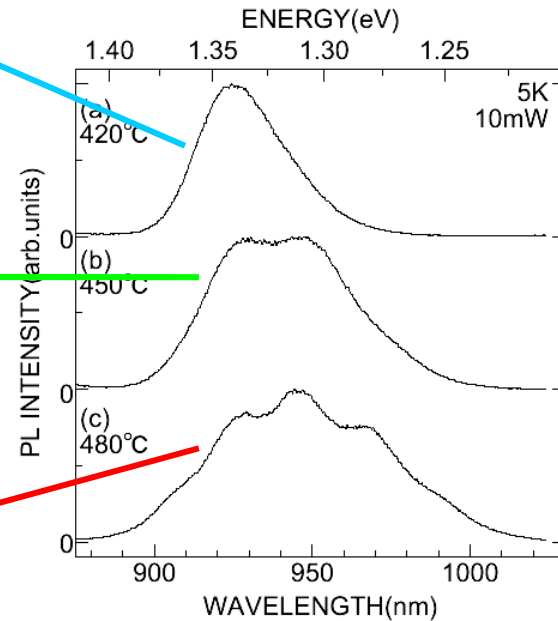
'nr' ..non-radiative

Quantum dots: Size dependence

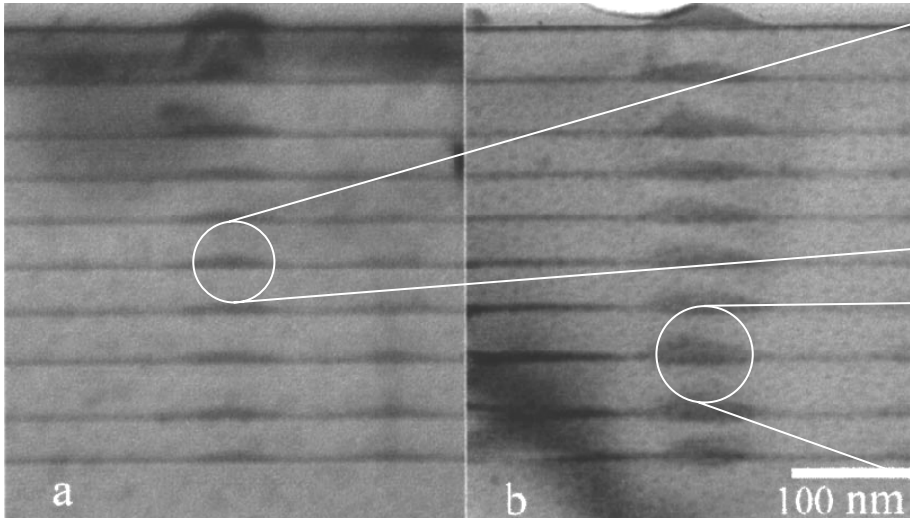
InAs/GaAs(001)



Photoluminescence spectroscopy

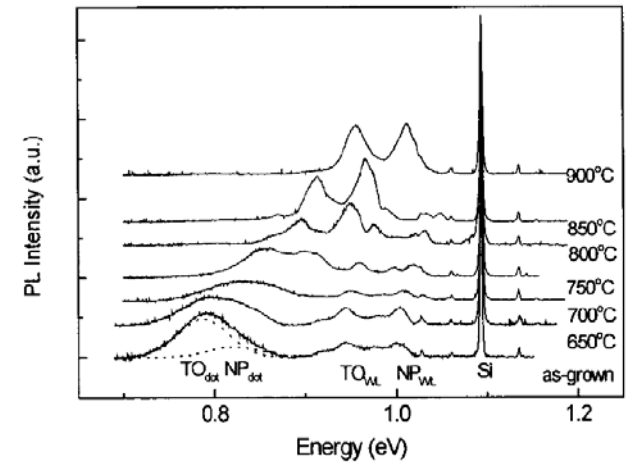
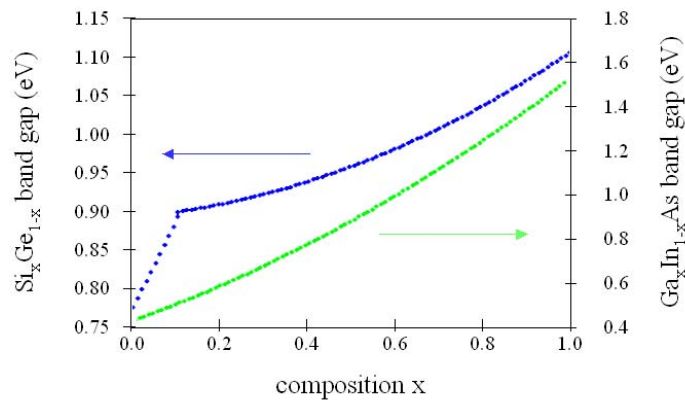
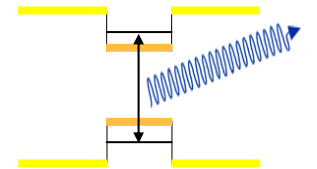
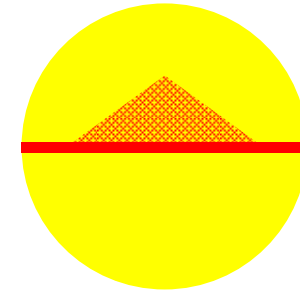
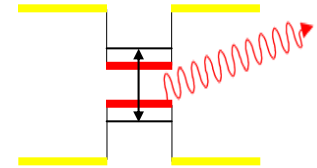
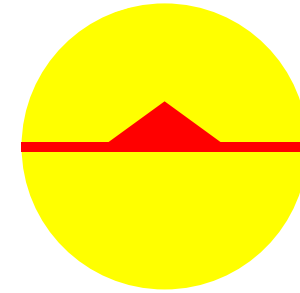


Composition dependence



as grown

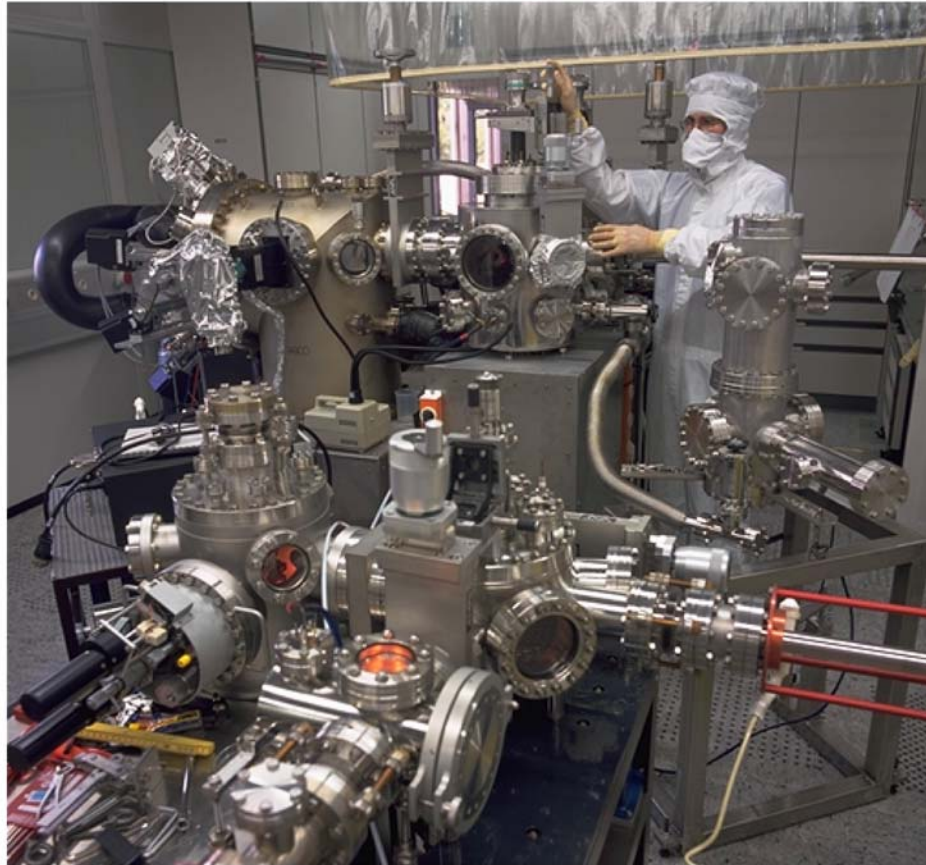
annealed @ 900°C



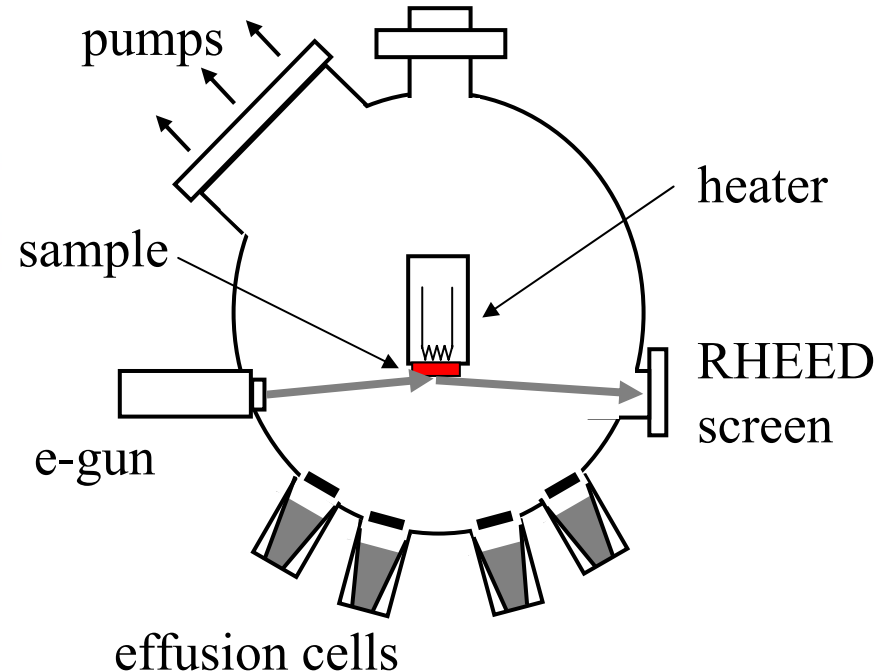
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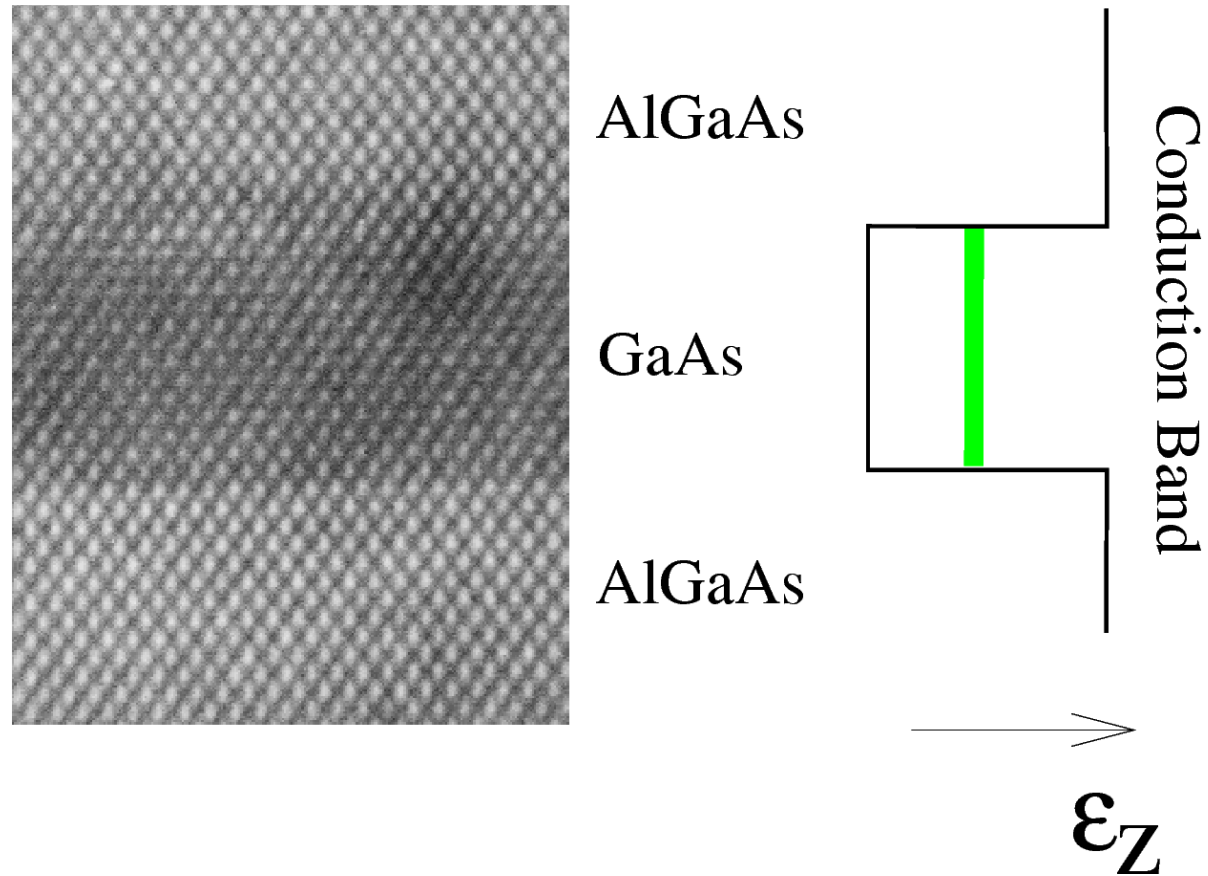
Molecular Beam Epitaxy (MBE) in UHV Chambers



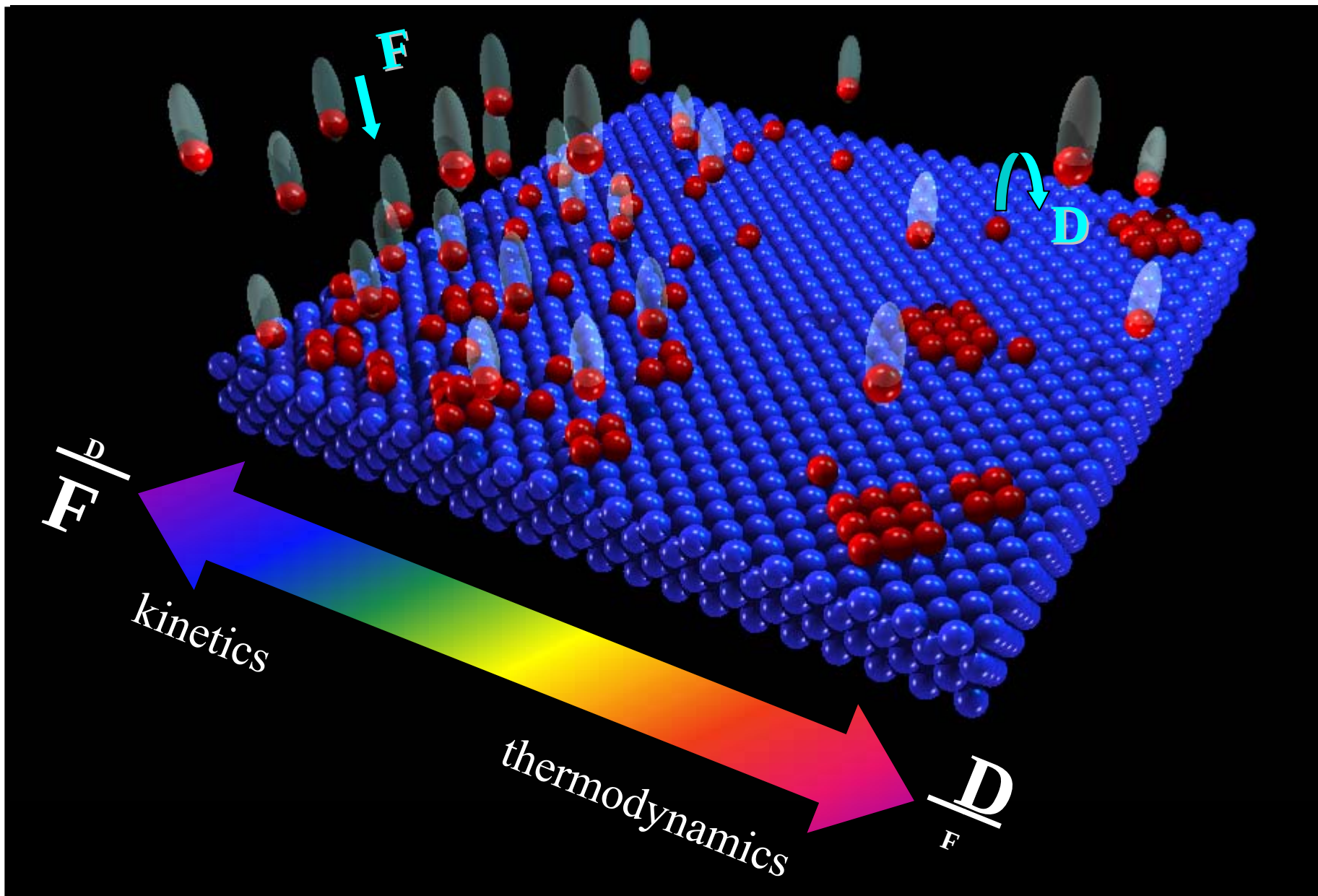
UHV: base pressure $< 10^{-10}$ mbar
growth rate: 0.1 – 1.0 ML/s



Example: 2DES in a Quantum Well



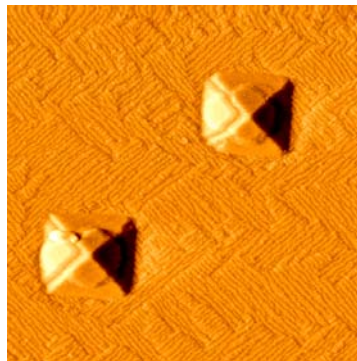
Thin Film Growth



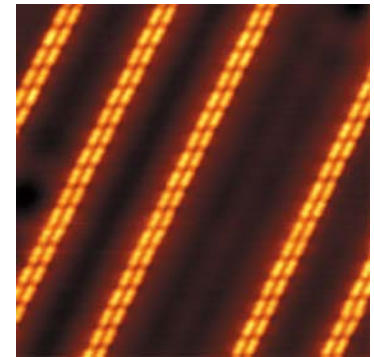
Self-Organized Growth at Surfaces



metal epitaxy

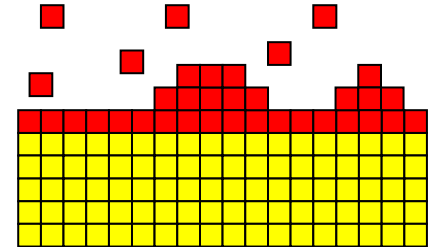
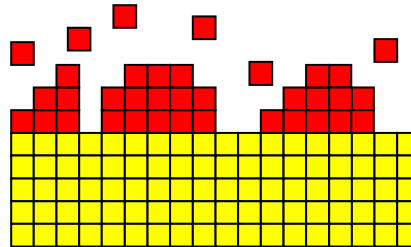
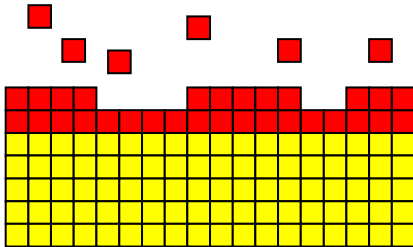
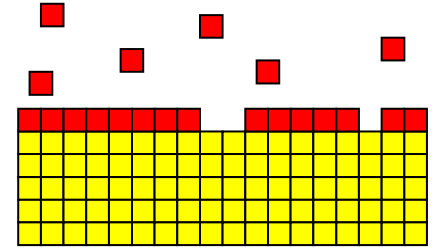
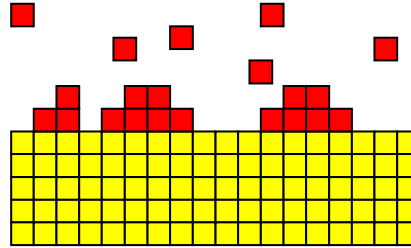
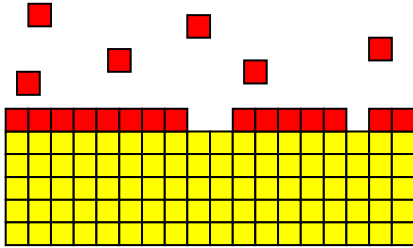


semiconductor
MBE



molecular
self-assembly

Growth modes



layer - by - layer growth
(Frank - van der Merve)

island growth
(Volmer - Weber)

