



Ultra-brief summary: 1) Atoms have a spin (S) and orbital (L) moment

2) Competition between V <sub>e-e</sub>	and CF determine S and L:
a) 3d metals	if V <sub>e-e</sub> > CF -> high spin
	if V <sub>e-e</sub> < CF -> low spin
b) rare earth	$V_{e-e} > CF \rightarrow high spin$

3) SOC ( $\xi$ LS) locks S to L

4) Competition between CF and SOC determine the MAE
a) in 3d metals CF > SOC
b) rare earth SOC > CF

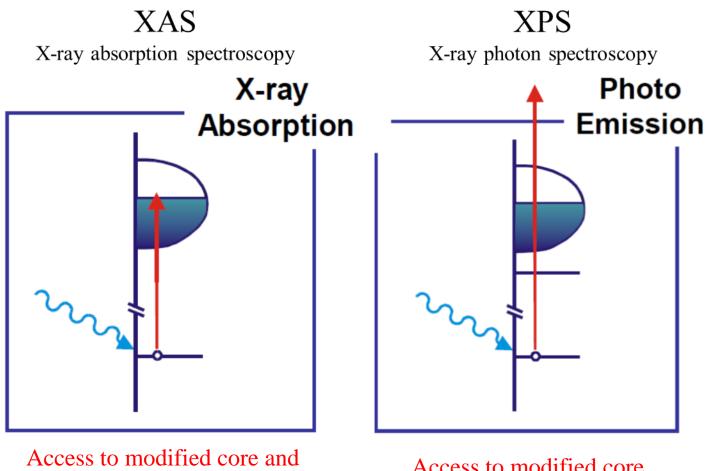
Experimentally: how do we get information about all of this?





CF -> bond formation -> modified valence state (and also core level)

# XPS vs. XAS

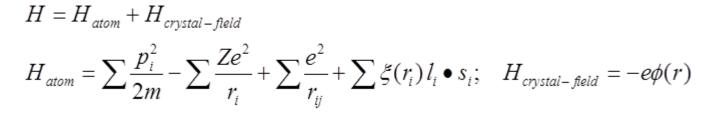


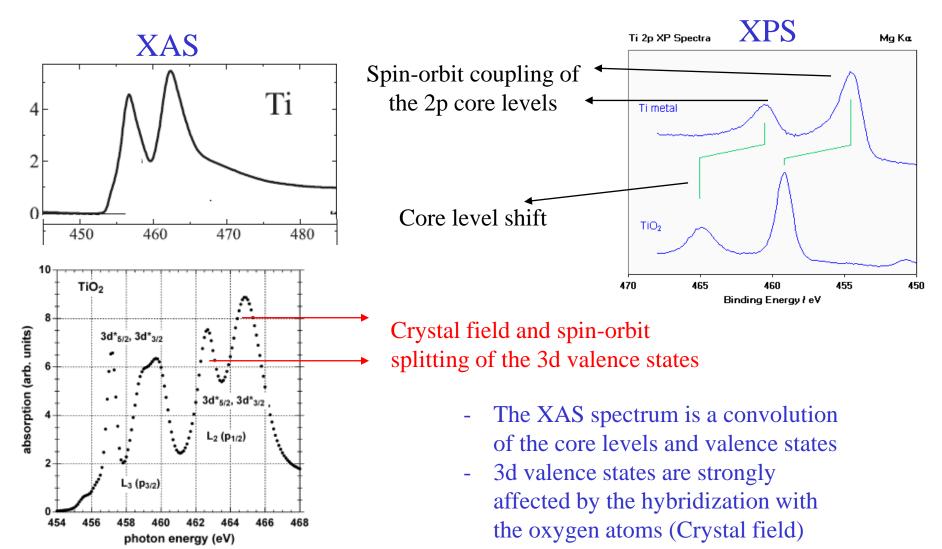
valence states

Access to modified core states



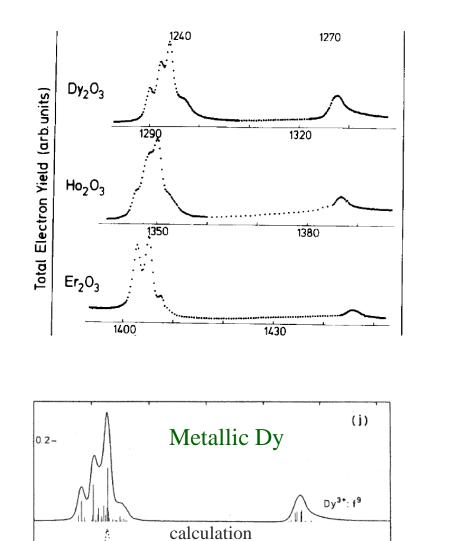












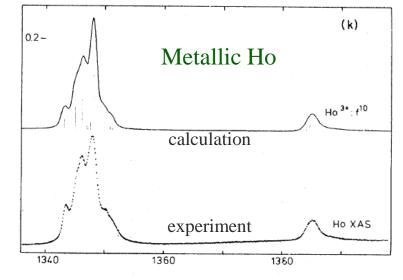
experiment

1310

1290

DyXAS

1330



- The XAS spectrum of rare earth in a metal or in an oxide are very similar
- 4f valence states are strongly localized and only slightly affected by the hybridization with the oxygen atoms (Crystal field)

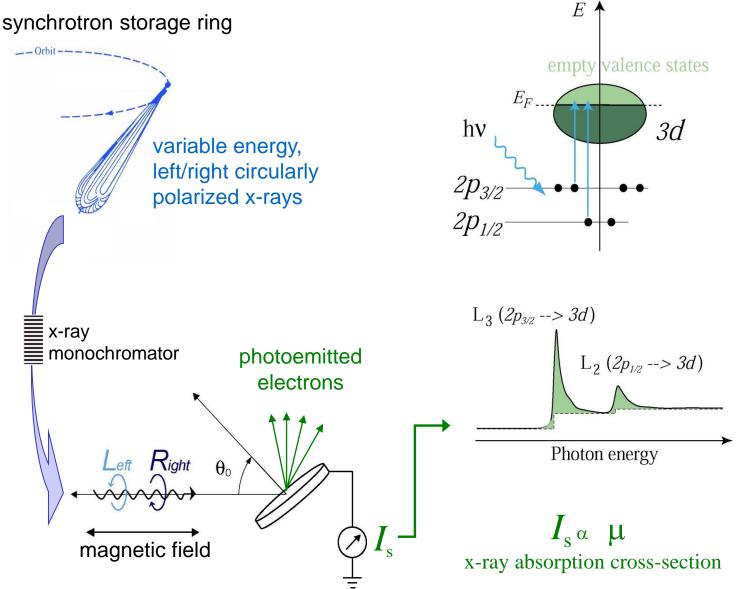


# X-rays absorption and X-ray magnetic circular dichroism (XMCD)



Two step model:

- 1) spin-polarized photoelectrons are created by using circularly polarized x-rays
- 2) these polarized photoelectrons are used to analyze the spin-split valence density of states, thus the valence band acts as a spin-sensitive detector.