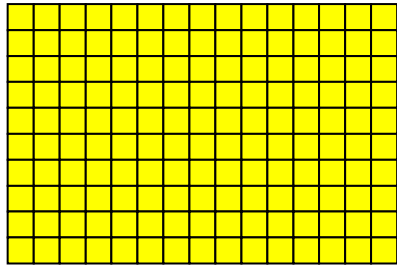
layer - by - layer
+ island growth
(Stranski - Krastanov)



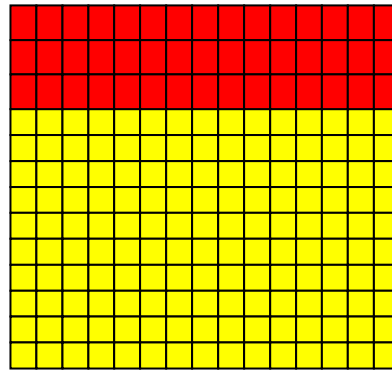
quantum dots

Stranski-Krastanov Growth of Semiconductor QDs

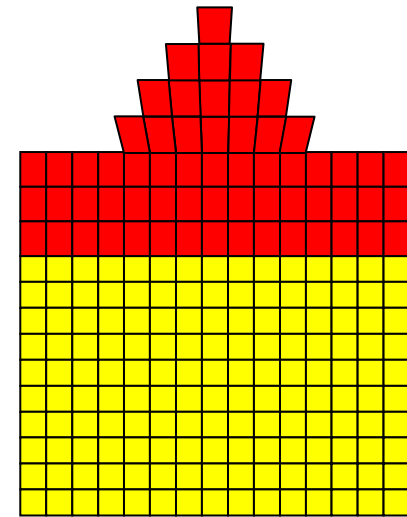
lattice constants: $a_A > a_B$



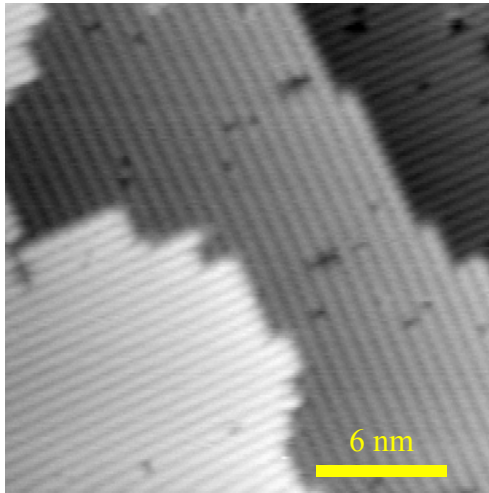
substrate



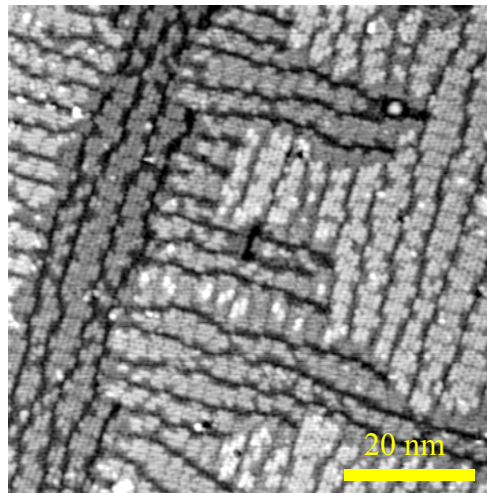
wetting layer



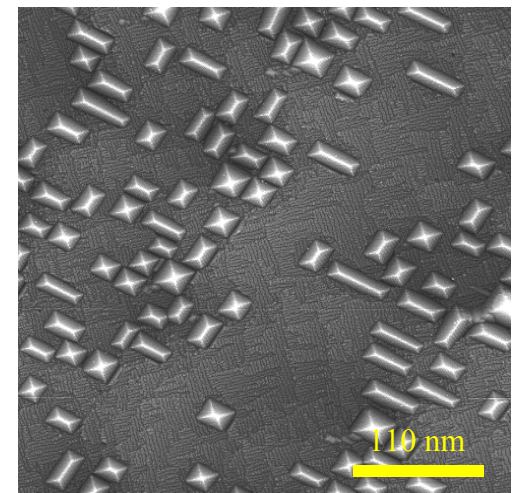
islands



Si(001)

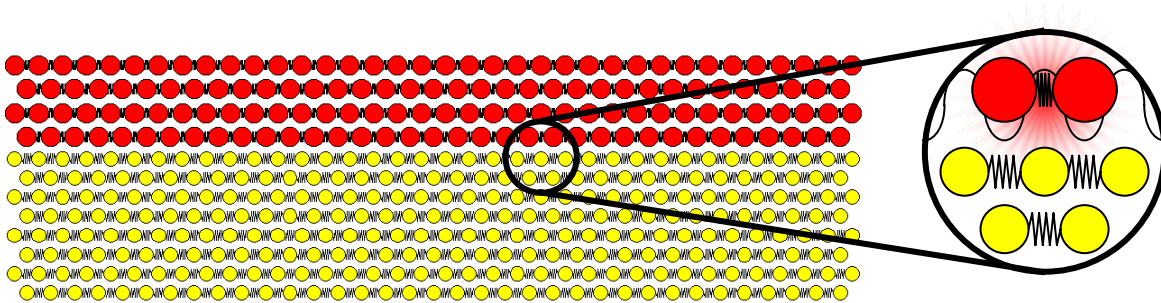


3ML Ge on Si(001)

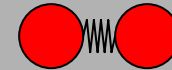


6ML Ge on Si(001)

Stranski-Krastanov Growth



Equilibrium lattice parameter:



Material **A**

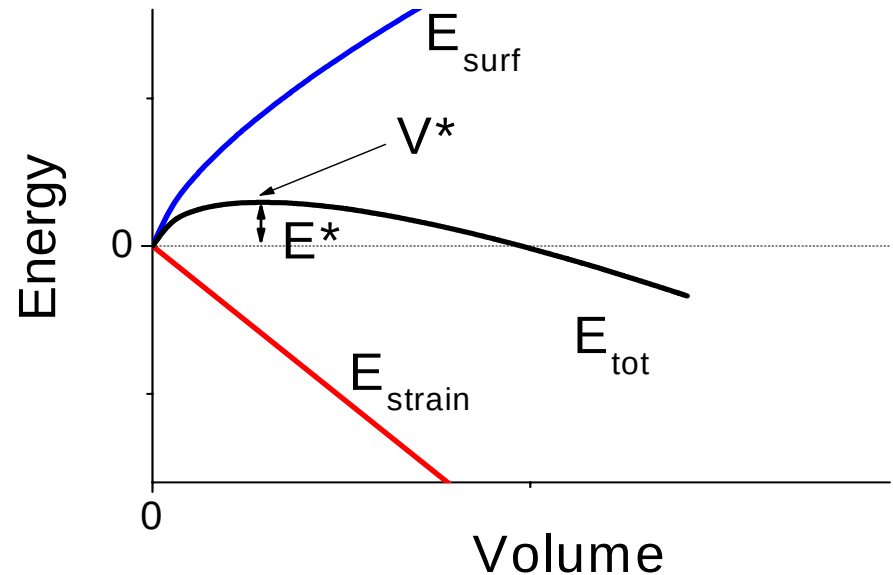


Material **B**

$$E_{\text{tot}} = E_{\text{strain}} + E_{\text{surf}}$$

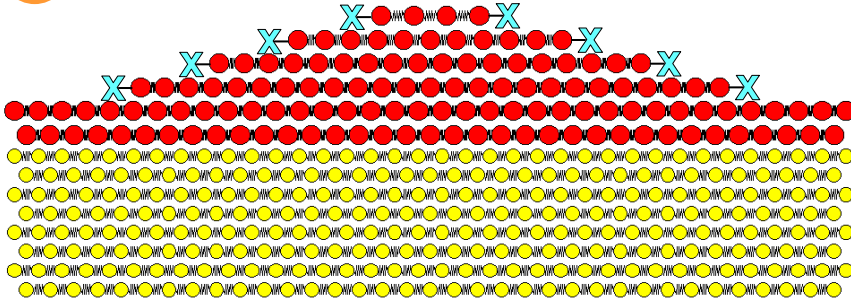
$$E_{\text{strain}} = -\alpha V$$

$$E_{\text{surf}} = +\beta V^{2/3}$$



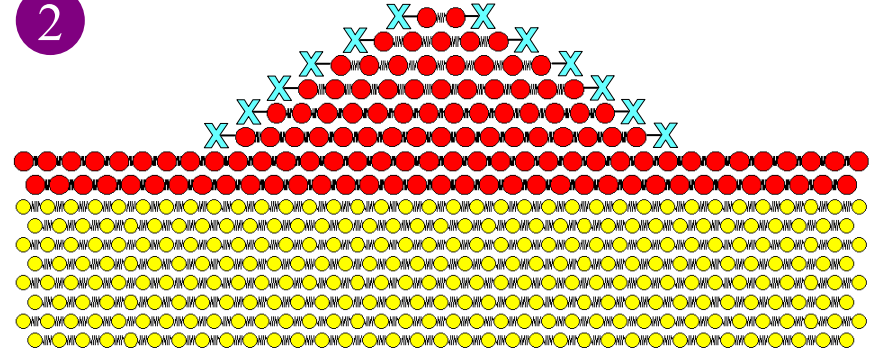
Stranski-Krastanov Growth

1



more strain energy
less surface energy

2



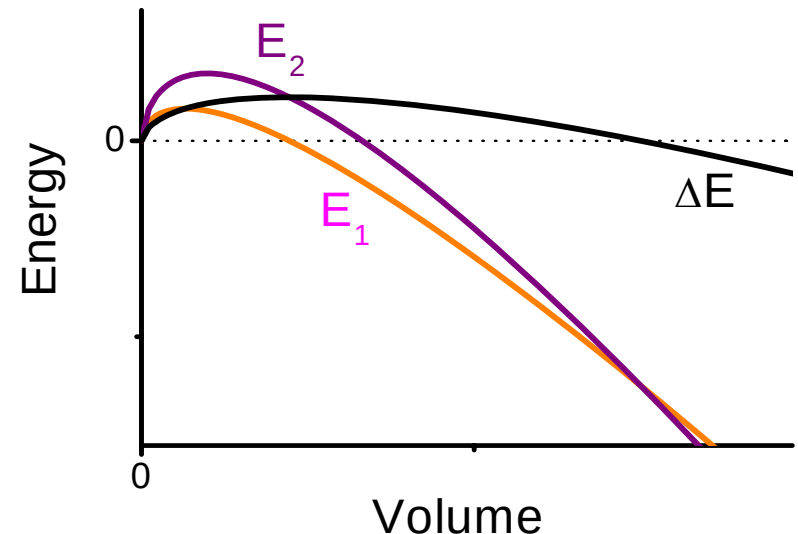
less strain energy
more surface energy

$$E_1 = -\alpha_1 V + \beta_1 V^{2/3} ; E_2 = -\alpha_2 V + \beta_2 V^{2/3}$$

$$\alpha_2 > \alpha_1$$

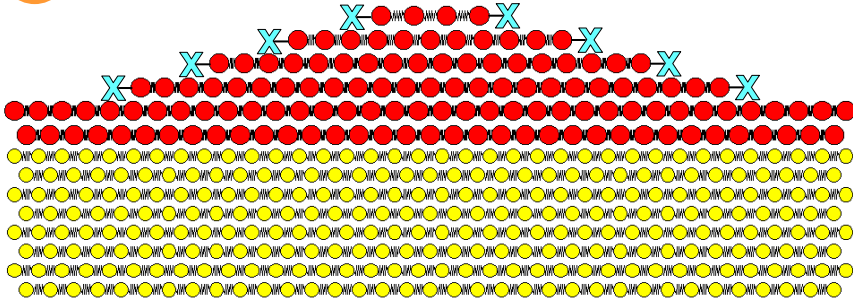
$$\beta_2 > \beta_1$$

$$E_2 - E_1 = -(\alpha_2 - \alpha_1)V + (\beta_2 - \beta_1)V^{2/3}$$



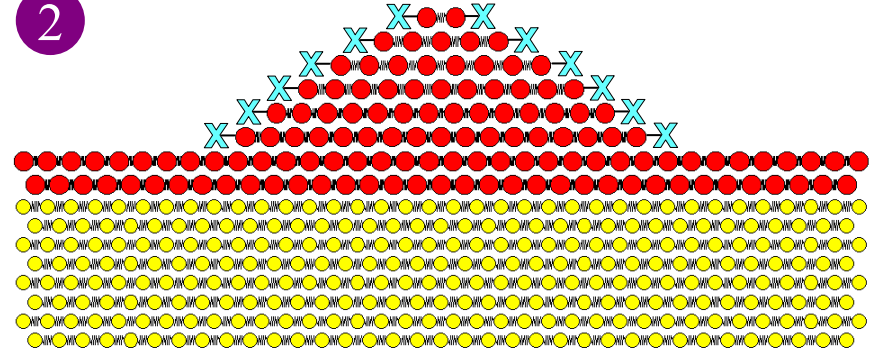
Stranski-Krastanov Growth

1

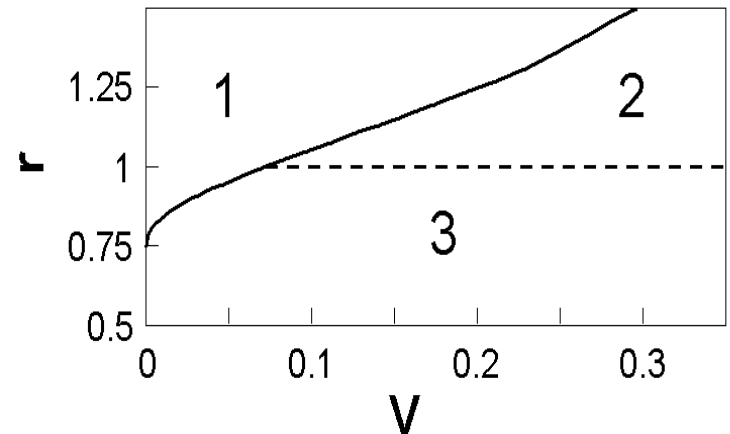
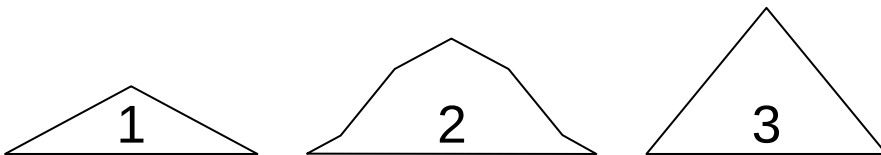


more strain energy
less surface energy

2

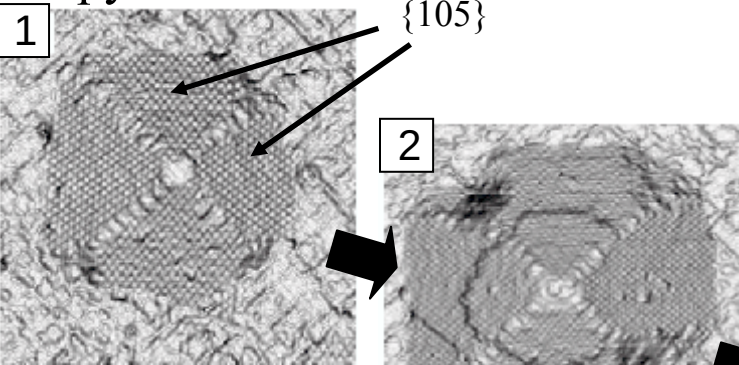


less strain energy
more surface energy



Pyramid-to-Dome transformation : Ge/Si(001)

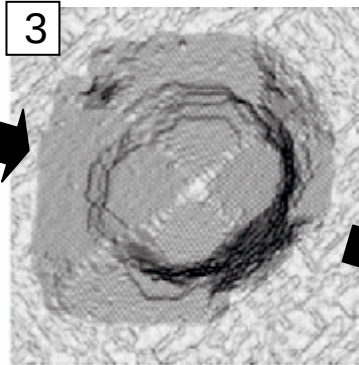
pyramids ...



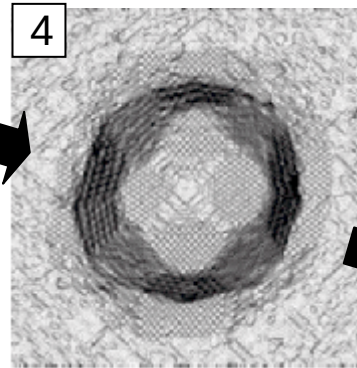
{105}

2

... transition domes ...

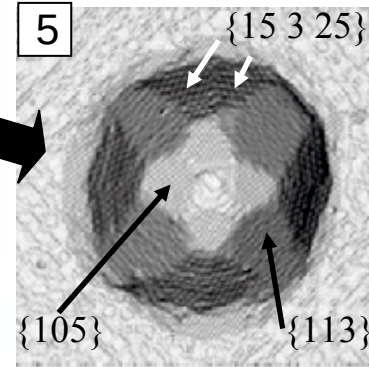


3



4

... domes

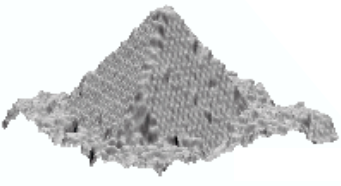


5

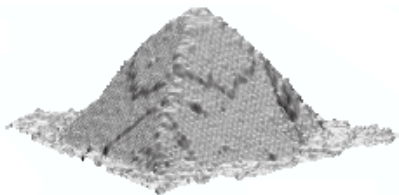
{15 3 25}

{105}

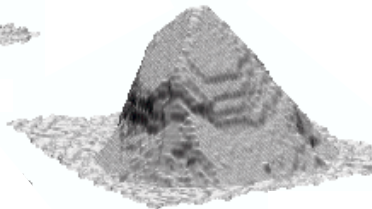
{113}



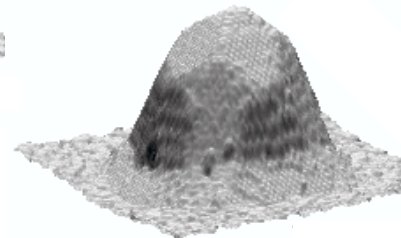
45 x 45 x 3.6 nm³



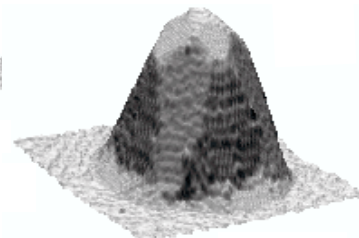
55 x 55 x 5.3 nm³



75 x 75 x 7.3 nm³

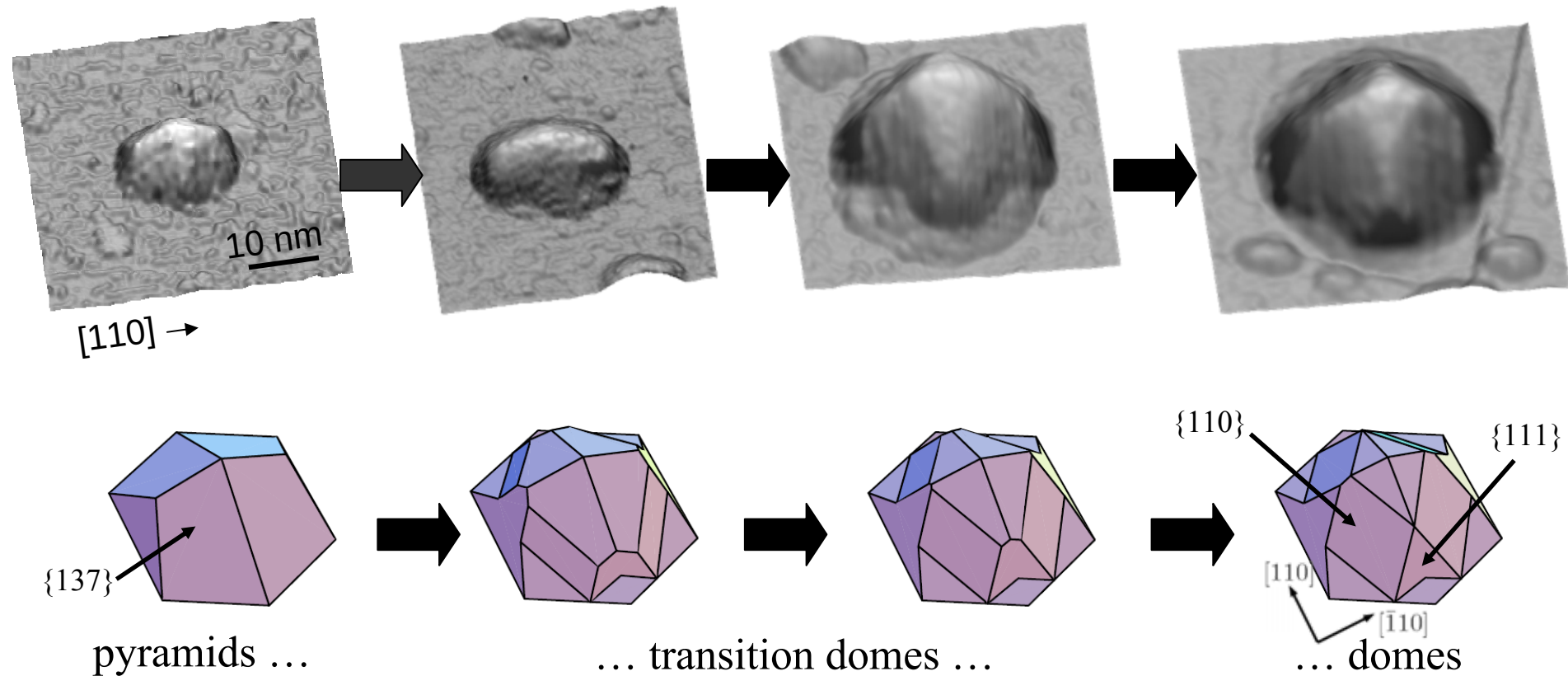


75 x 75 x 7.8 nm³



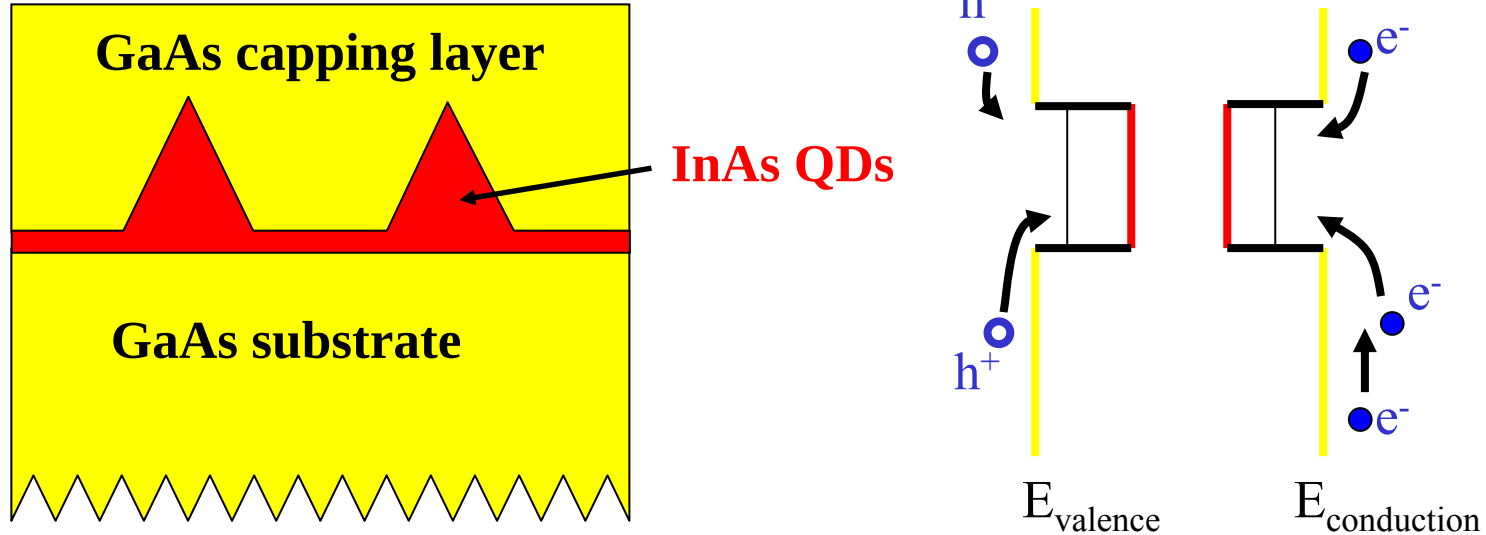
70 x 70 x 11.4 nm³

Pyramid-to-Dome transition : InAs/GaAs(001)



successive evolution of $\{110\}$ and $\{111\}$ facets at the expense of $\{137\}$ facets
→ transformation pyramid to dome

Overgrowth: GaAs/InAs/GaAs(001)



overgrowth of QDs:

- protection of the surface: passivation of surface states
- bandgap discontinuity acts as a trap for the charge carriers
- capping layer effects the composition and morphology of the islands

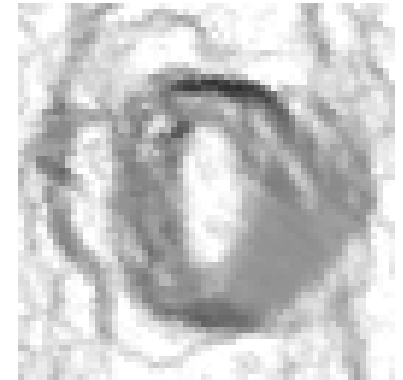
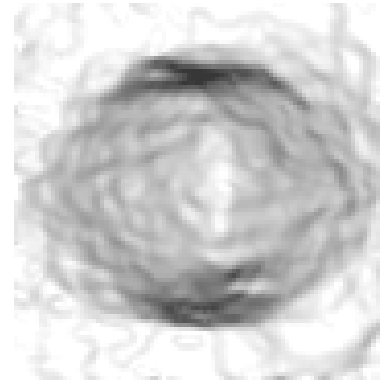
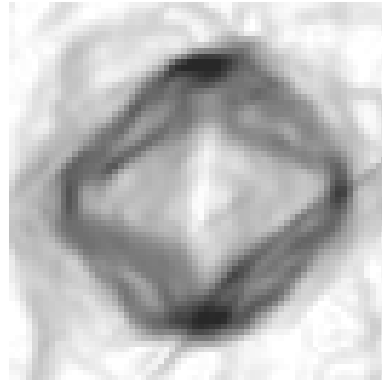
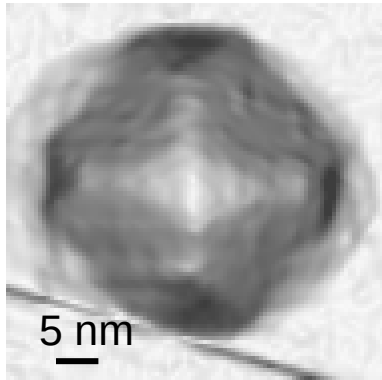
High resolution analysis of the overgrowth

0 ML

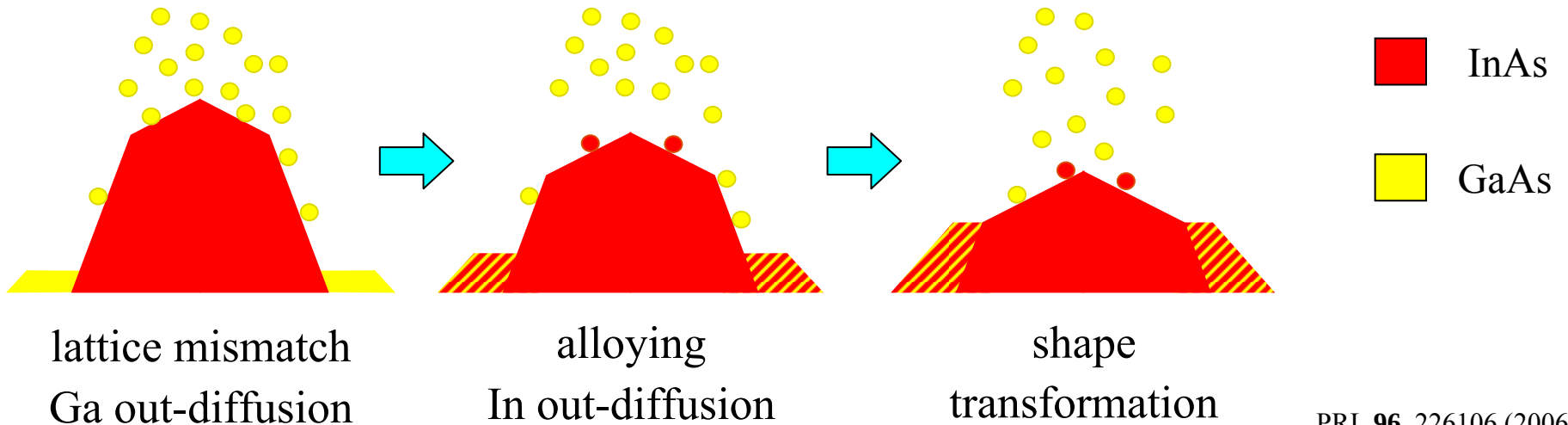
1 ML

2 ML

3 ML



backward dome-to-pyramid transition



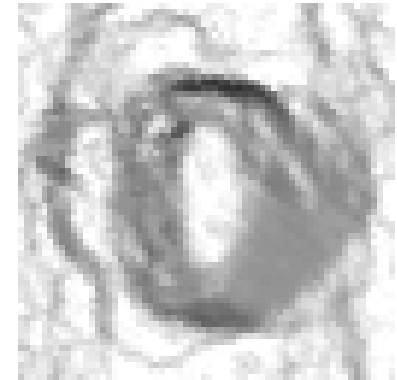
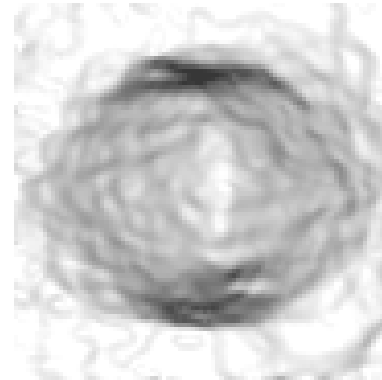
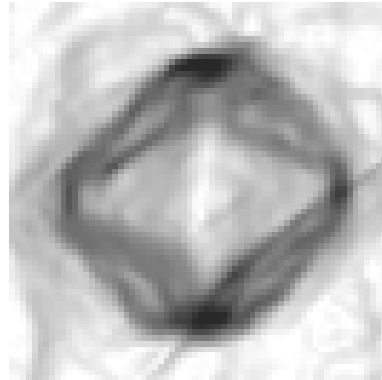
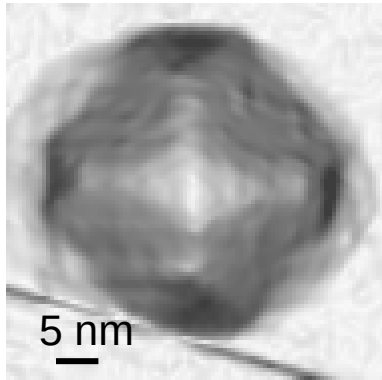
High resolution analysis of the overgrowth

0 ML

1 ML

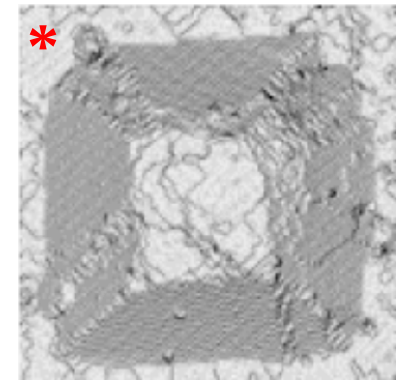
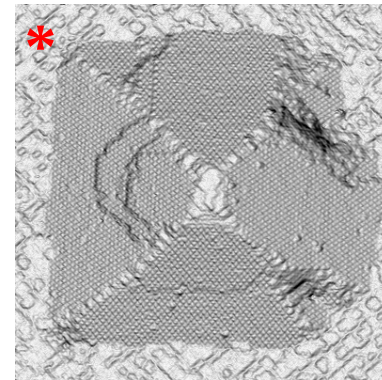
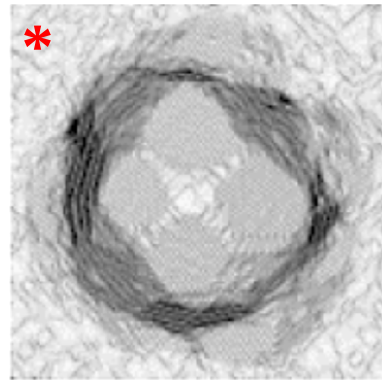
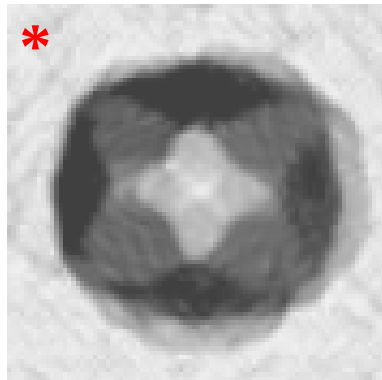
2 ML

3 ML



InAs / GaAs(001)

backward dome-to-pyramid transition



Ge / Si(001)

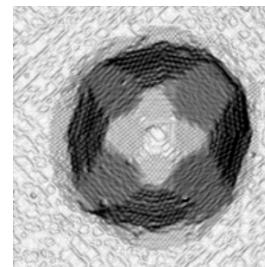
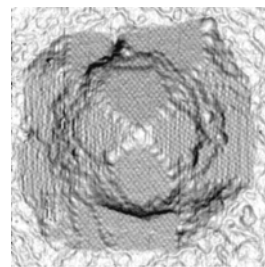
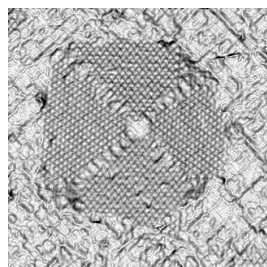
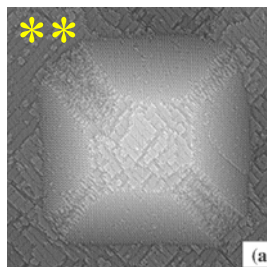
0 ML

1 ML

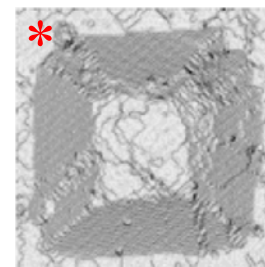
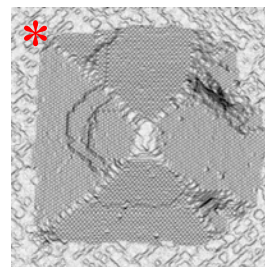
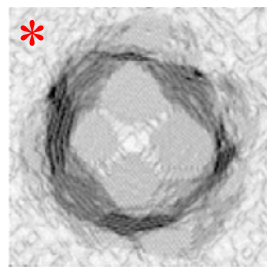
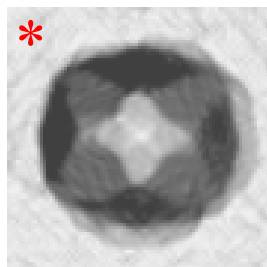
2 ML

3 ML

Ge / Si(001)

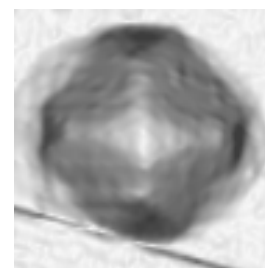
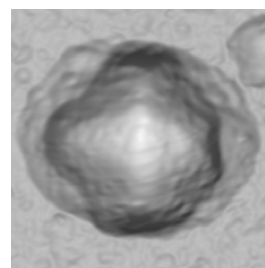
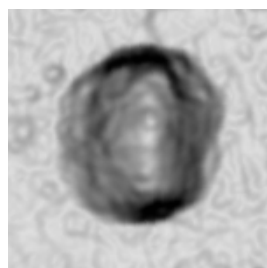
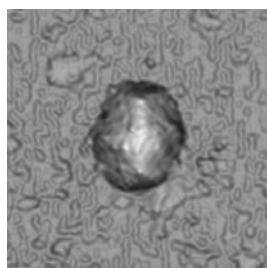


growth

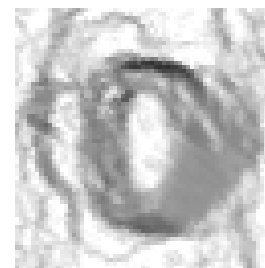
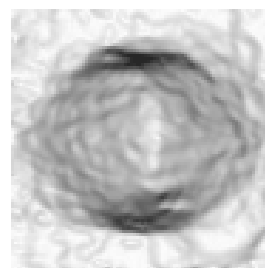
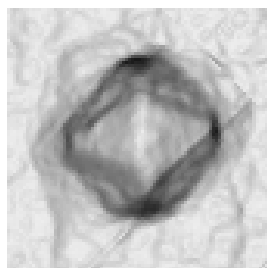
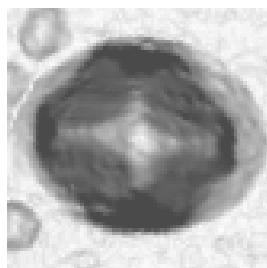


overgrowth

InAs / GaAs(001)

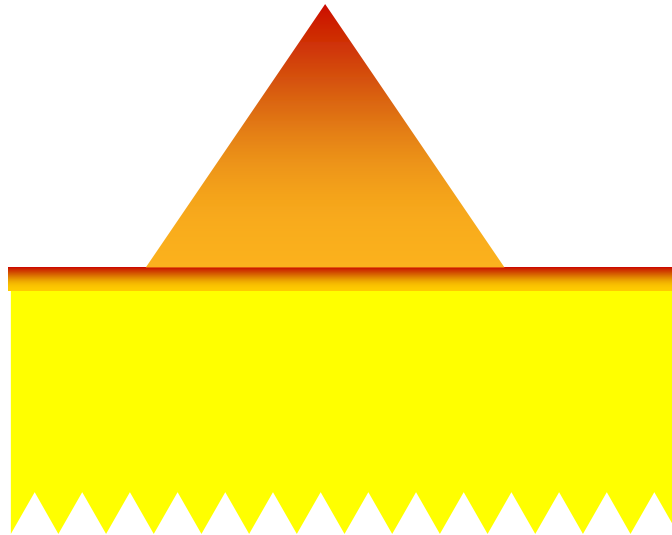


growth



overgrowth

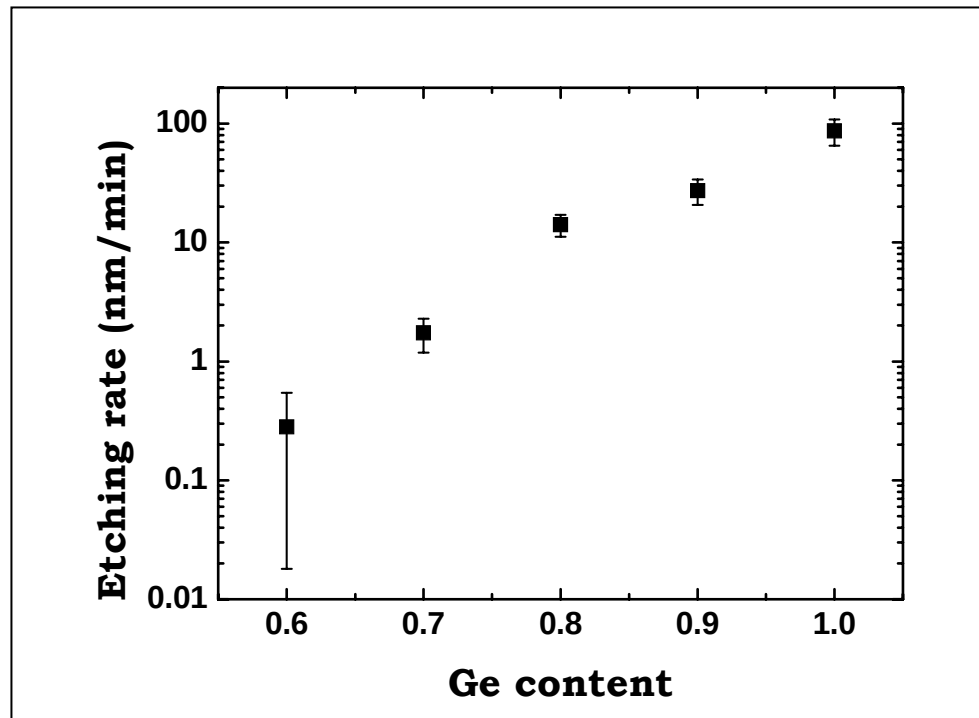
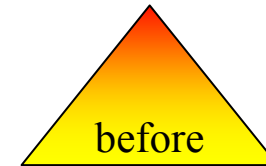
Quantum dot composition