Photon-electron interaction: dipole approximation

$$H_{int}(0,t) \approx \underline{r} \cdot \underline{\varepsilon}_{q} \left[ a_{k} \exp(-i\omega_{k}t) + c.c. \right]$$

The dipole operator  $P_q^{\ 1} = \underline{r} \cdot \underline{\varepsilon}_q$  can be written in terms of Racah's tensor operators (where  $Y_{1,m}$  are the spherical harmonics)

The photon absorption generates a transition from an initial core level to a final level close to the Fermi level (note that the spin is not affected)

$$|i\rangle = R_i(r) |c, m_c; s = \frac{1}{2}, m_s\rangle \qquad \longrightarrow \qquad |f\rangle = R_f(r) |l, m_l; s = \frac{1}{2}, m_s\rangle$$

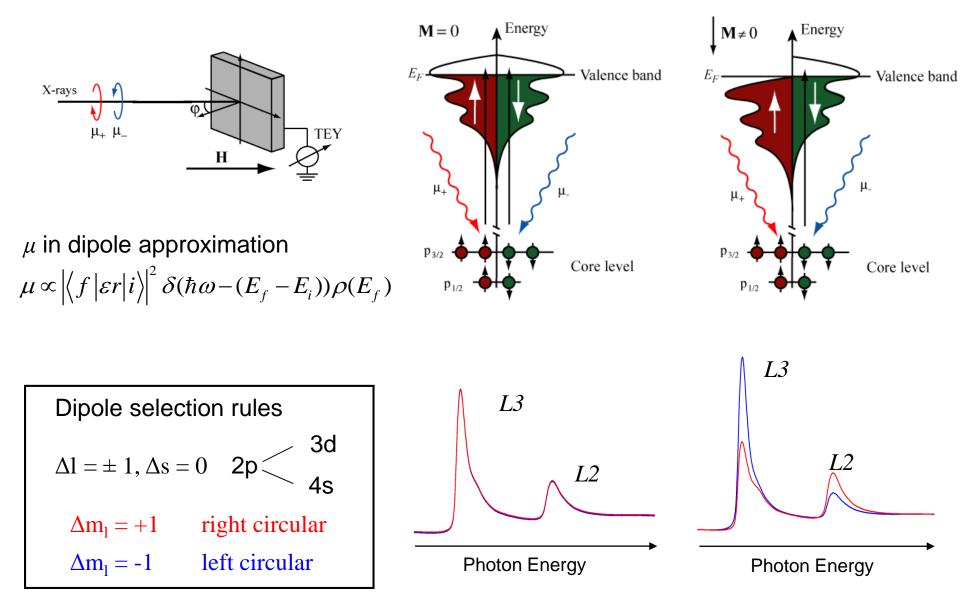
**Table 1.3:** Electric dipole matrix elements  $\langle l, m_l | C_q^{(1)} | c, m_c \rangle$  in the one electron model. The matrix elements are non-vanishing when c = l - 1 (left column) or c = l + 1 (right column), and when  $m_c + q = m_l$ . q denotes the state of polarization of the photons which mix the states  $|l, m_l\rangle$  and  $|c, m_c\rangle$ .

Remember: things become easily complicate. For example, if spin-orbit interaction is not negligible the (L,  $m_L$ , S,  $m_S$ ) is not the good basis and you have to use the (L, S, J,  $m_J$ ) basis

 $\underline{\varepsilon}_q$  is the polarization dependent electric vector





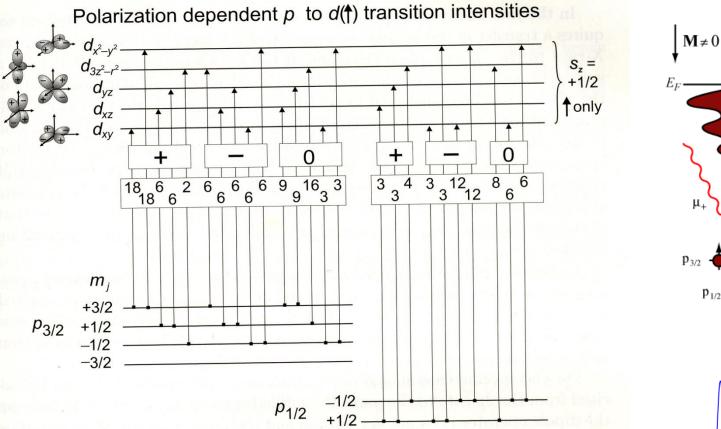


2p -> 4s transitions account for less than 5% of the total XAS intensity -> neglected

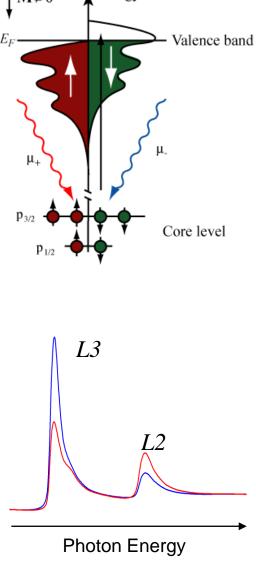


# X-rays absorption and X-ray magnetic circular dichroism (XMCD)





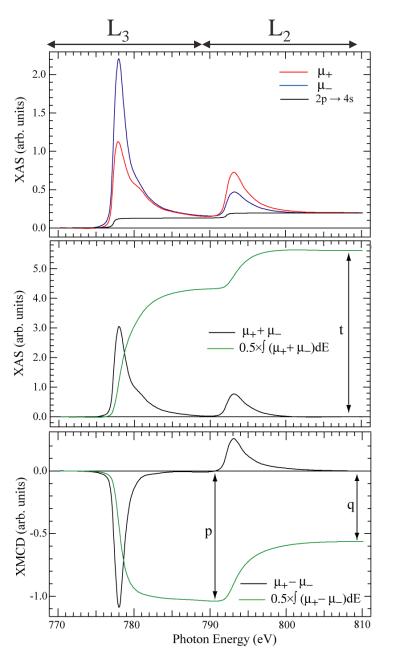
**Fig. 9.14.** Polarization dependent transition intensities in a one-electron model from spin-orbit and exchange split p core states  $|j, m_j\rangle$  to spin-up  $(m_s = +1/2) d$  valence orbitals (Table A.2), assumed to be split by the exchange interaction. The listed intensities each need to be divided by 90 to get the proper absolute values in units of  $\mathcal{AR}^2$ . We have chosen the z-axis as the spin quantization axis and the transition intensities are for circular polarization with  $k \parallel z$  and angular momenta q = +1(labeled +) and q = -1 (labeled -) and for linear polarization with  $E \parallel z$  (labeled q = 0). We have assumed a splitting of the p states by the exchange interaction, lifting the degeneracy in  $m_j$ . Note that this causes an opposite order of  $m_j$  states for  $p_{3/2}$ , l + s and  $p_{1/2}$ , l - s because of the opposite sign of s



Energy







Sum rules for 3d transition metals:  $L = -\frac{4}{3}h_d \frac{\int_{L_{3+L_2}} (\mu_+ - \mu_-)dE}{\int_{L_{3+L_2}} (\mu_+ + \mu_-)dE} = -\frac{4}{3}h_d \frac{q}{t}$   $S + 7D = -h_d \frac{6\int_{L_3} (\mu_+ - \mu_-)dE - 4\int_{L_{3+L_2}} (\mu_+ - \mu_-)dE}{\int_{L_{3+L_2}} (\mu_+ + \mu_-)dE}$   $= -h_d \frac{6p - 4q}{t}$ 

h<sub>d</sub> -> number of d-holes in the valence band (frequently unknown) D -> spin dipole moment

$$r = \frac{L}{S + 7D}$$

This value is independent on h<sub>d</sub> and can be easily compared among different samples

B. T. Thole *et al.* PRL **68**, 1943 (1992)P. Carra *et al.* PRL **70**, 694 (1993)



#### **General sum rules**



 $\equiv \frac{\int_{\text{edge}} d\omega (\mu^+ - \mu^-)}{\int_{\text{edge}} d\omega (\mu^+ + \mu^- + \mu^0)}$  $\rho$  $= \frac{1}{2} \frac{c(c+1) - l(l+1) - 2}{l(l+1)(4l+2-n)} \frac{\langle L_z \rangle}{\hbar}$ 

Orbital moment L

$$\delta \equiv \frac{\int_{j_{+}} d\omega (\mu^{+} - \mu^{-}) - [(c+1)/c] \int_{j_{-}} d\omega (\mu^{+} - \mu^{-})}{\int_{j_{+}+j_{-}} d\omega (\mu^{+} + \mu^{-} + \mu^{0})}$$
  
magnetic dipole T
$$= \frac{l(l+1) - 2 - c(c+1)}{3c(4l+2-n)} \frac{\langle S_{z} \rangle}{\hbar}$$

Spin S + n

$$\frac{J_{j_{+}+j_{-}} d\omega (\mu^{+} + \mu^{-} + \mu^{z})}{\frac{l(l+1) - 2 - c(c+1)}{3c(4l+2-n)}} \frac{\langle S_{z} \rangle}{\hbar} + \frac{l(l+1) [l(l+1) + 2c(c+1) + 4] - 3(c-1)^{2}(c+2)^{2}}{6lc(l+1)(4l+2-n)} \frac{\langle T_{z} \rangle}{\hbar}$$

 $c \rightarrow core$  electron orbital moment

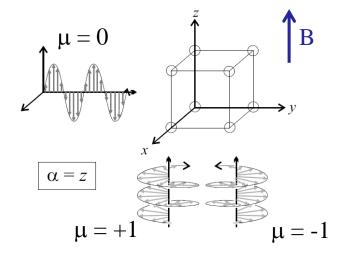
 $l \rightarrow$  valence electron orbital moment

 $n \rightarrow$  number of electrons in the valence shell

 $L_{2,3}$  edges of 3d metal : c = 1 (p states) and l = 2 (d states)  $M_{4.5}$  edges of rare earth: c = 2 (d states) and l = 3 (f states)

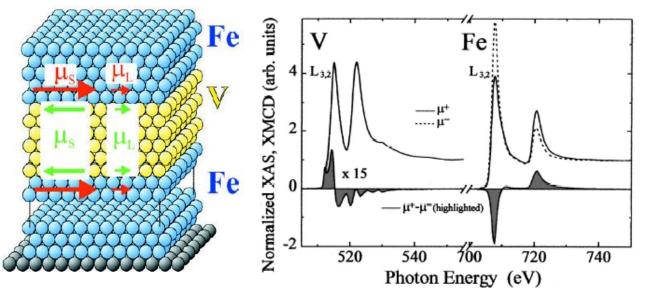
$$h_d \propto \int_{L_{3+L_2}} (\mu_+ + \mu_- + \mu_0) dE \approx \frac{3}{2} \int_{L_{3+L_2}} (\mu_+ + \mu_-) dE$$

Experimentally difficult to measure along the three directions ( $\alpha$  is the quantization axis defined by the external field)









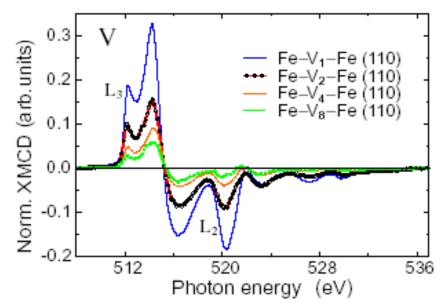
Normalized XAS of L (dashed line) and R (solid line) circularly polarized light and the XMCD at the  $L_{2,3}$  edges of V and Fe for a Fe/V4 /Fe(110) trilayer.

Antiferromagnetic coupling: XMCD signal for V and Fe have opposite signs

The induced magnetic moment in the V atoms strongly reduces with increasing the V thickness