Determining intermixing by AFM

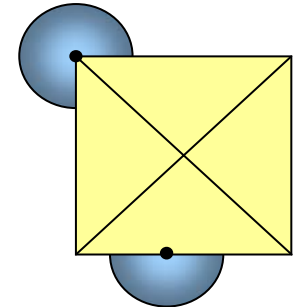
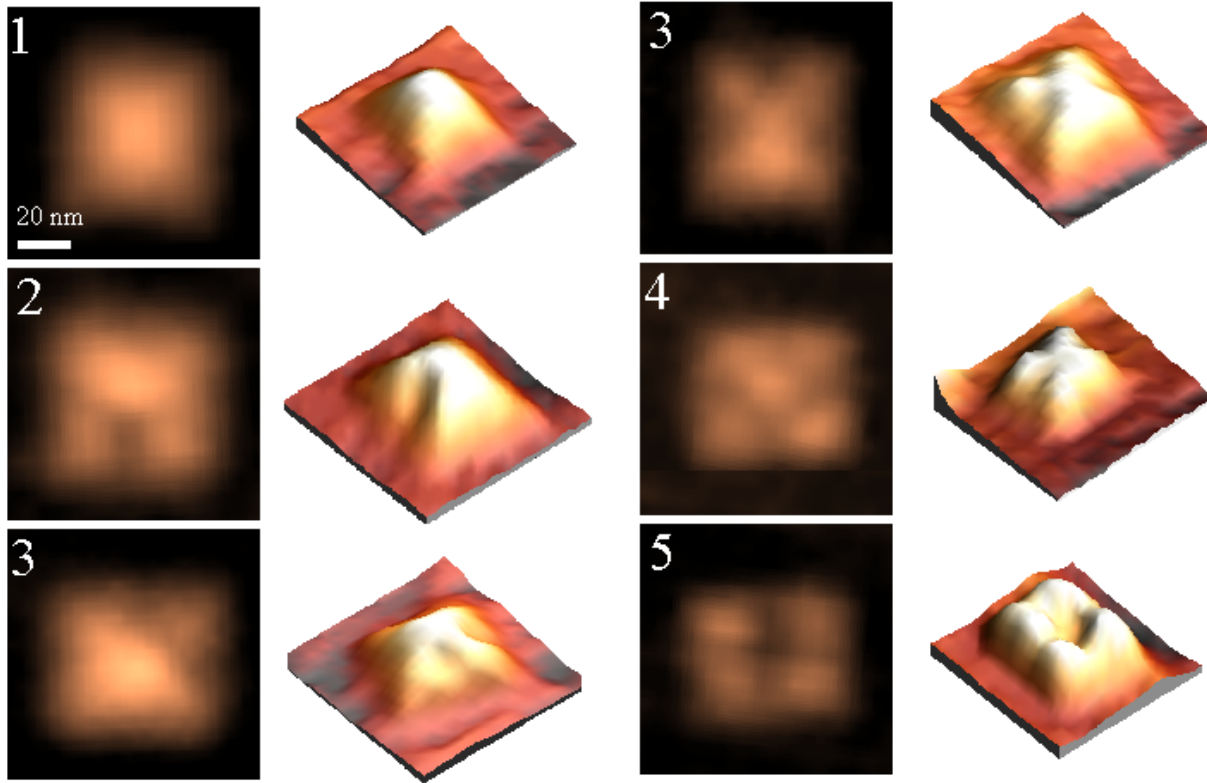
Indirect method: Selective Chemical Etching

E.g.: etching $A_{1-x}B_x$
for $x \leq 20\%$

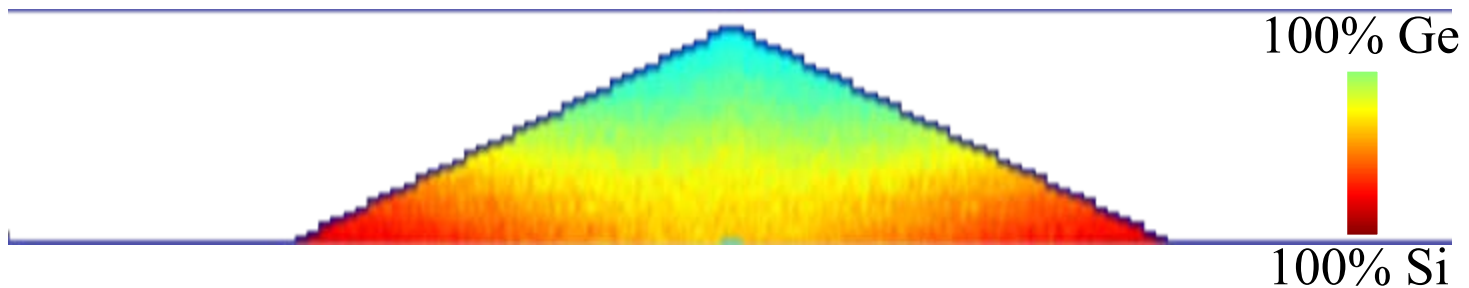


U. Denker et al., PRL **90**, 196102 (2003)

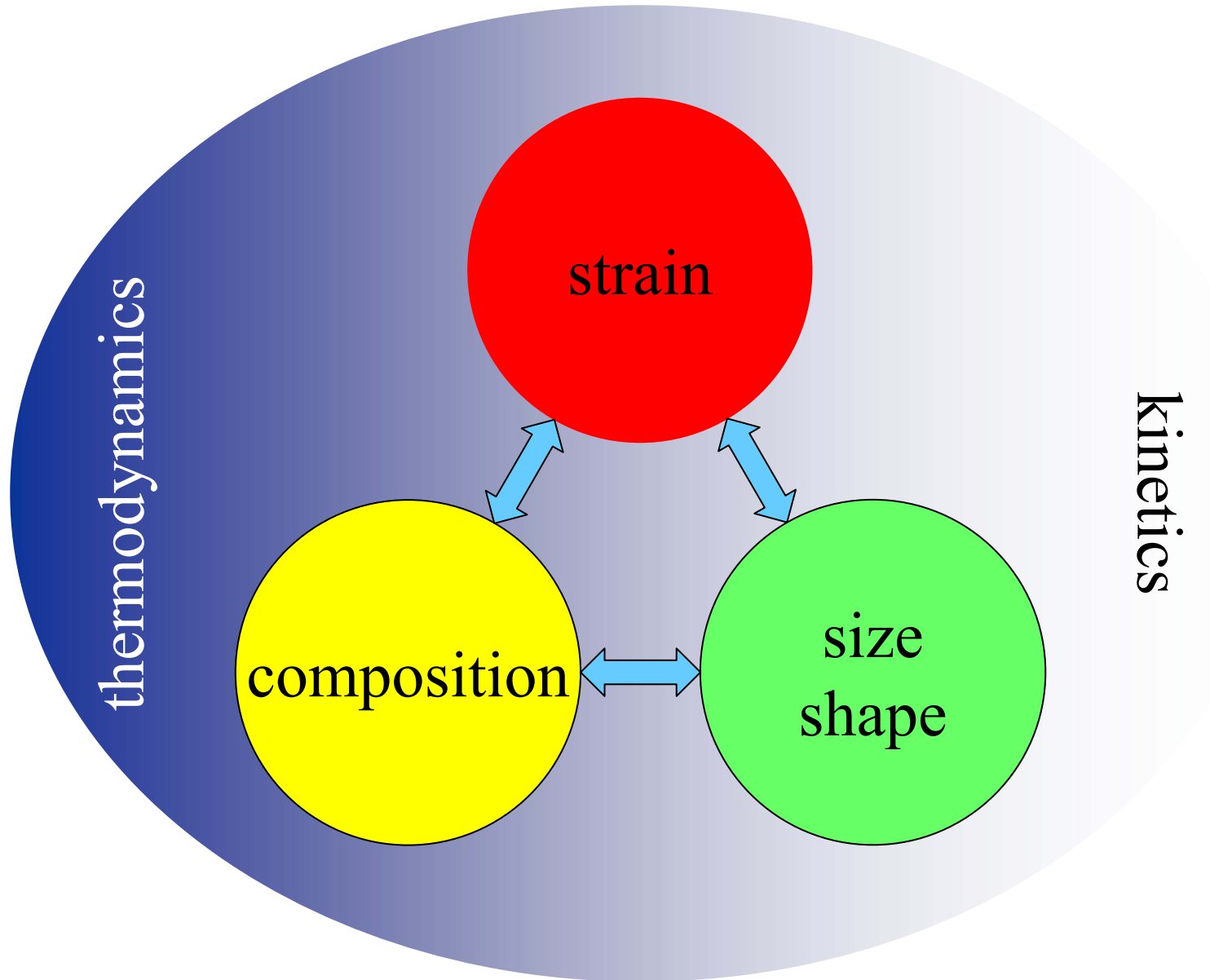
Composition profile of Ge/Si(001) pyramids



Si enrichment at the corners of the pyramids



Self – organized semiconductor quantum dots

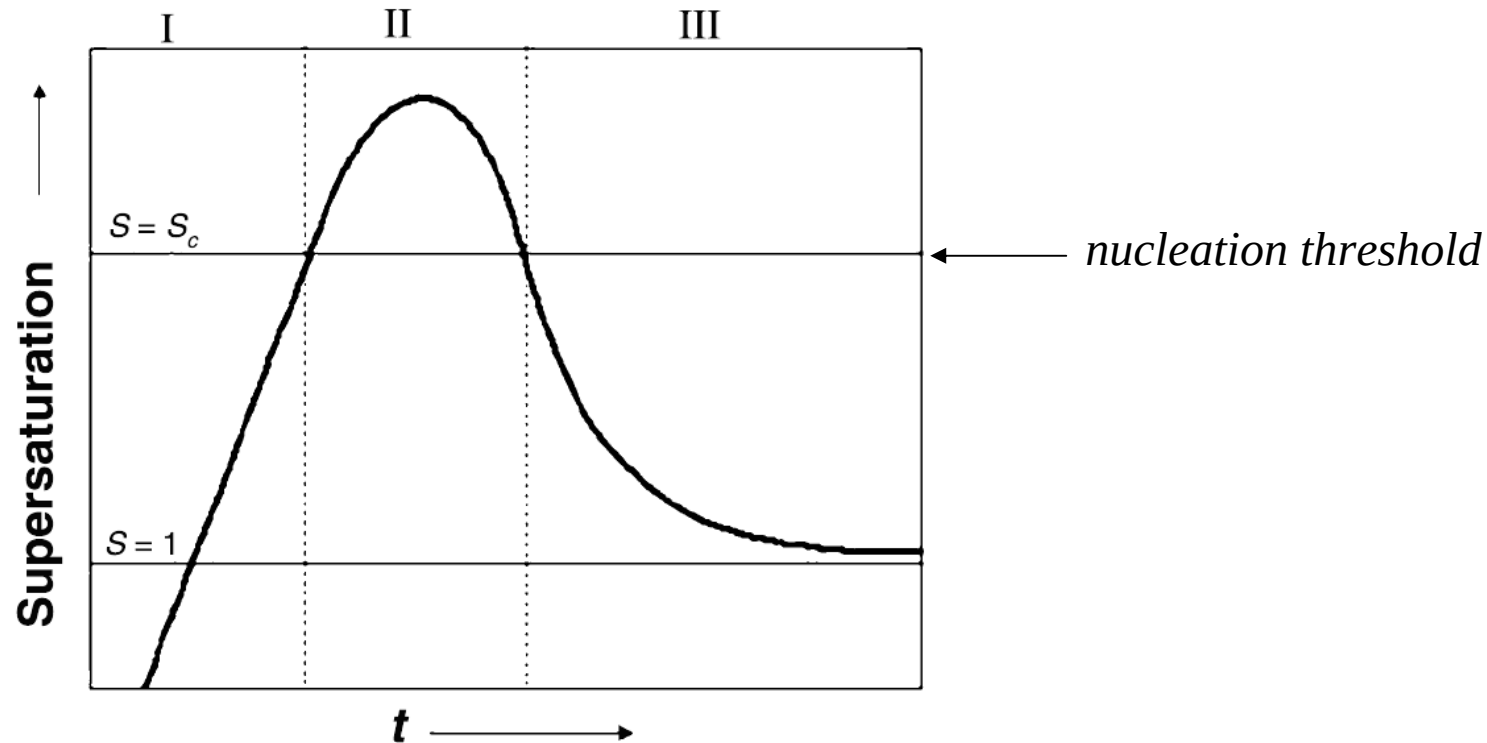


Semiconductor Nanostructures

- basics
- MBE quantum dots
- nanocrystals
- nanowires

Solution-based nanocrystal synthesis

Degree of supersaturation vs. reaction time (LaMer plot):

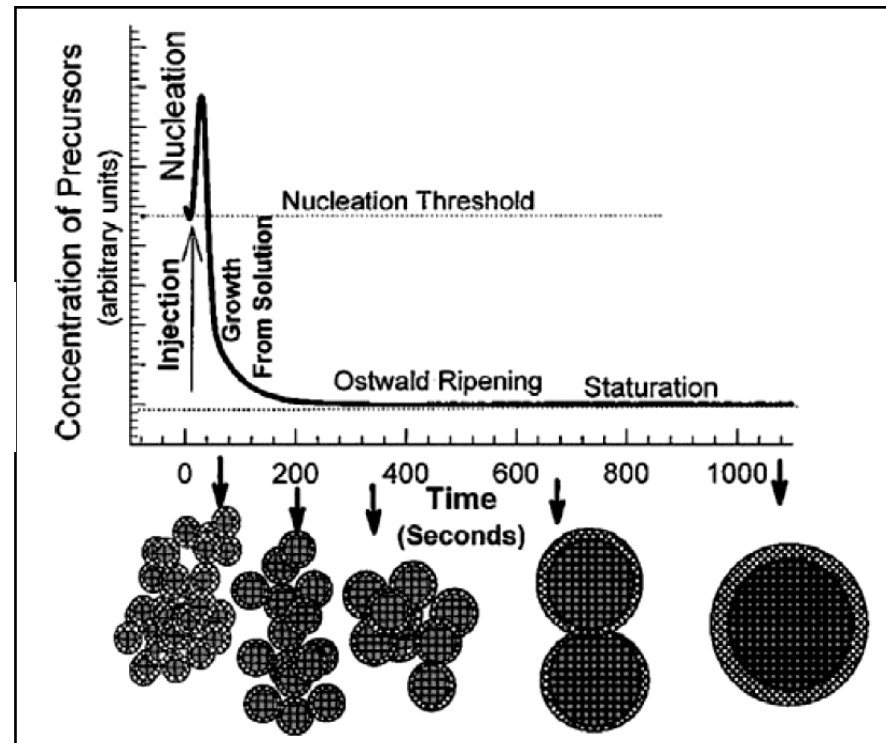
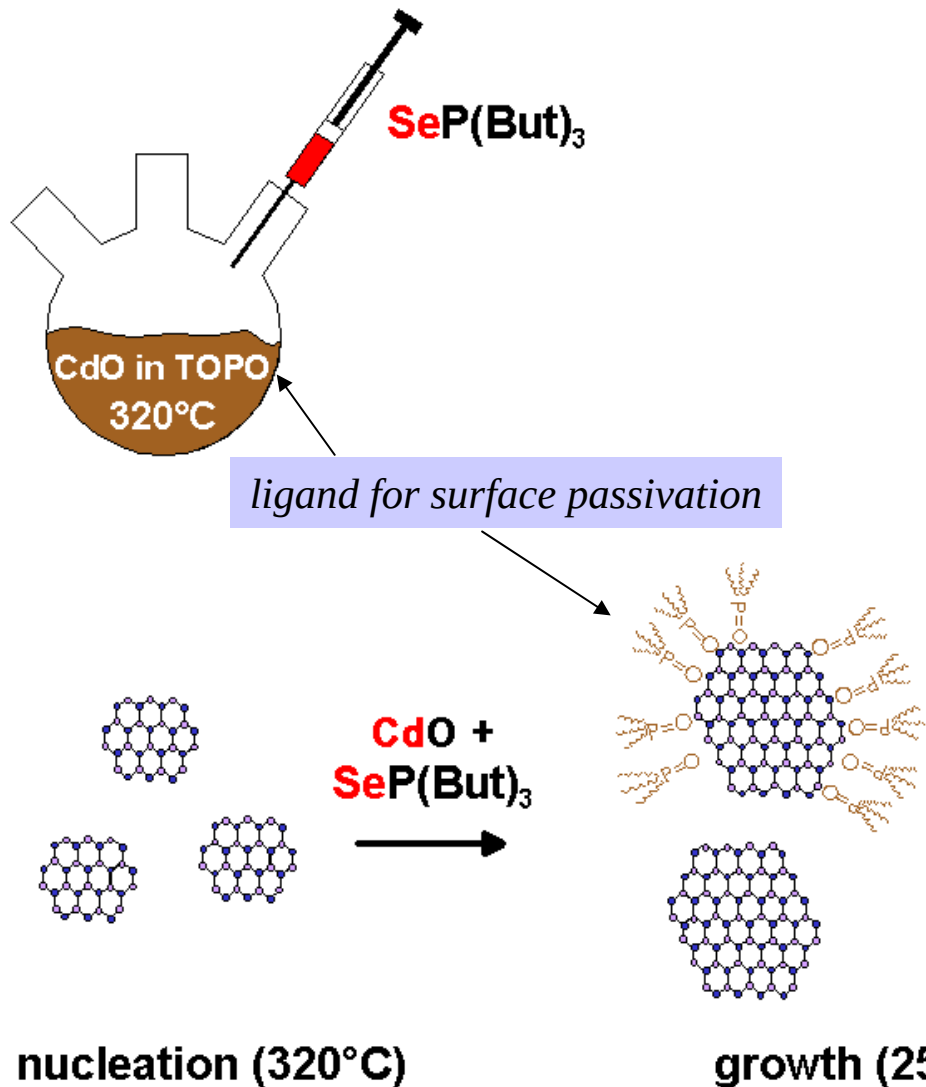


→ homogeneous nucleation requires temporal separation of nucleation and growth of the seeds.

hot injection method
(instantaneous nucleation)

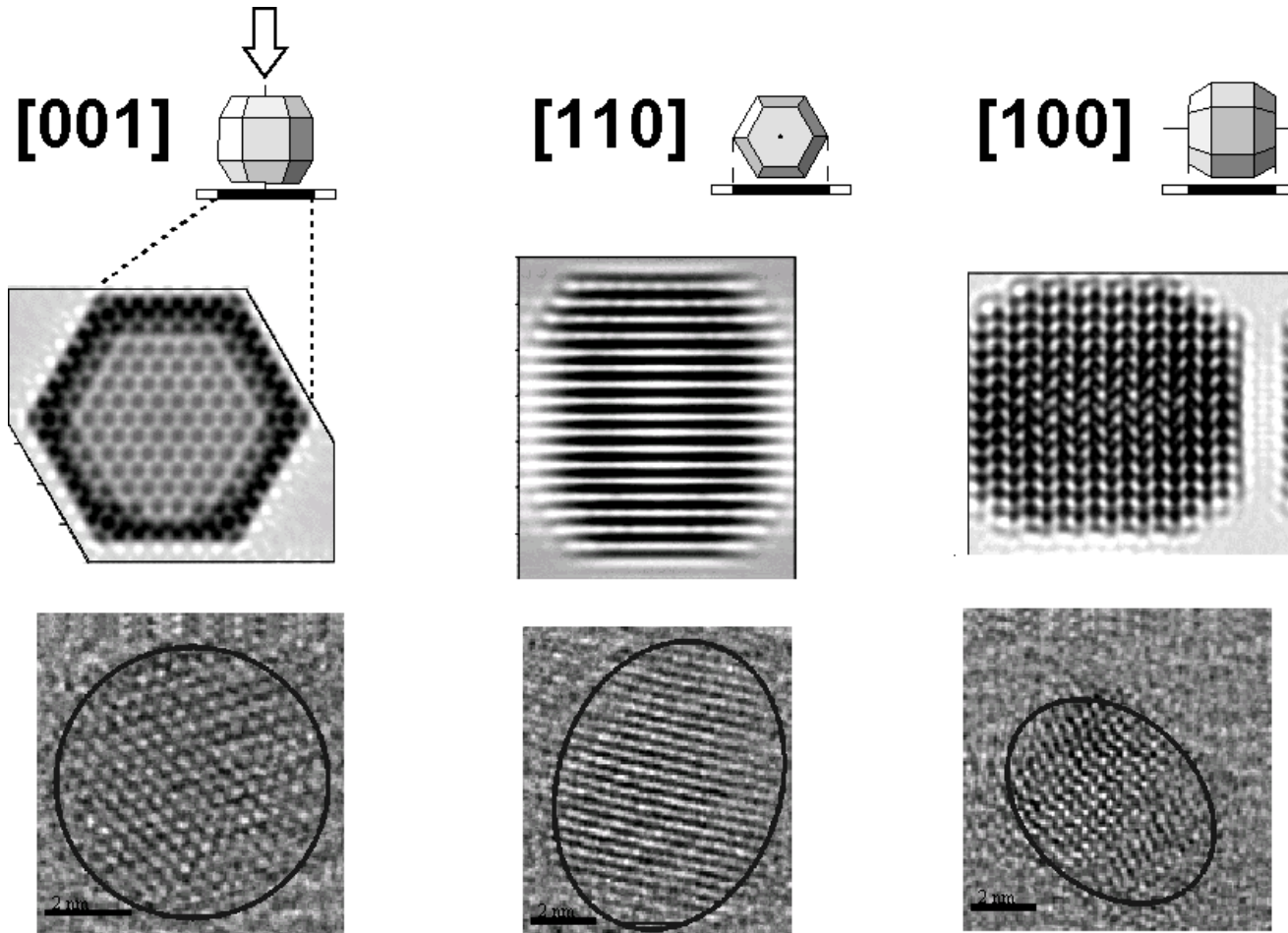
heating-up method
(in situ formation of reactive species)