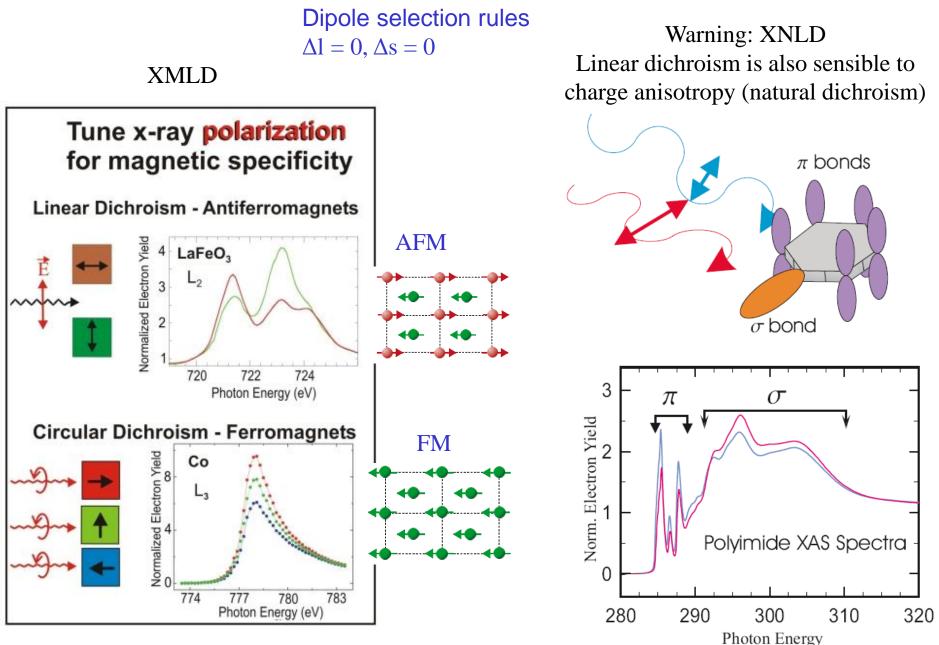
Sum rules can not be easily applied due to overlapping between  $2p^{1/2}$  and  $2p^{3/2}$  states

A. Scherz et al., J. Appl. Phys. 91, 8760 (2002)





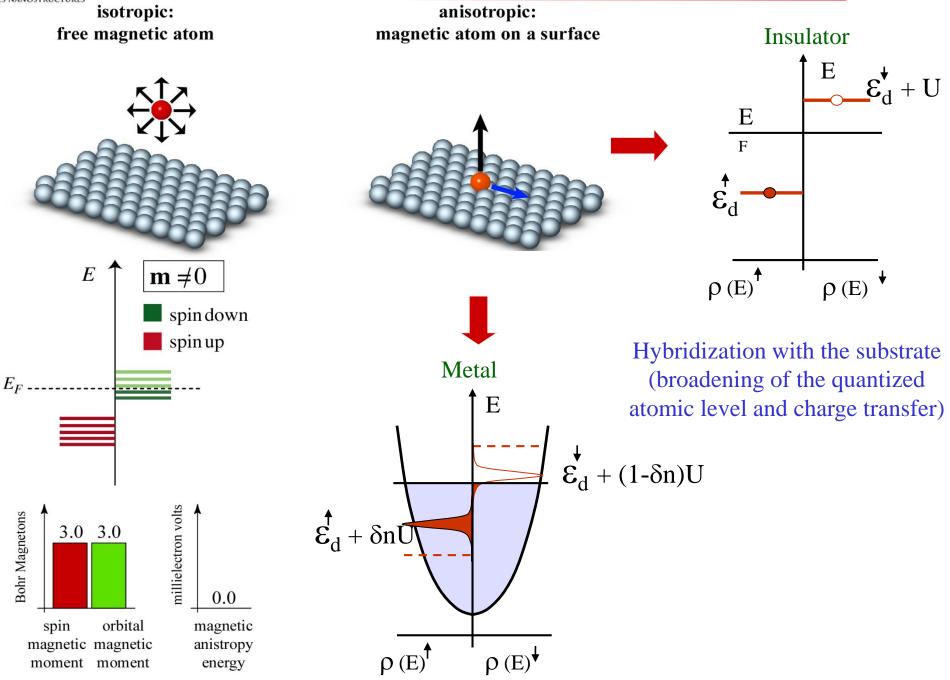




J. Regan, PhD thesis (2001), Stanford university

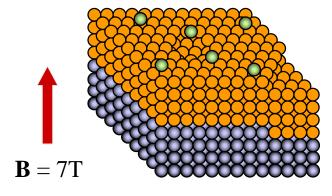












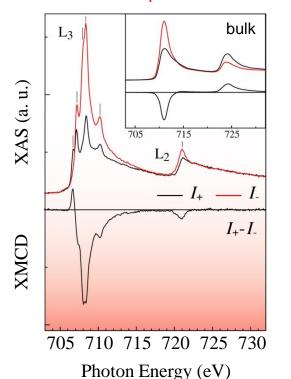
Fe, Co atoms (<0.01 ML)

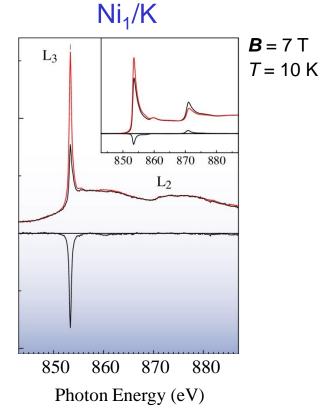
Cs, K, Na, or Li film Cu(100)

Co<sub>1</sub>/K

Spectra are independent on the **B** field orientation: absence of magnetization easy axis





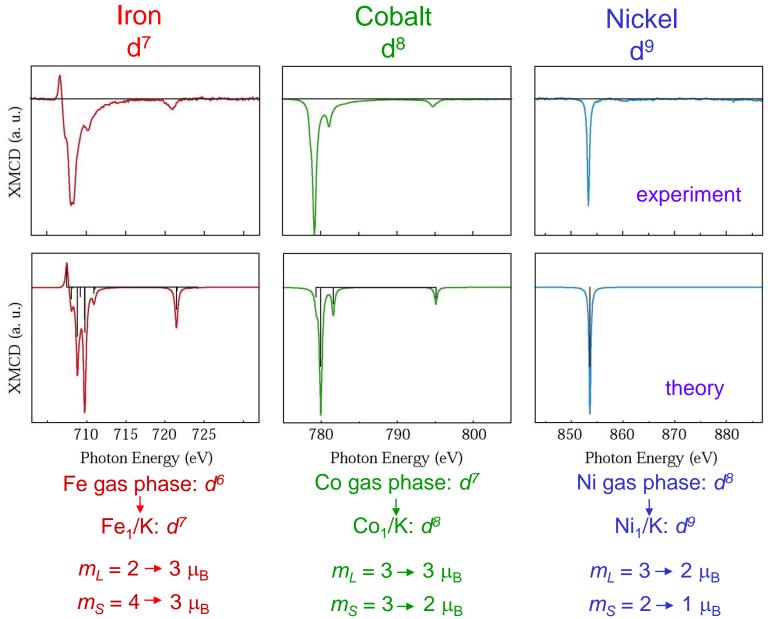


P. Gambardella et al. Phys. Rev. Lett. 88, 047202 (2002)



3d atomic spectra





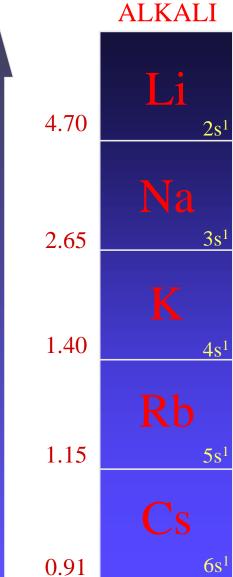
XMCD multiplet calculations: Hartree-Fock atomic wavefunctions, zero-crystal field limit G. Van der Laan and B.T. Thole, Phys. Rev. B **43**, 13401 (1991).



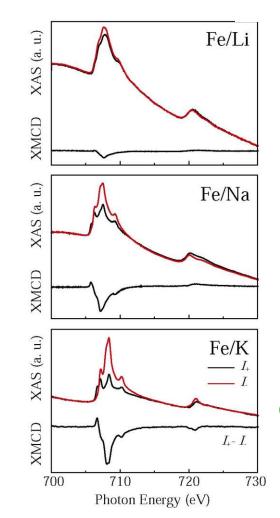
#### Magnetic moment vs. substrate electron density

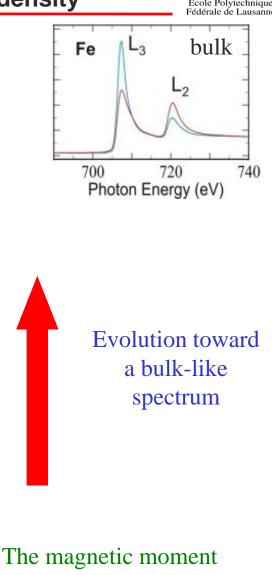






**B** = 7 Tesla, T = 10 K

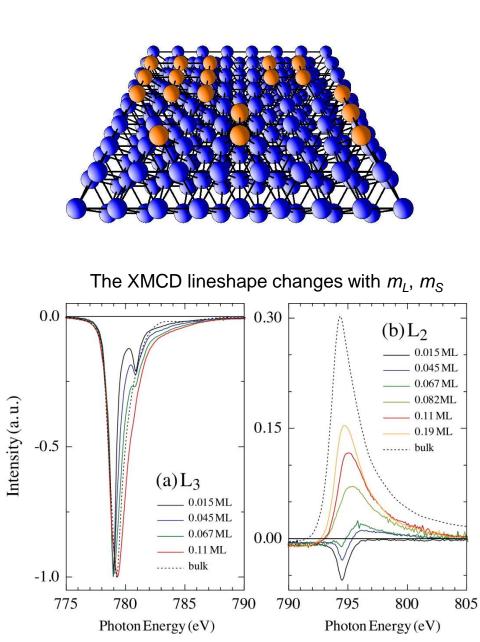


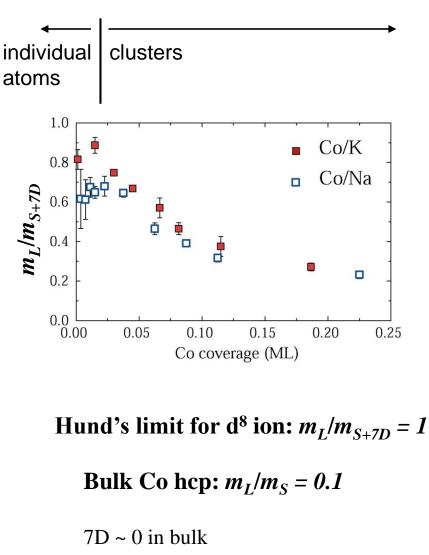


(amplitude of the XMCD signal) decreases increasing the substrate electron density





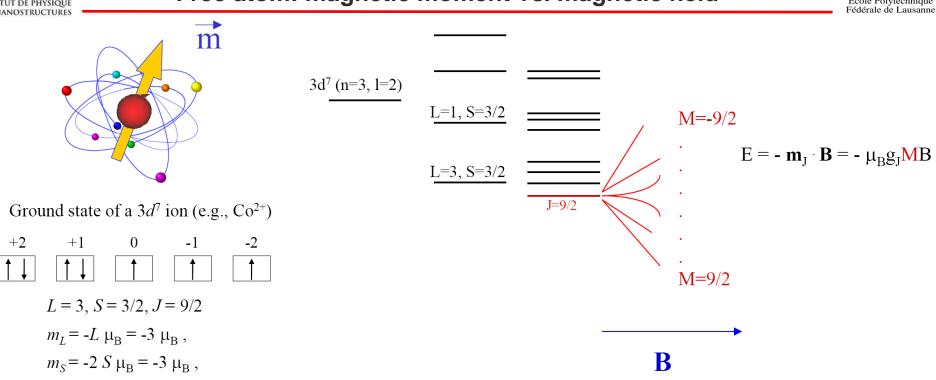




P. Gambardella et al., Phys. Rev. Lett. 88, 047202 (2002)







$$\langle m \rangle = N \frac{\sum_{M=-J}^{J} m_{J} e^{-\frac{\mu_{B} g_{J} B M}{kT}}}{\sum_{M=-J}^{J} e^{-\frac{\mu_{B} g_{J} B M}{kT}}} = N \frac{\sum_{M=-J}^{J} \mu_{B} g_{J} M e^{-\frac{\mu_{B} g_{J} B M}{kT}}}{\sum_{M=-J}^{J} e^{-\frac{\mu_{B} g_{J} B M}{kT}}} = N \mu_{B} g_{J} J B_{J} \left(\frac{\mu_{B} g_{J} J B}{kT}\right)$$

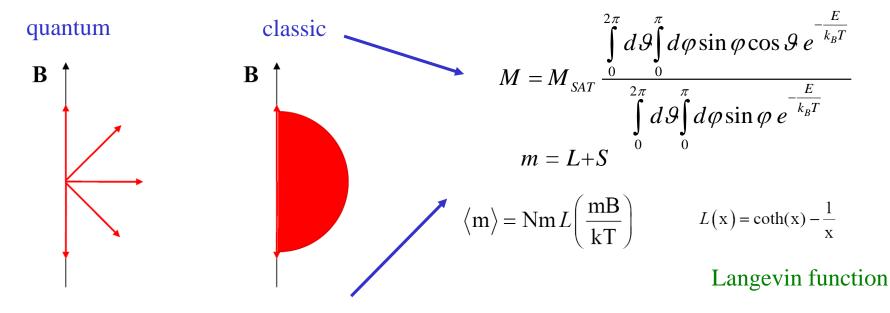
$$B_{J}(\mathbf{x}) = \frac{2\mathbf{J}+1}{2\mathbf{J}} \operatorname{coth}\left(\frac{2\mathbf{J}+1}{2\mathbf{J}}\mathbf{x}\right) - \frac{1}{2\mathbf{J}} \operatorname{coth}\left(\frac{1}{2\mathbf{J}}\mathbf{x}\right)$$