CdSe nanocrystal synthesis

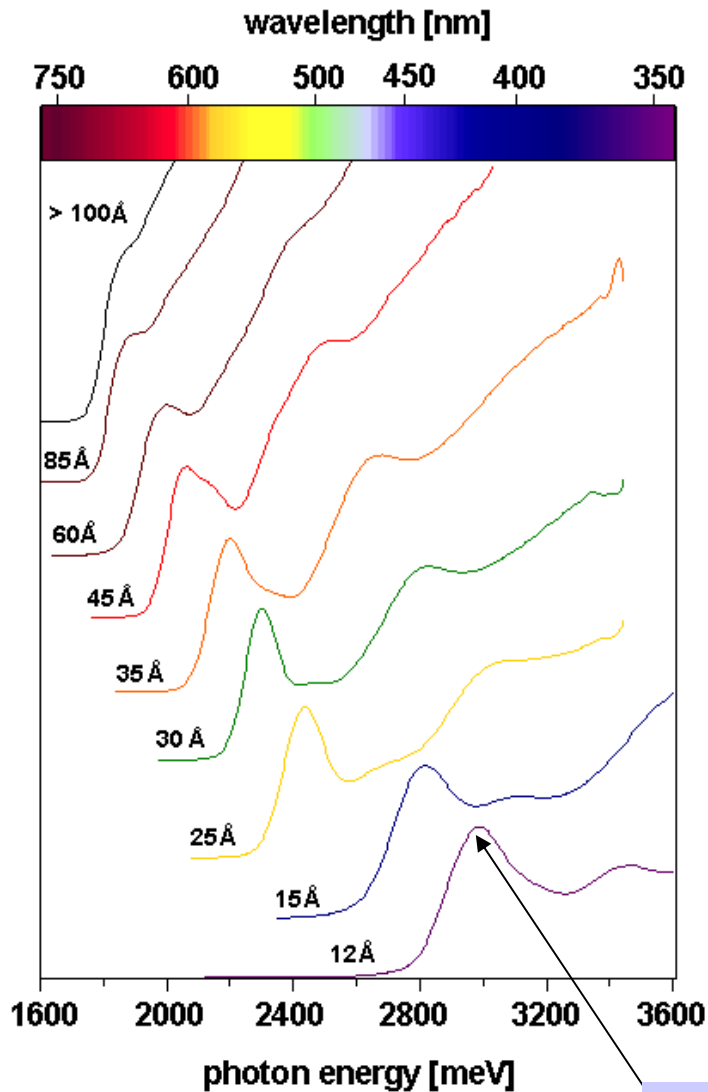


Microscopic structure

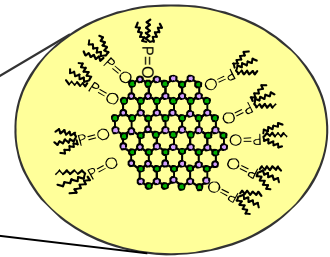
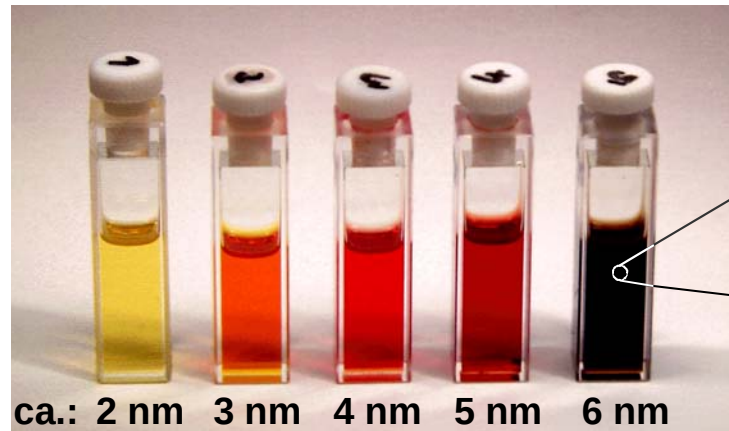
HRTEM images of hexagonal CdSe nanocrystals:



Size-dependence of optical absorption



CdSe nanocrystals

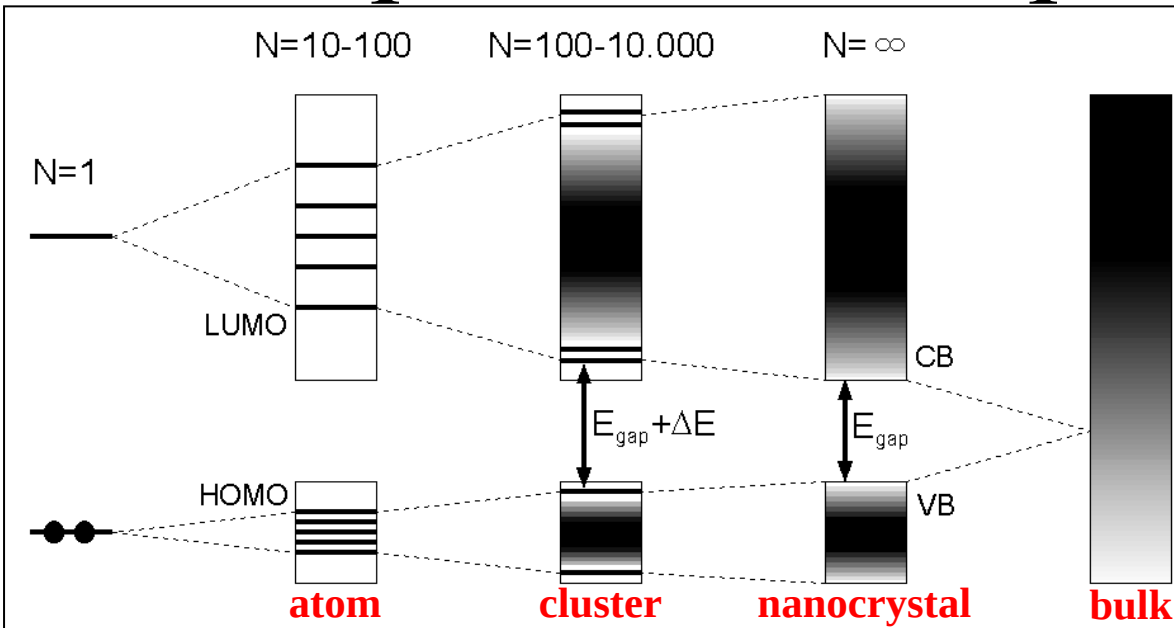


1-10 nm

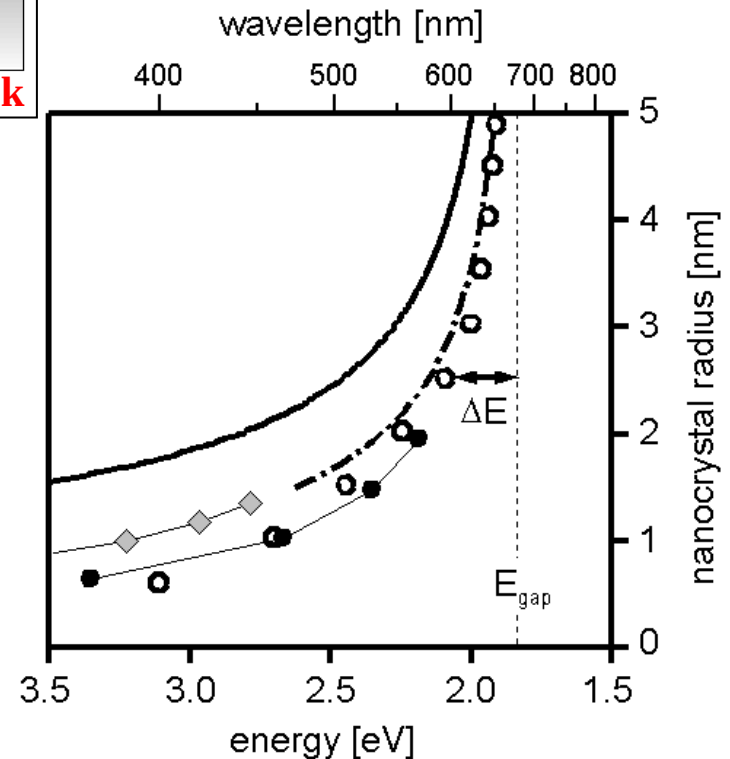
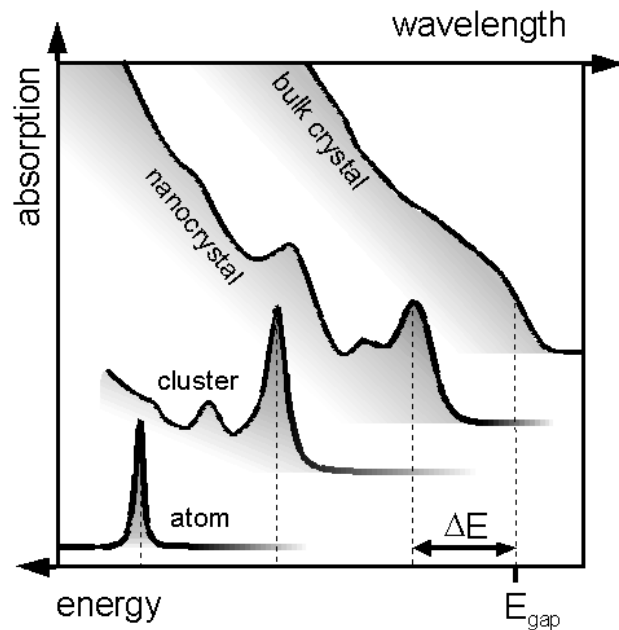
- very large molar extinction coefficients ($1-5 \times 10^6 \text{ M}^{-1} \text{ cm}^{-1}$), $\sim 10-50$ times larger than that of organic dyes

excitonic peak

Size-dependence of optical absorption

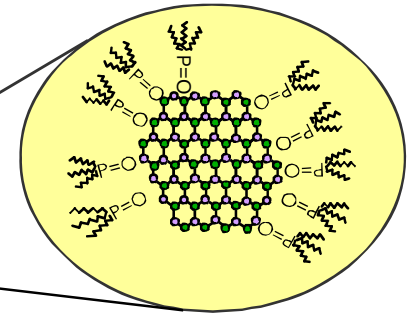
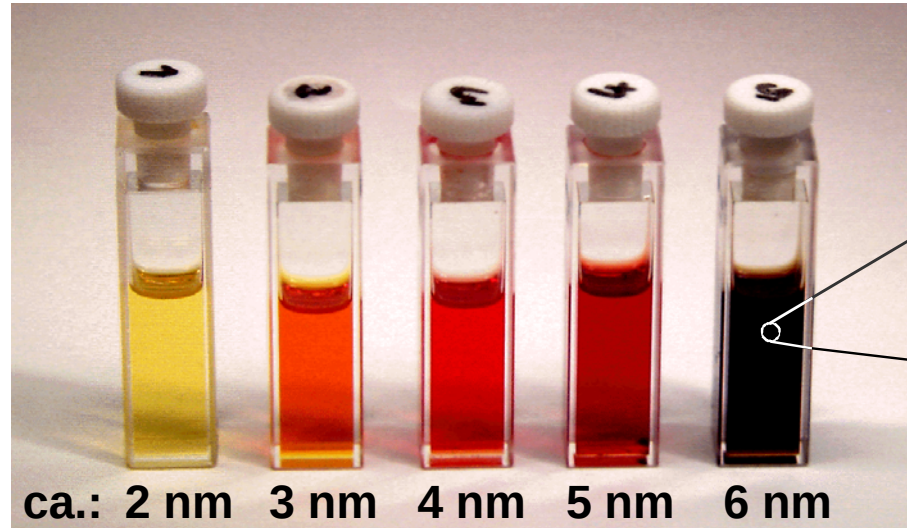


band gap as a function of nanocrystal size:



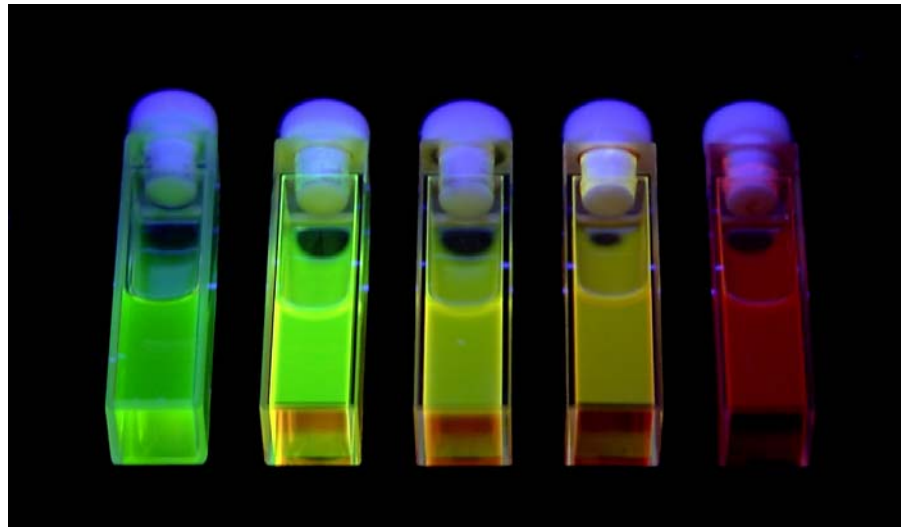
Colloidal CdSe nanocrystals

**CdSe
absorption**

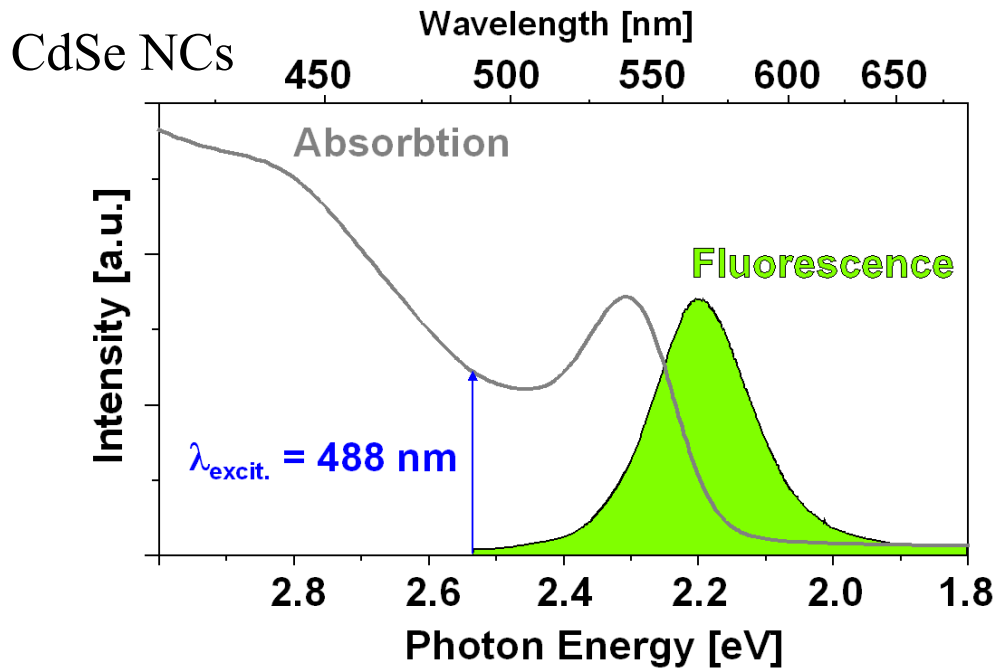


1-10 nm

**CdSe
fluorescence**

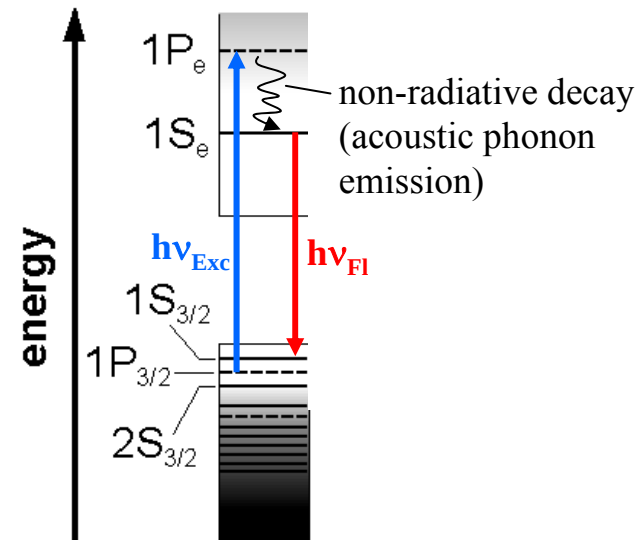


Fluorescence of nanocrystals

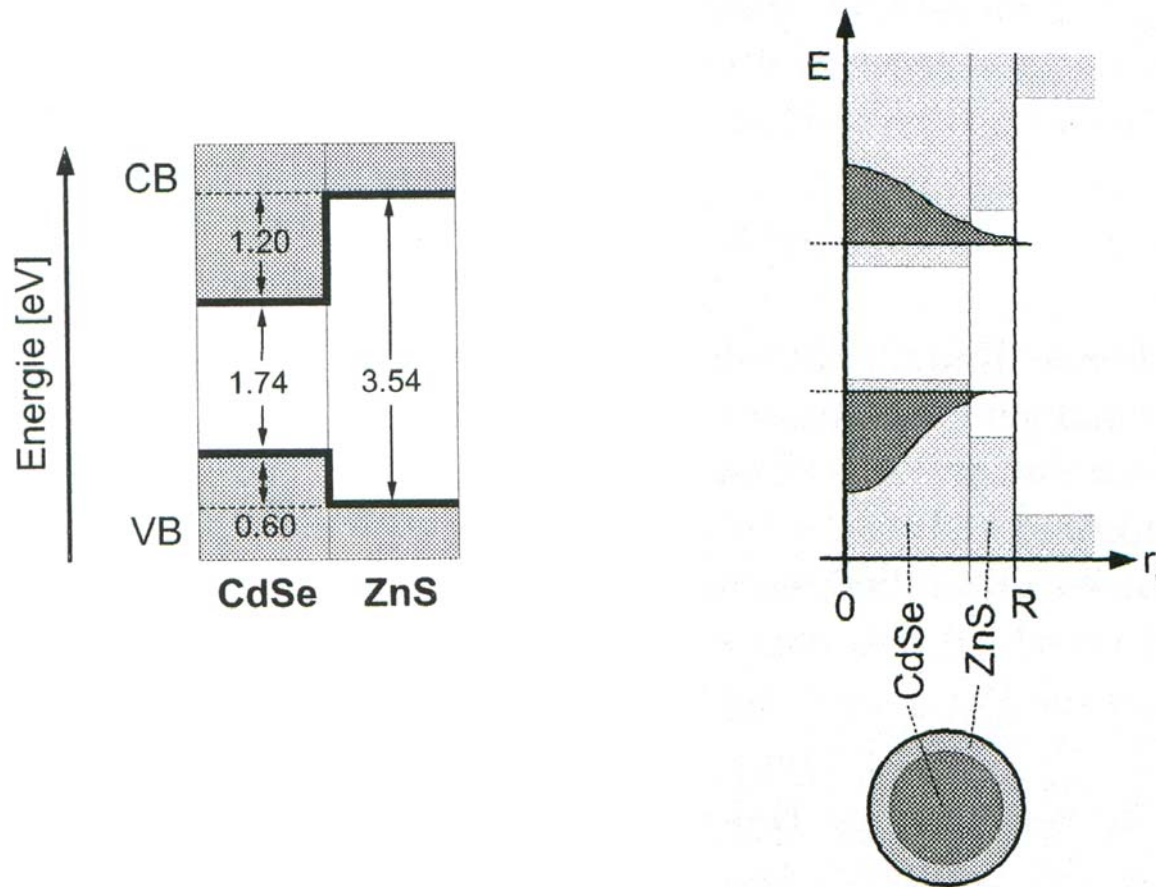


origin of pronounced Stark shift:

fluorescence quantum yield ranges between ~ 40 and 80% , depending on the influence of surface trap states



Core/shell nanocrystals (CdSe/ZnS)

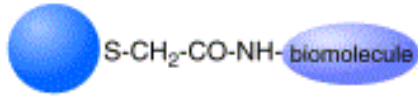


The larger gap ZnS shell confines the wavefunction of the CdSe core and reduces non-radiative exciton recombination at surface defects