#### **Brillouin** function

P. Gambardella et al., Phys. Rev. Lett. 88, 047202 (2002)

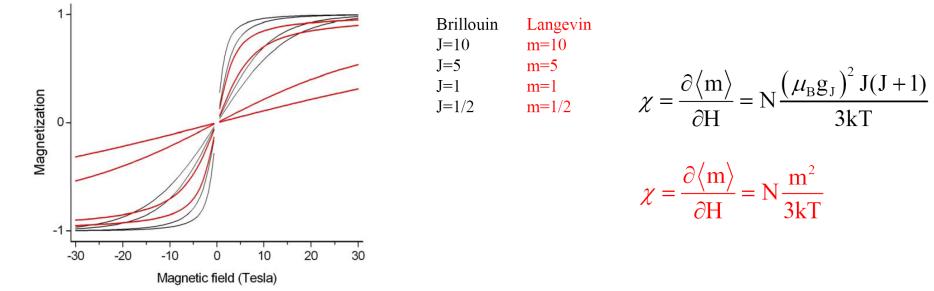






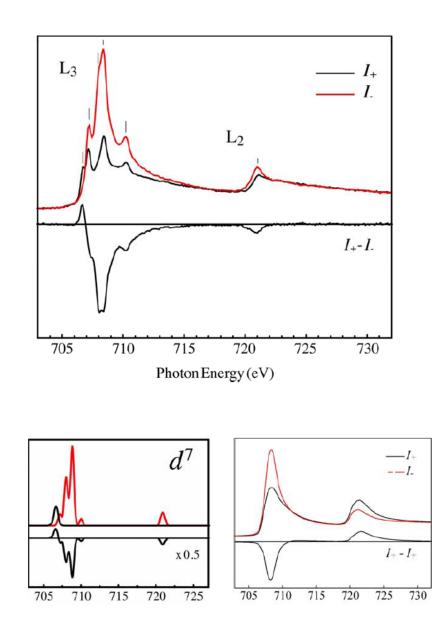
 $E = -m_J \cdot B = -\mu_B g_J MB$ 

 $E = -\mathbf{m}_{I} \cdot \mathbf{B} = - \mathrm{mB}\mathrm{cos}\theta$ 

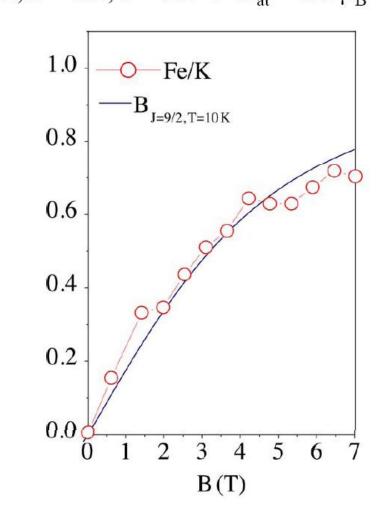








Atomic-like Fe orbitals Fe d<sup>6</sup>  $\rightarrow$  d<sup>7</sup>.  $L = 3, S = 3/2, J = 9/2 \rightarrow m_{at} = 6.6 \mu_{B}$ 



P. Gambardella et al., Phys. Rev. Lett. 88, 047202 (2002)

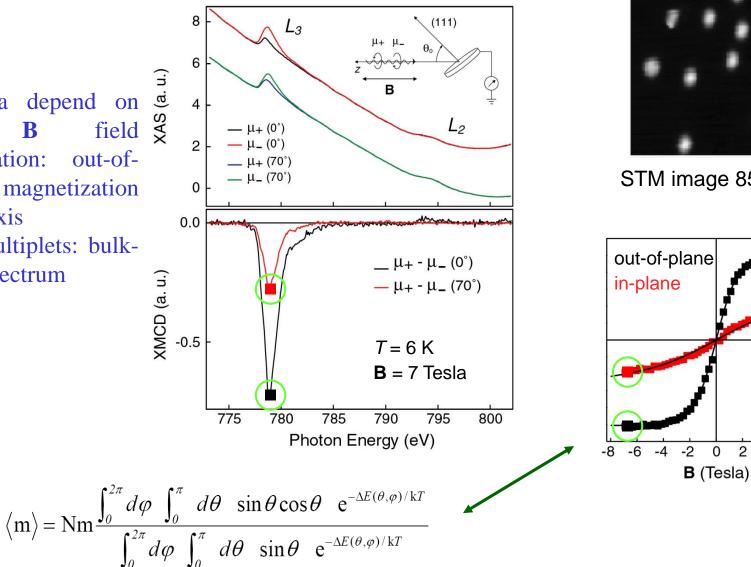


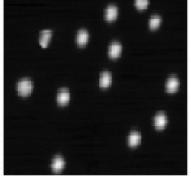


*Magnetization* (a. u.)

#### Spin-orbit interaction between Co wave functions and substrate d-states

- Spectra depend on the **B** field **S** orientation: out-ofplane magnetization easy axis No multiplets: bulk--
- like spectrum