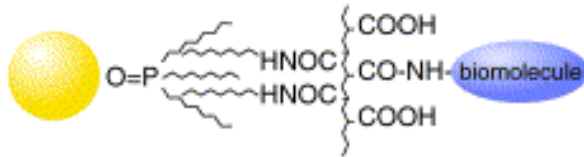
SC nanocrystals as bio-labels

bio-conjugation strategies:

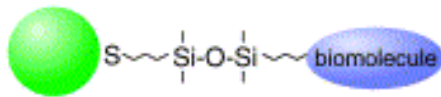
(a) Bifunctional linkage



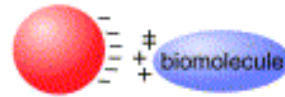
(b) Hydrophobic attraction



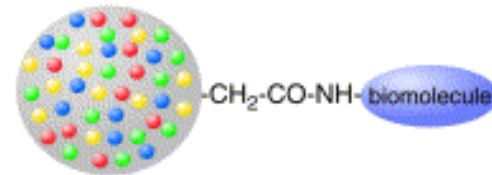
(c) Silanization



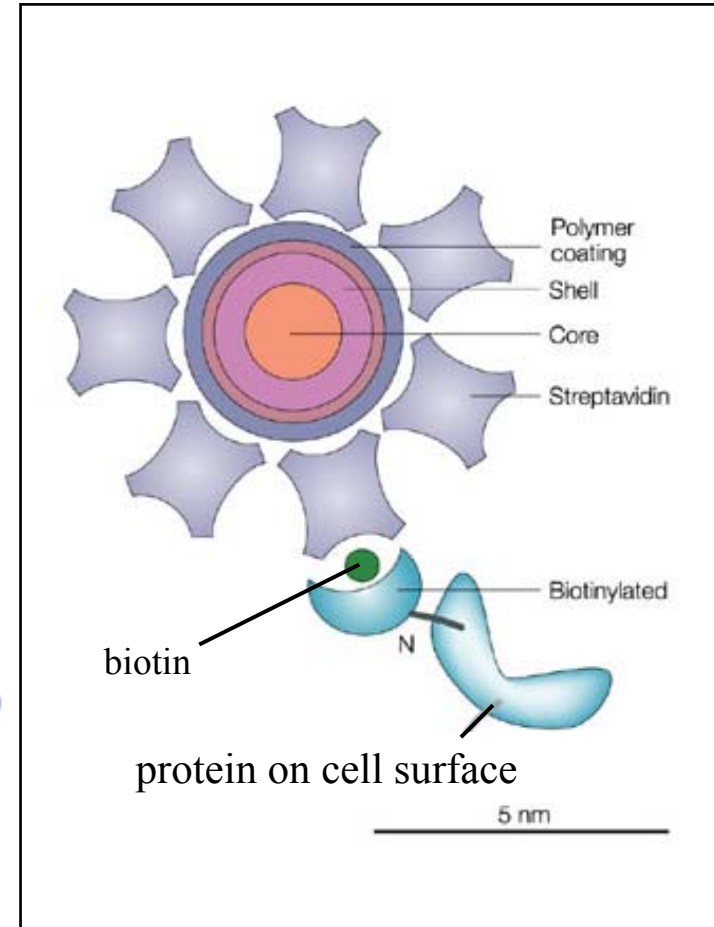
(d) Electrostatic attraction



(e) Nanobeads

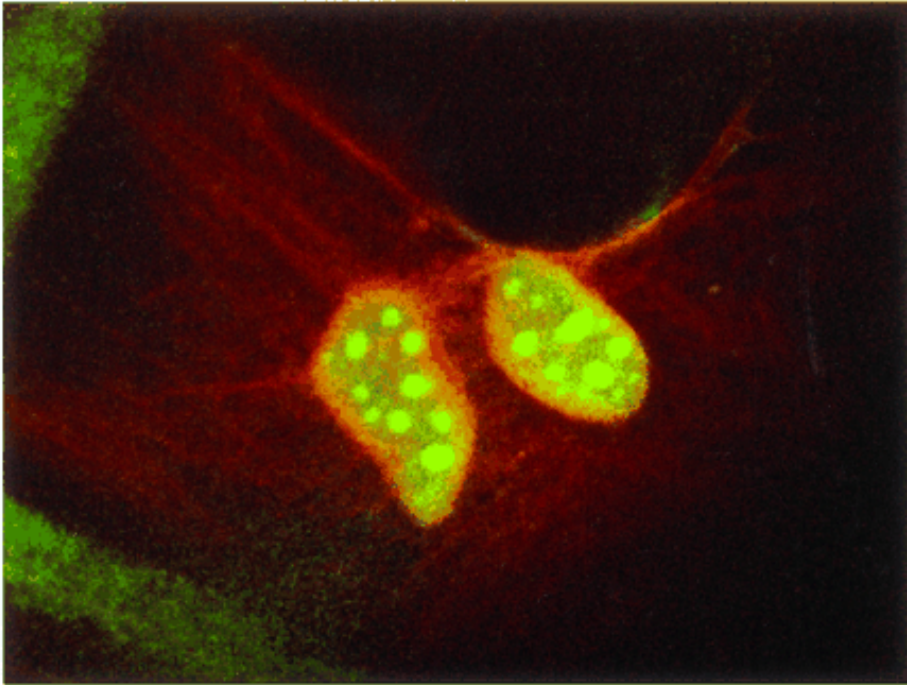


example:



core-shell nanocrystal
conjugated to streptavidin

SC nanocrystals as bio-labels



mouse fibroblast cells stained with CdSe-CdS core-shell particles of different size
(2 nm core particles: green emission;
4 nm core particles: red emission)

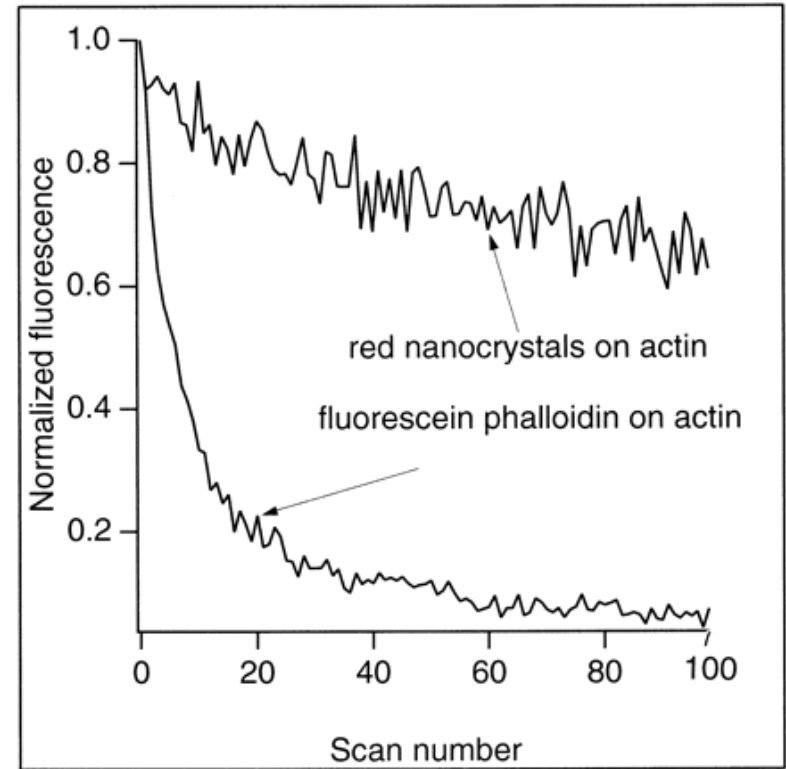
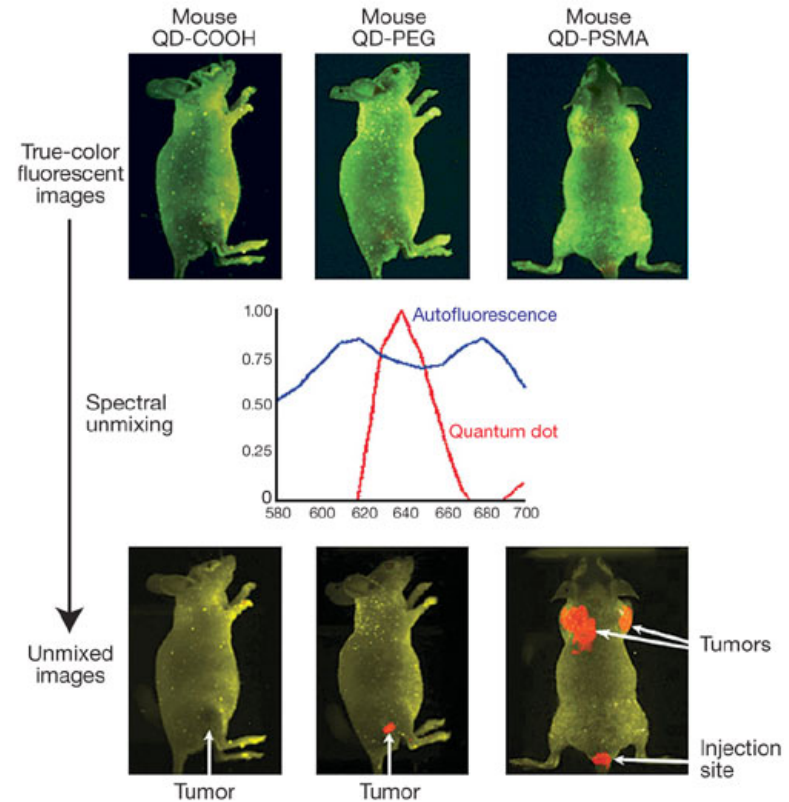
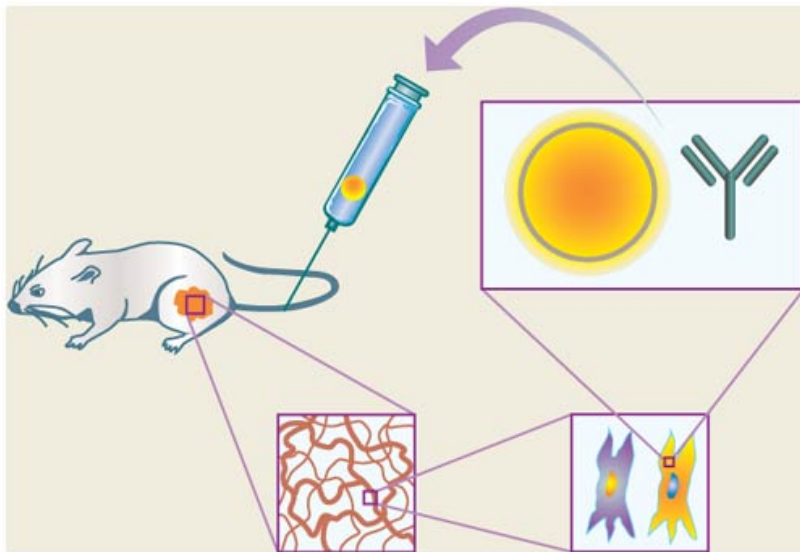


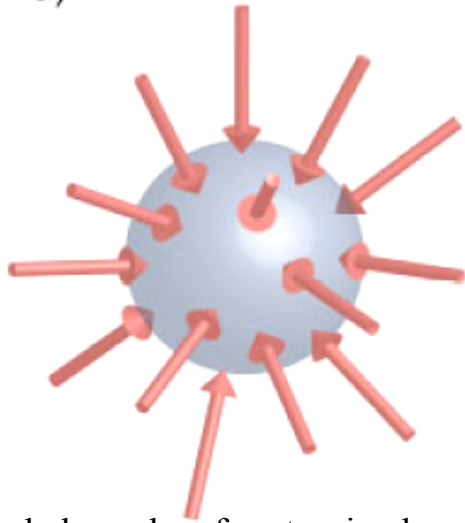
photo-stability comparison for
actin fibres stained with
fluorescent dyes or
core-shell nanocrystals

In-Vivo Cancer Imaging with QD's



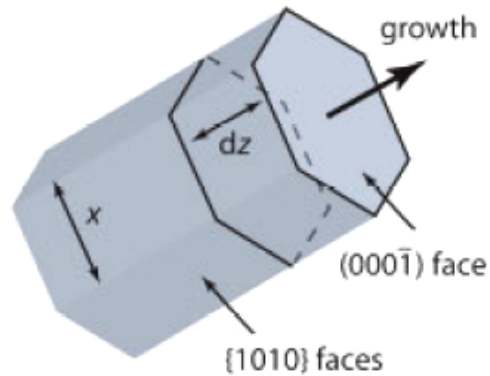
Shape control of NCs

a)



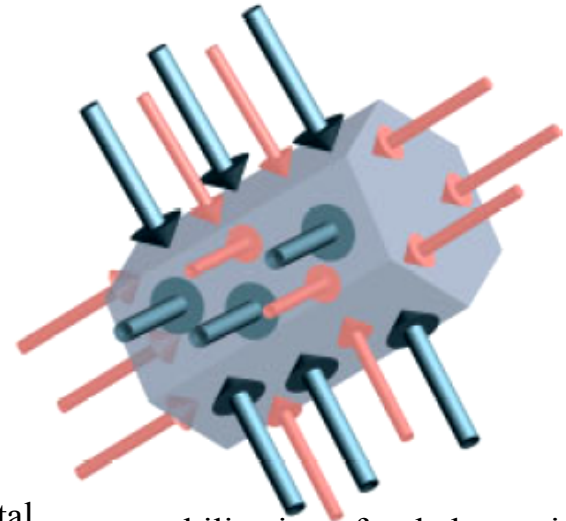
balanced surface tension by
uniform ligand coverage

b)



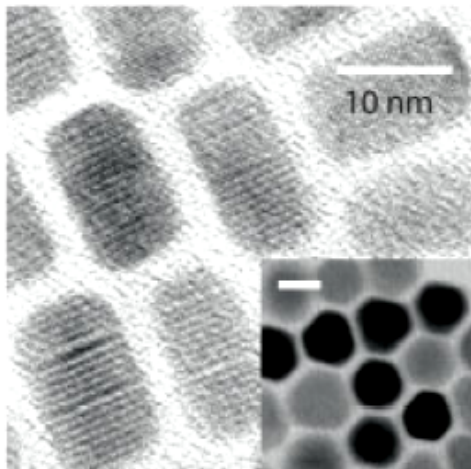
growth of a hexagonal nanocrystal
along the c-axis

c)



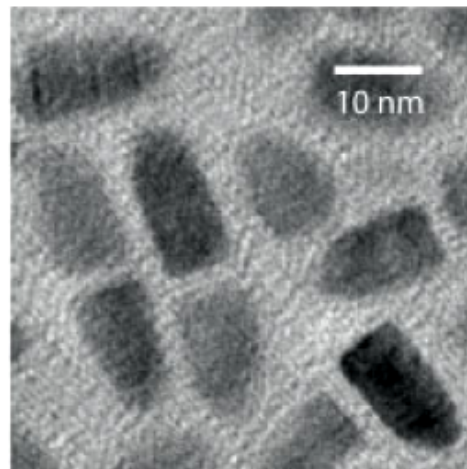
stabilization of rod-shape via
non-uniform ligand coverage

d)



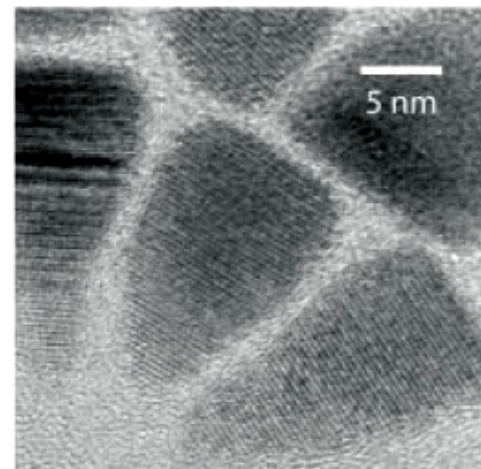
CdSe nanorods

e)



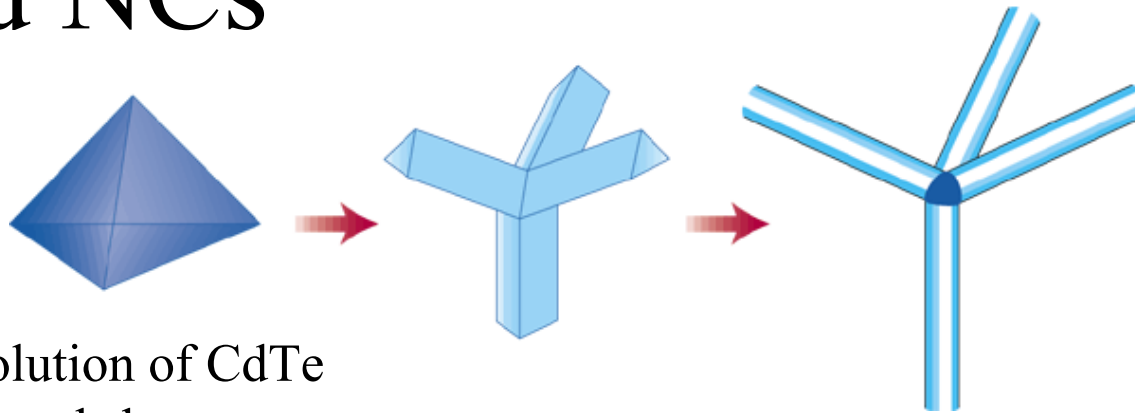
CdSe nanobullets

f)

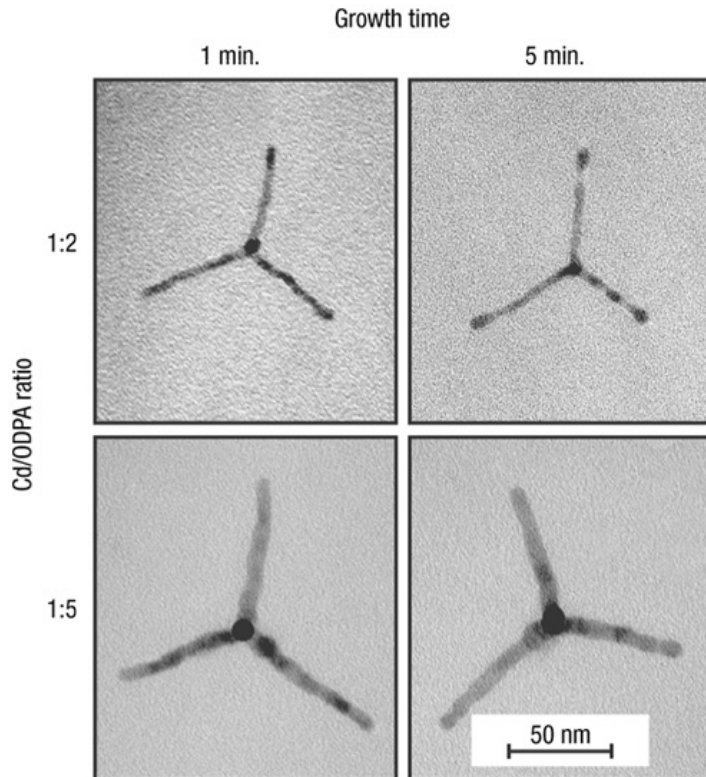


CdSe nanopyramids

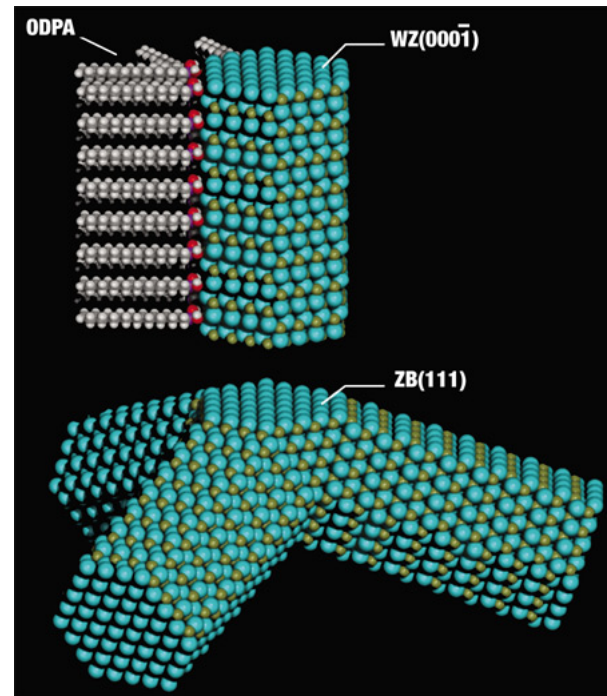
Branched NCs



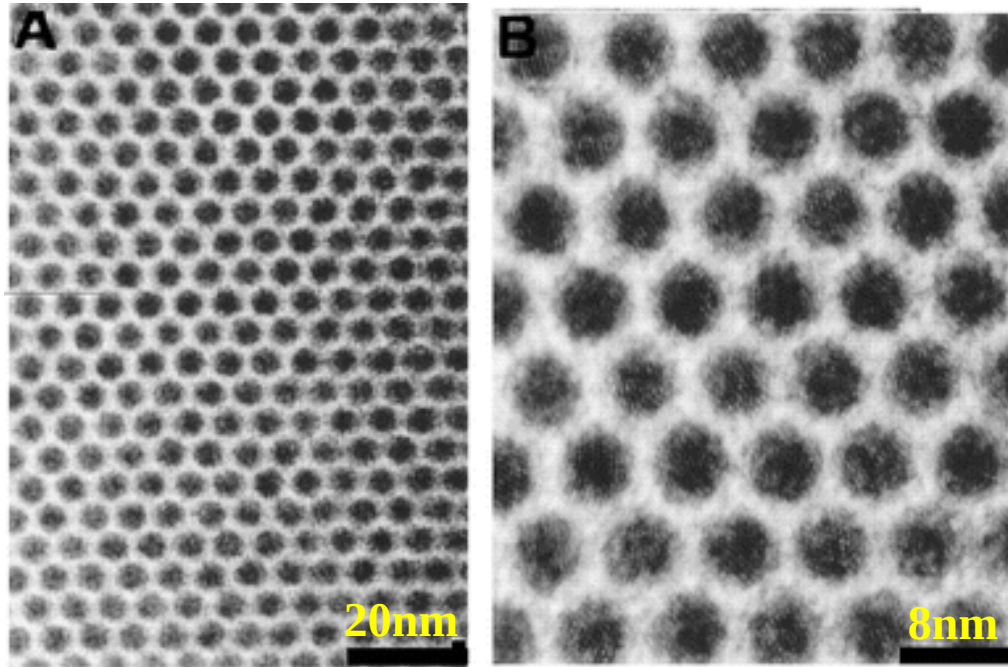
time evolution of CdTe
tetrapod shape:



model of a CdTe tetrapod:



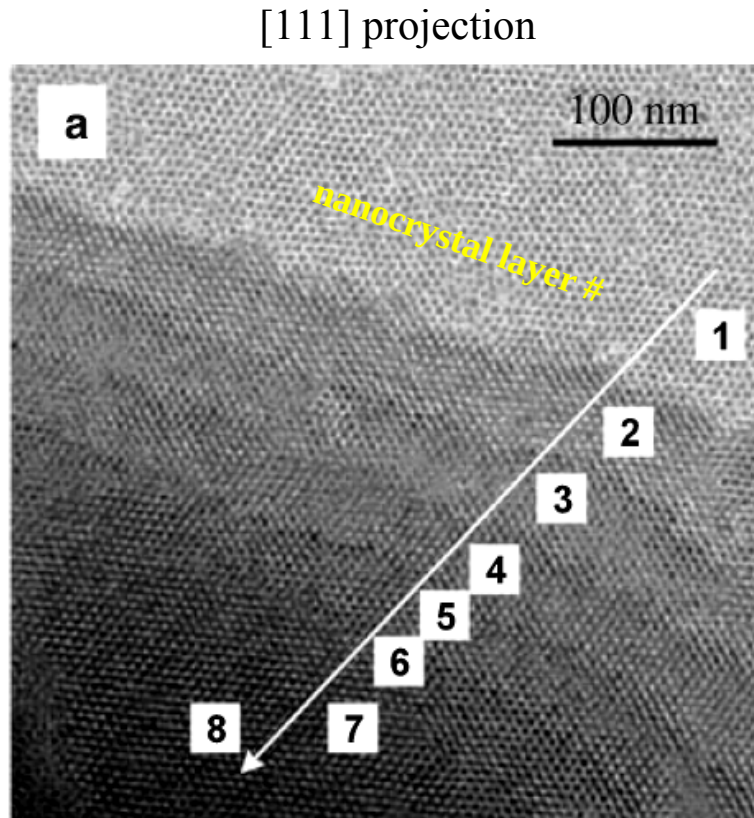
Ordered arrays of semiconductor NCs



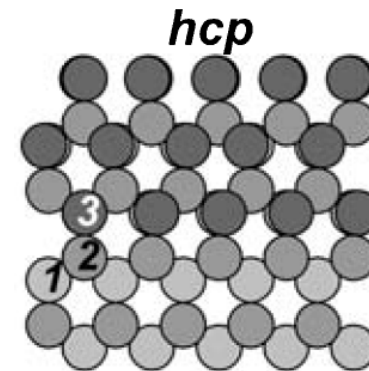
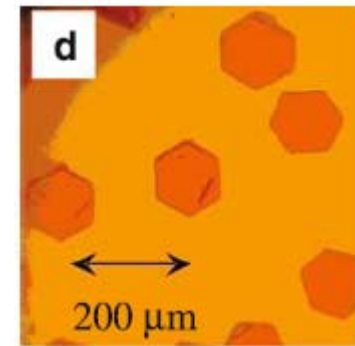
**2D-array of CdSe nanocrystals
($d = 4.8\text{nm}$) on carbon grid**

Semiconductor NC 3D-superstructures

A *hcp* superlattice self-assembled from CdSe NCs:



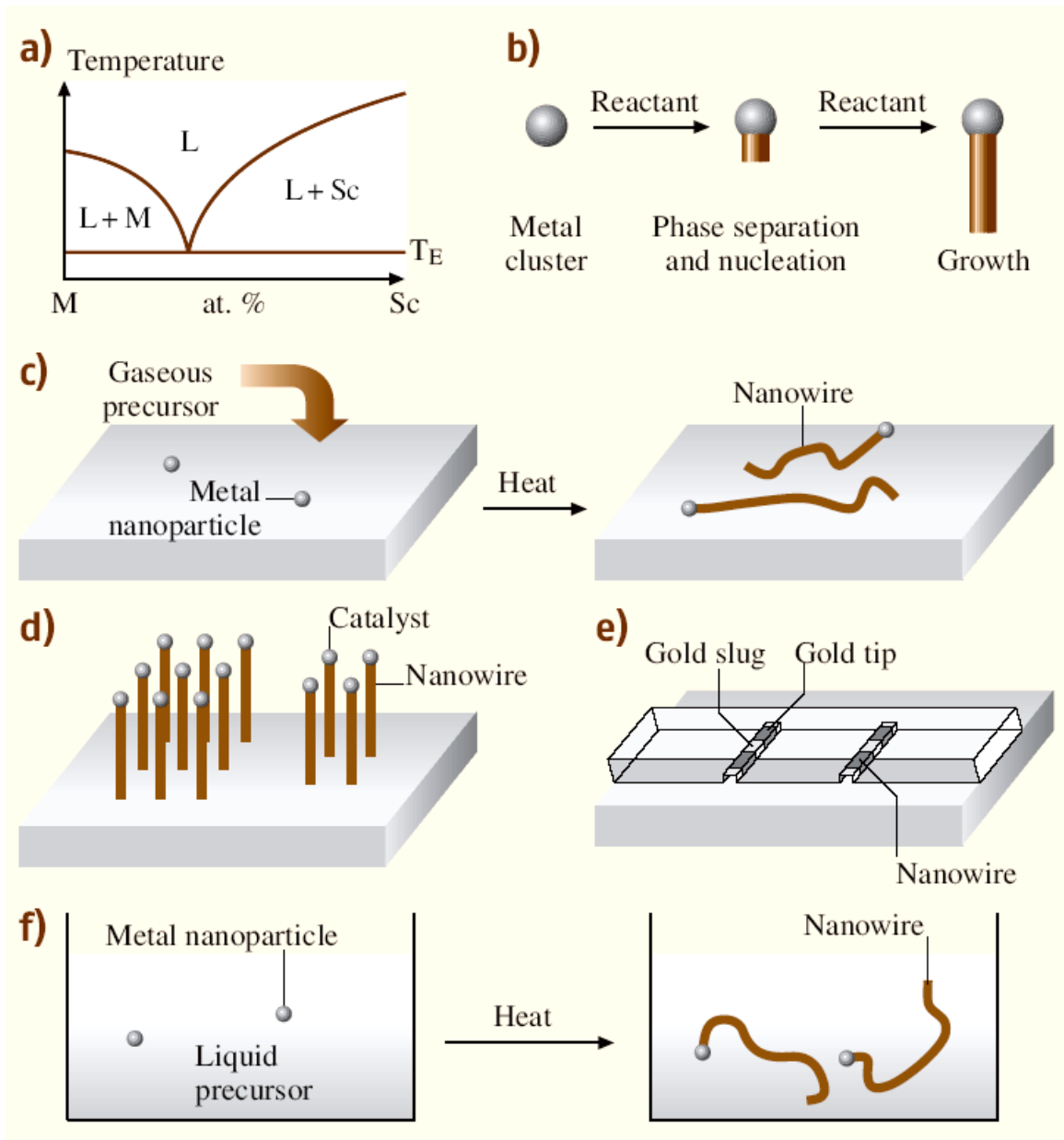
optical micrograph



Semiconductor Nanostructures

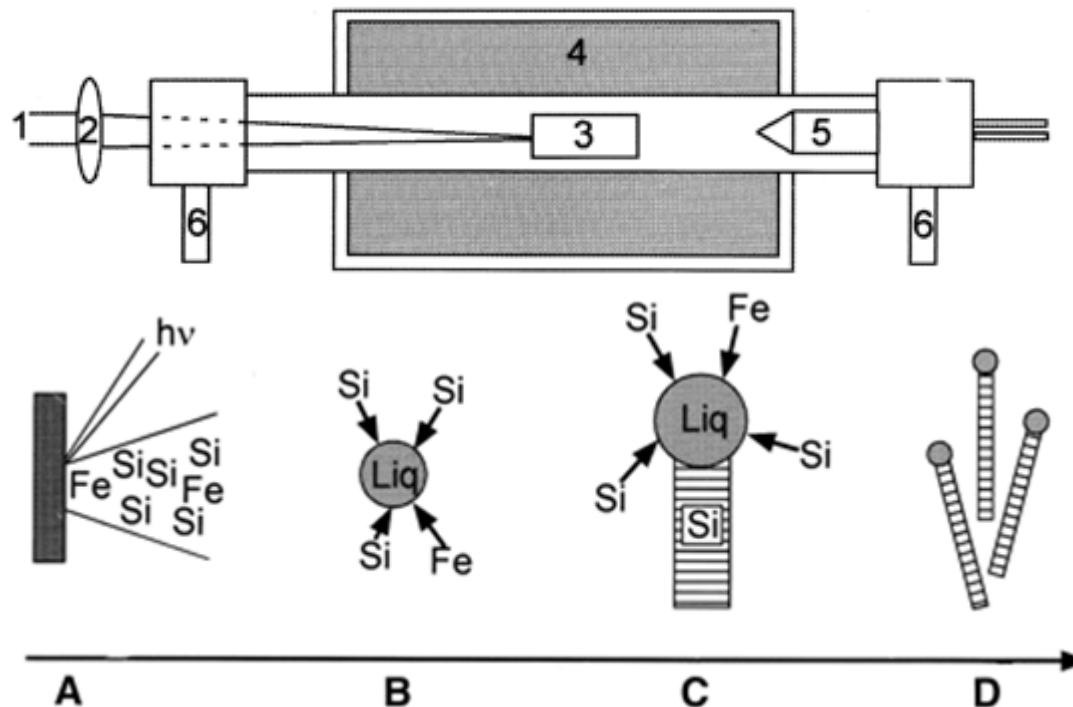
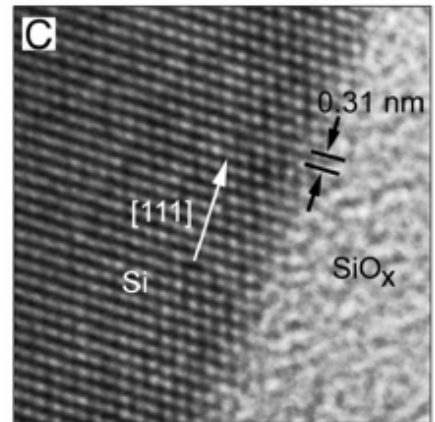
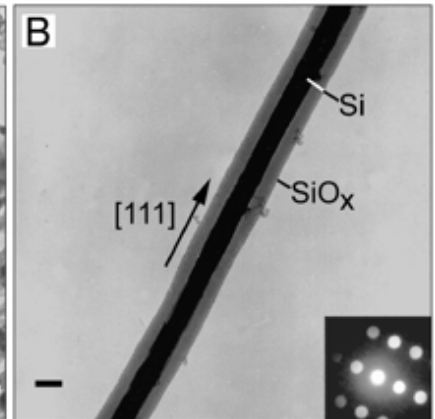
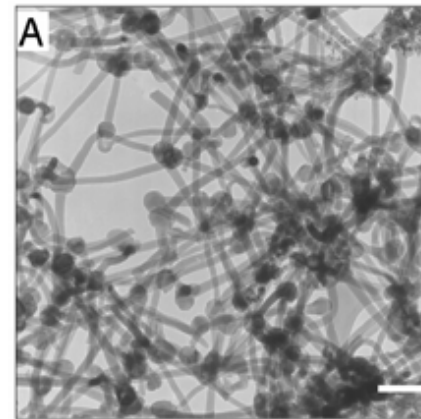
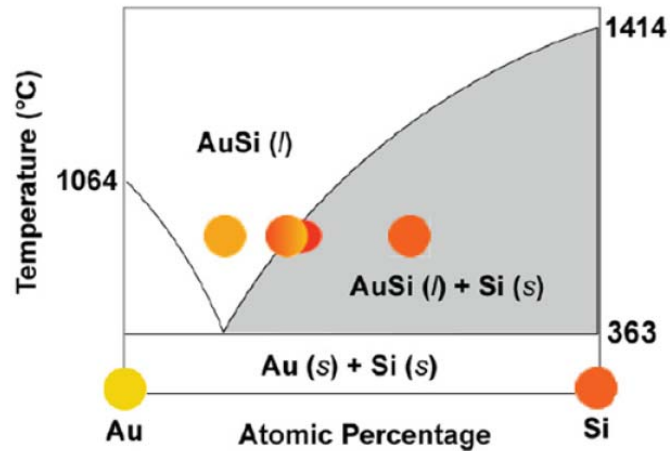
- basics
- MBE quantum dots
- nanocrystals
- nanowires

Synthesis methods - Overview

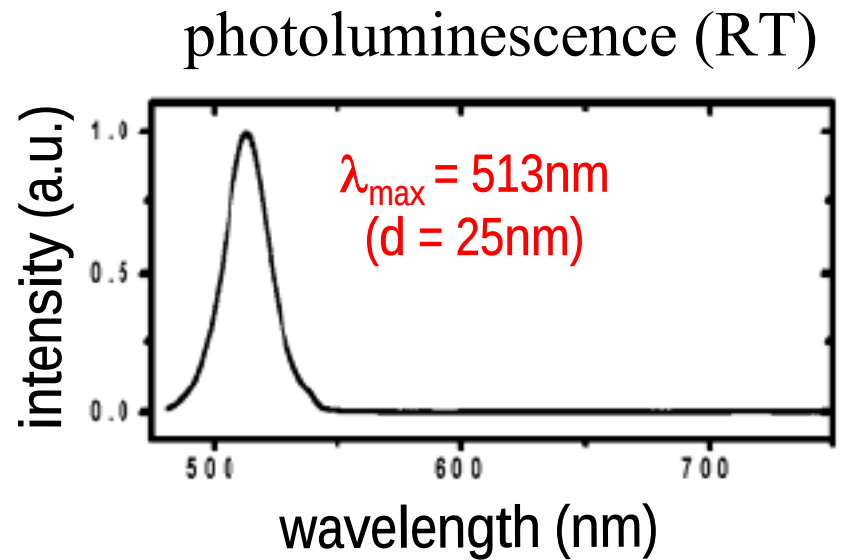
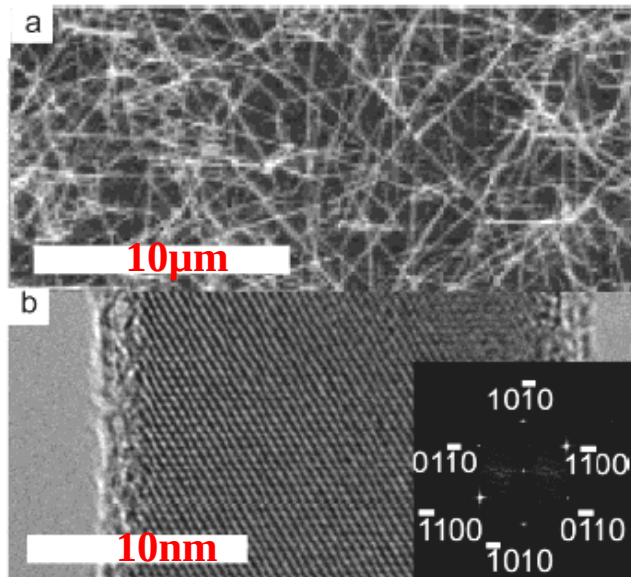
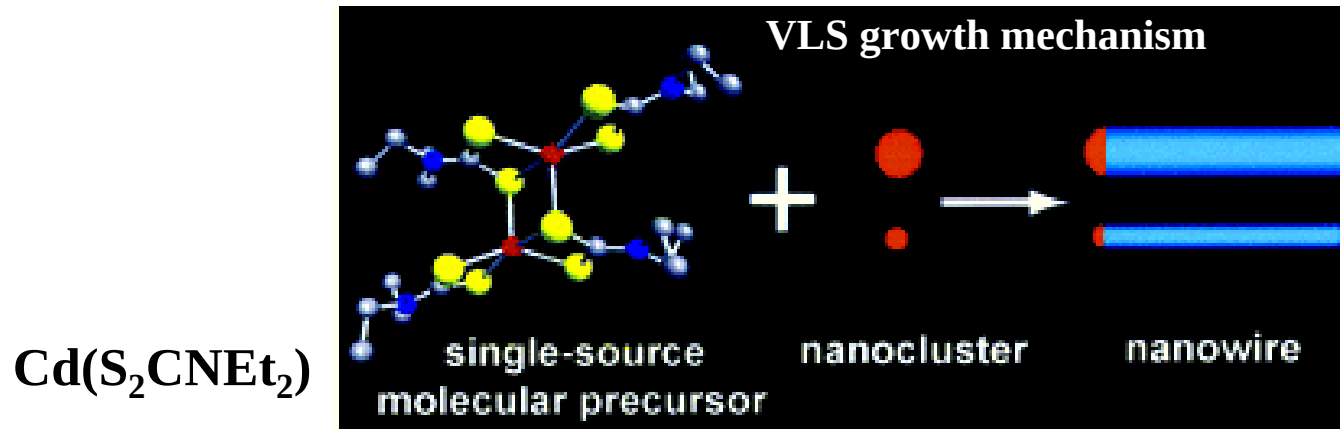


Vapor-liquid-solid growth mechanism

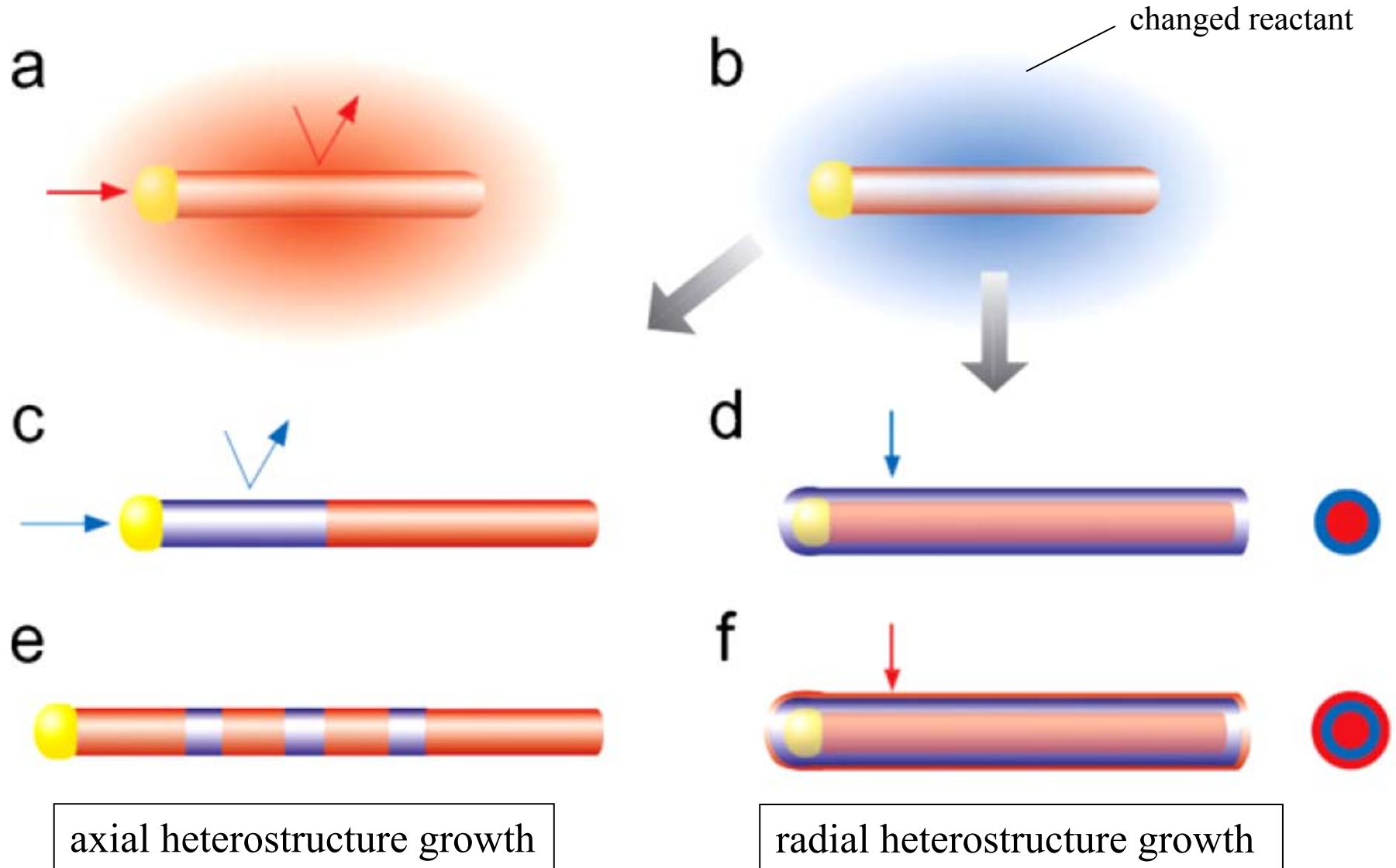
Si nanowire synthesis:



CdS NWs from molecular precursor



Nanowire heterostructure synthesis



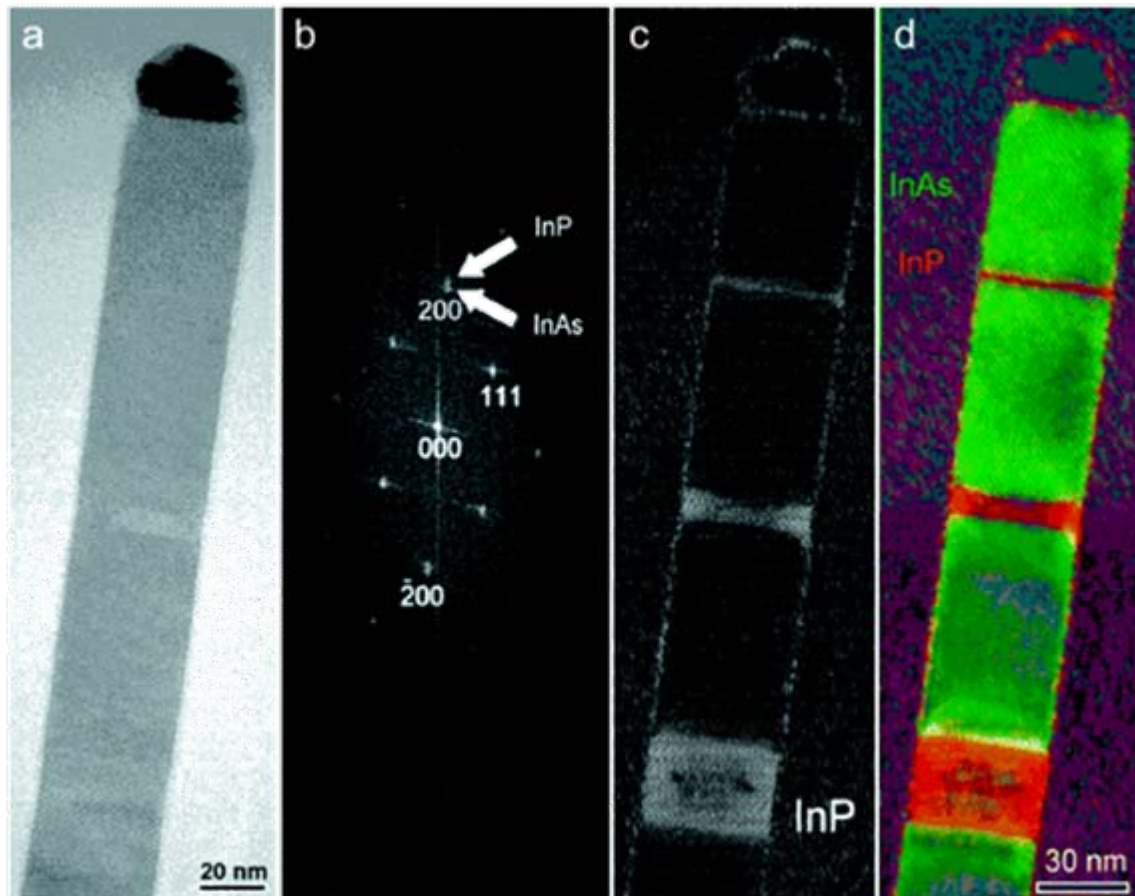
InAs/InP segmented nano-whiskers

TEM

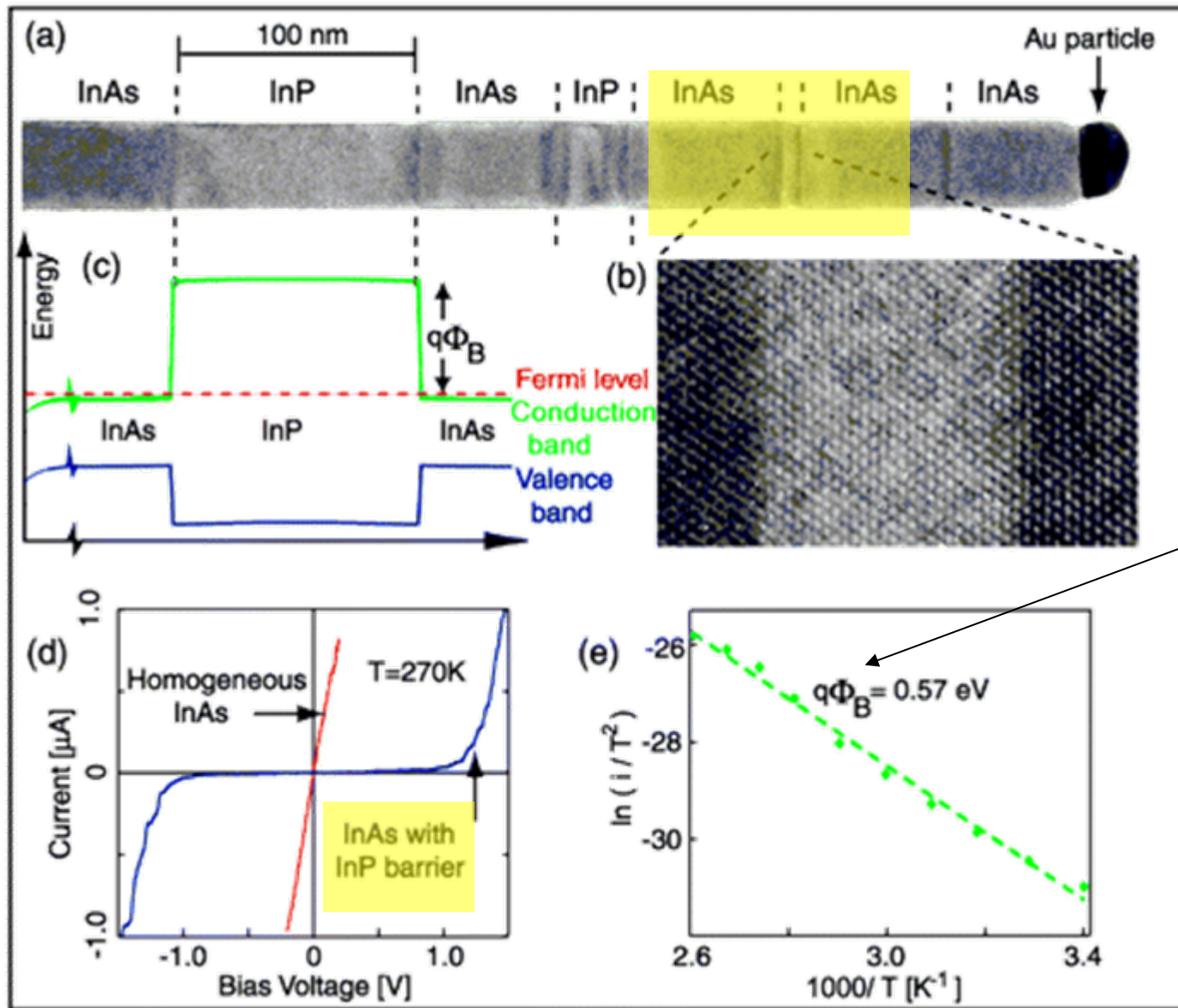
TED

Inverse
FT

Superimposed,
colour-coded
images



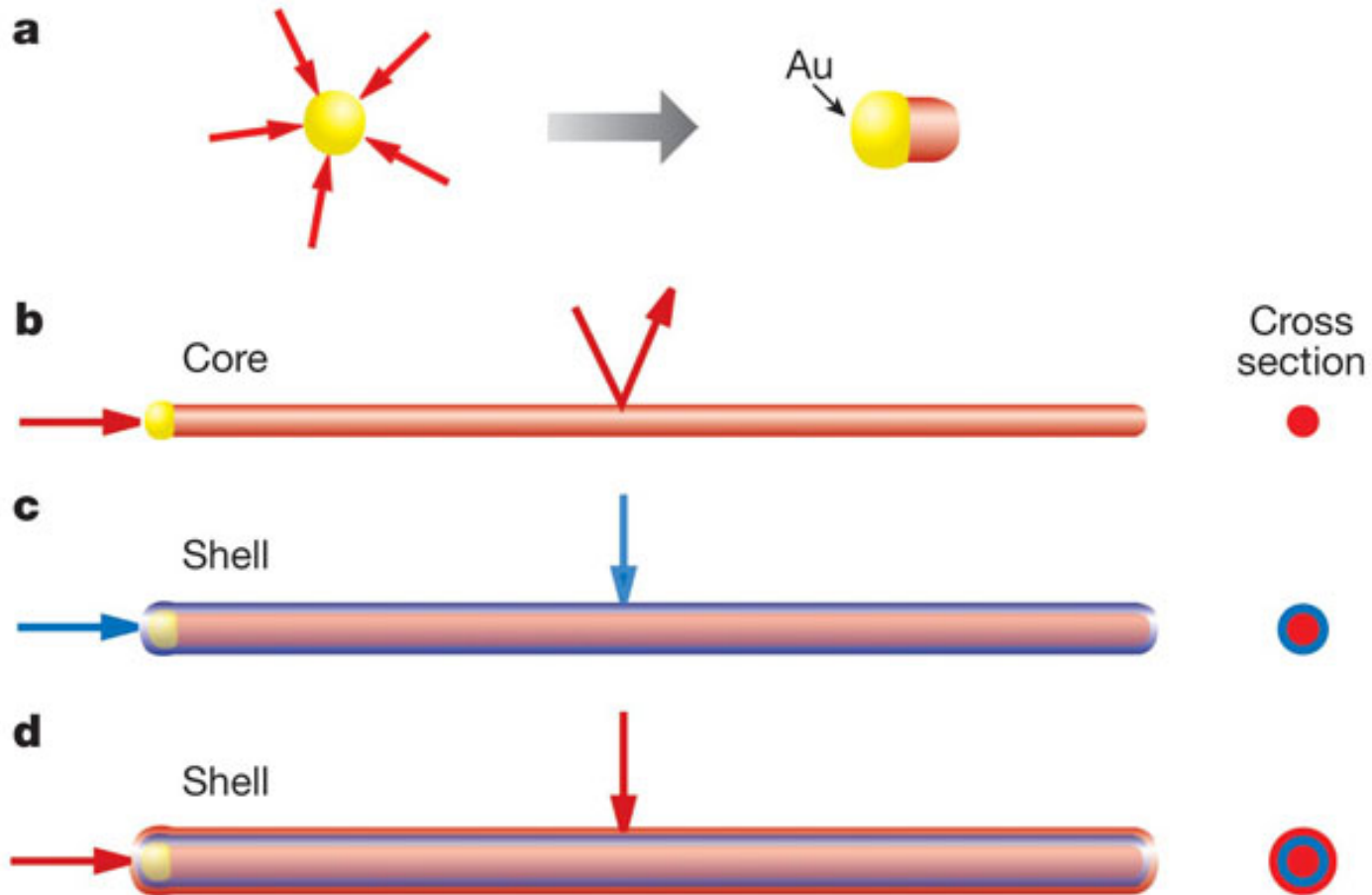
Charge transport over InP barrier



effective barrier
height
(thermionic
excitation)

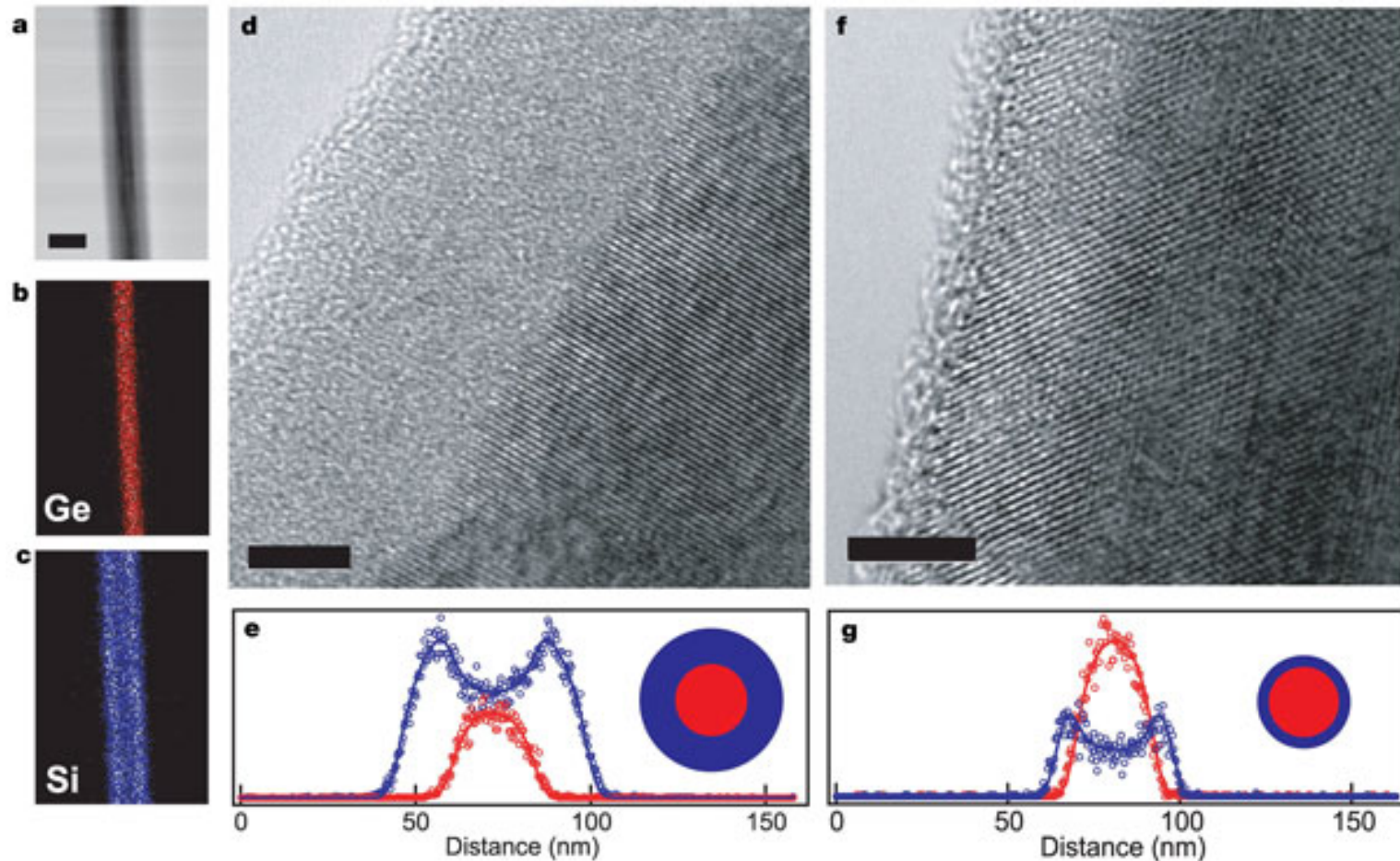
Core-shell semiconductor nanowires

synthesis by chemical vapour deposition:



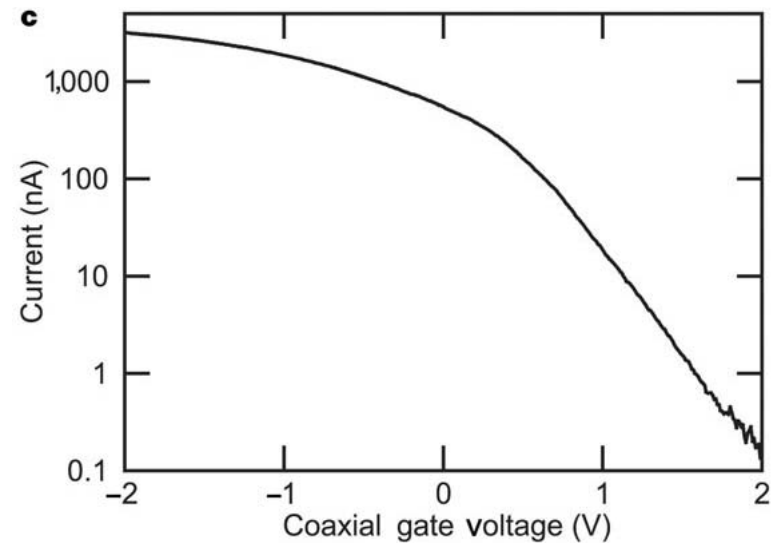
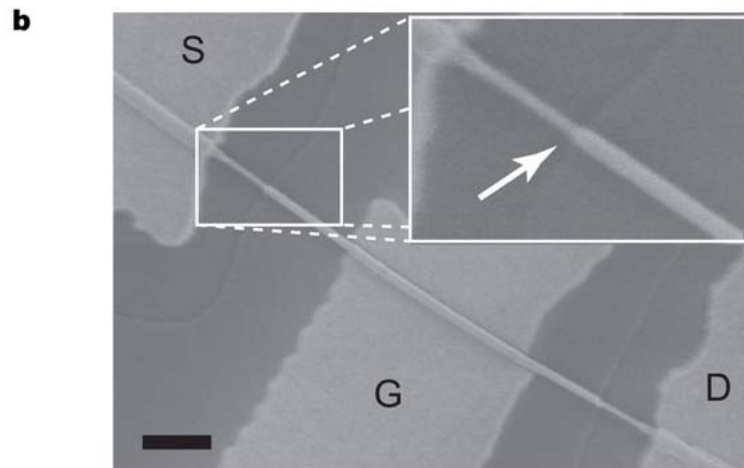
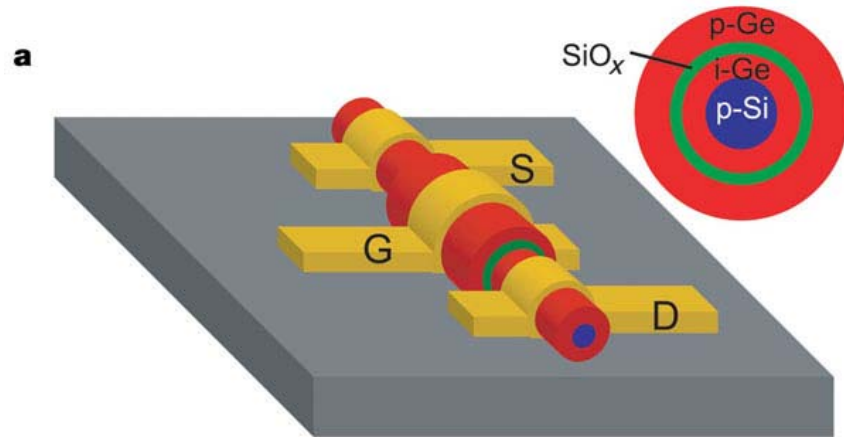
Core-shell semiconductor nanowires

TEM/EDX analysis of Ge-Si core-shell nanowires:



Core-shell semiconductor nanowires

coaxially gated nanowire field-effect transistor from
Ge-Si core-shell nanowires :



Electrons confined to nm dimensions

- can the electrons still be considered to be independent ?
- can the electrons still move in all three dimensions ?