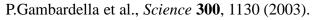
# STM image 85 x 85 Å<sup>2</sup>

0

2

4

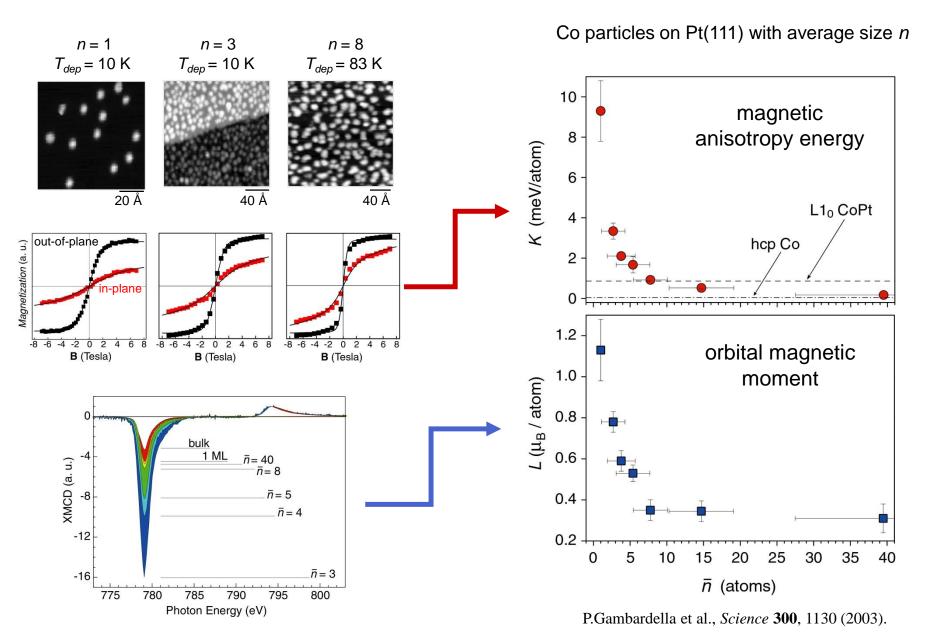
6 8







# Co on Pt(111)



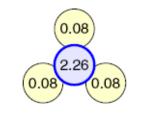


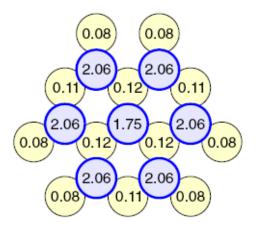


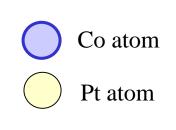
a) CF (C<sub>3v</sub>) is not enough to explain the (former) record MAE -> K ~  $\xi/4 \Delta L$  but  $\Delta L$  is too small b) There is a strong hybridization with the Pt(111) substrate

Local  $\mu_{spin}$  at Co atoms and at substrate atoms for Co clusters of 1–7 atoms

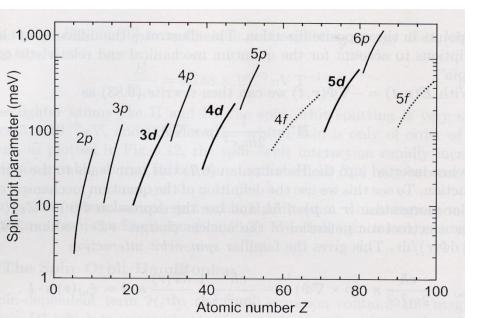
Spin moment induced in the Pt substrate: The induced moment is small but  $\xi_{Pt}$  is large -> the substrate contribute to the MAE







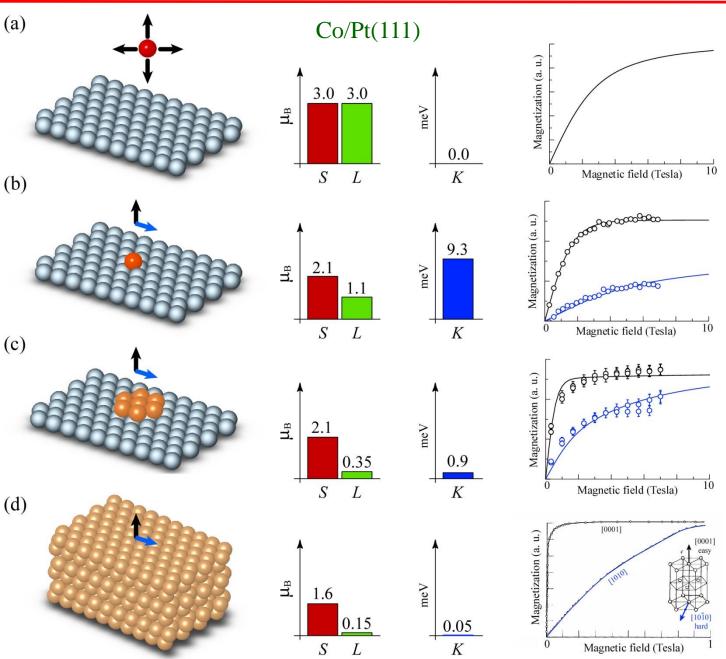
O. Sipr et al., J. Phys.: Condens matter **19**, 096203 (2007).





## Magnetic moments and magnetic anisotropy: from atom to bulk



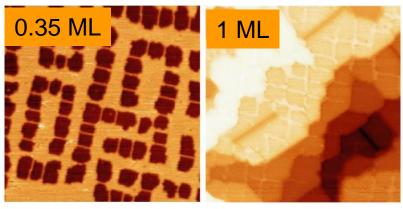


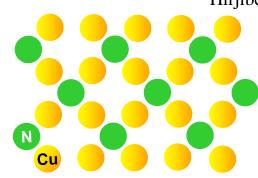


**Insulating substrates** 



### Cu<sub>2</sub>N/Cu(001)





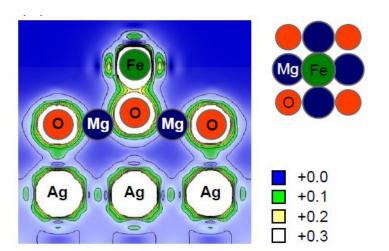
#### Hirjibehedin *et al.*, Science **317**, 1199 (2007)



# 200 Å

Sputtering with N at RT and annealing @ 600 K for 2 min 1 ML thick band gap of 4 eV Ruggiero *et al.*, APL **91**, 253106 (2007)

# **MgO/Ag(100)**

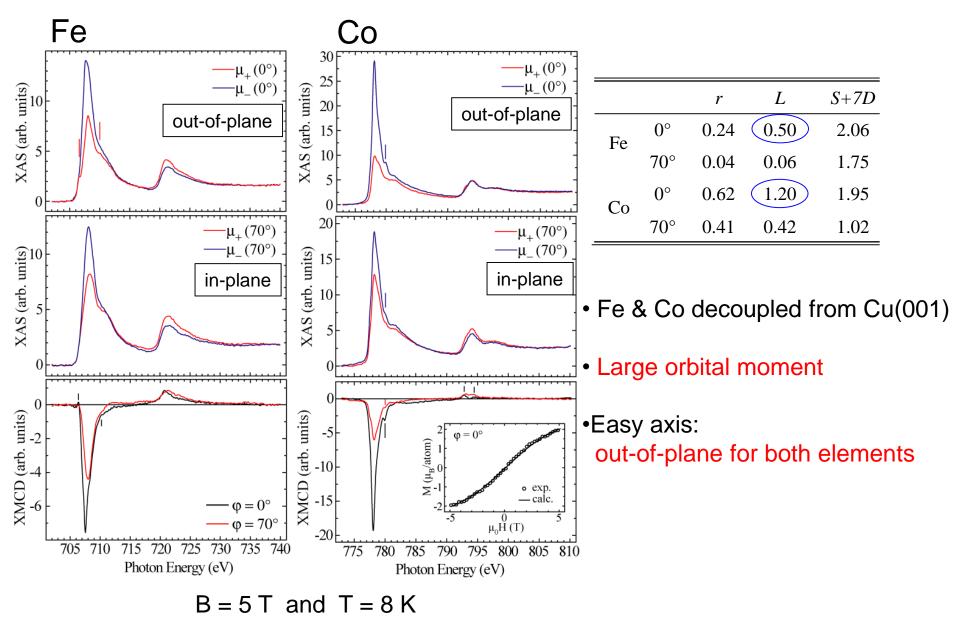


### MgO band gap of 8 eV

S. Schintke, et al. Phys. Rev. Lett. 87, 276801 (2001)



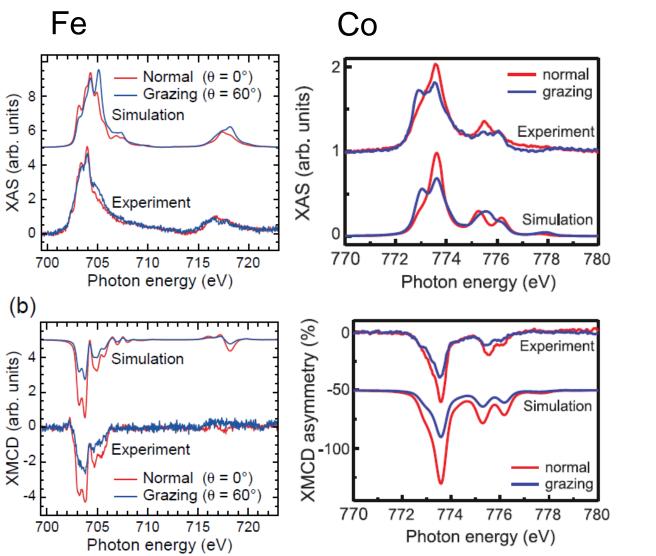




A. Lehnert, *EPFL thesis*  $n^{\circ}$  4411 (2009)







• Fe & Co decoupled from Ag(100): Spectra with multi-peaks

• atomic like orbital moments: •Co -> L = 2.5  $\mu_B$ •Fe -> L= 1.25  $\mu_B$ 

•Easy axis: out-of-plane for both elements

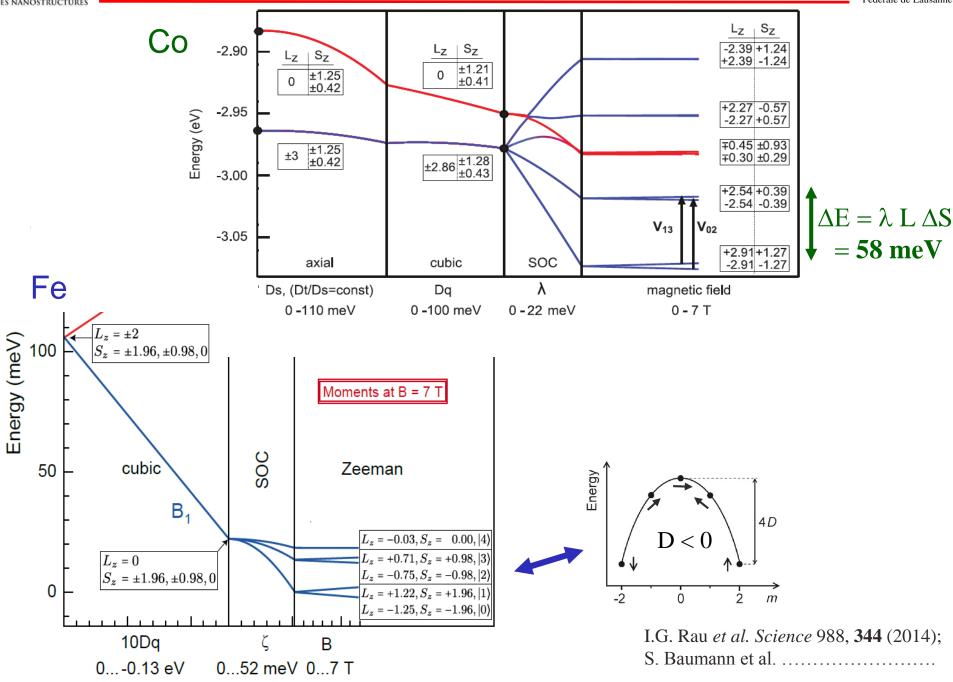
 $B = 7 \ T$  and  $T = 2 \ K$ 

I.G. Rau *et al. Science* 988, **344** (2014); S. Baumann *et al.* Phys. Rev. Lett. **115**, 237202 (2015).



#### Theoretical maximum MAE for Co atoms on MgO/Ag(100)

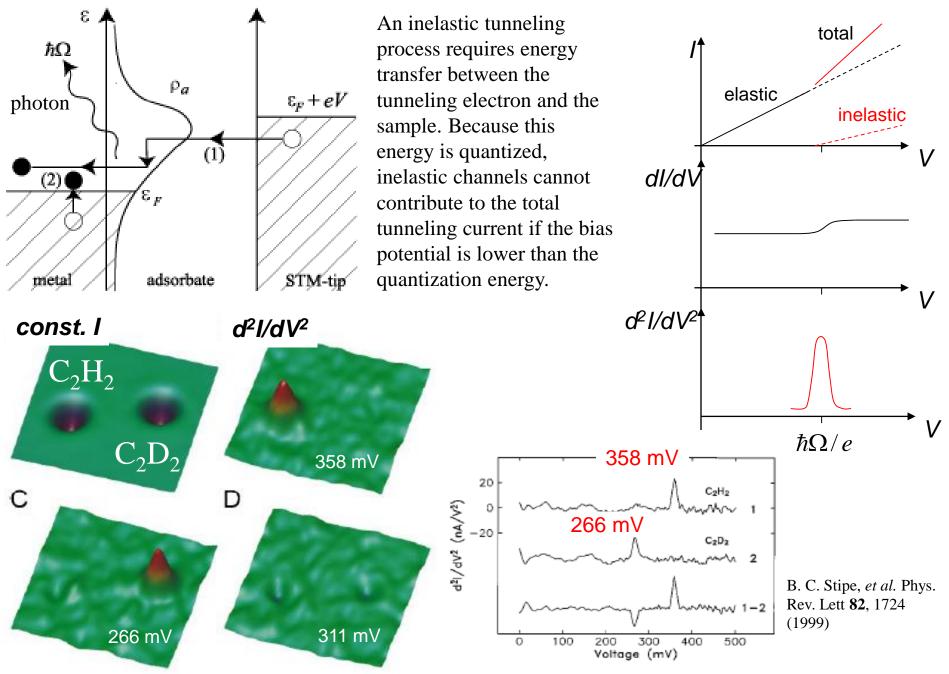






#### Excitation by means of STM







# Spin-flip excitation by means of STM



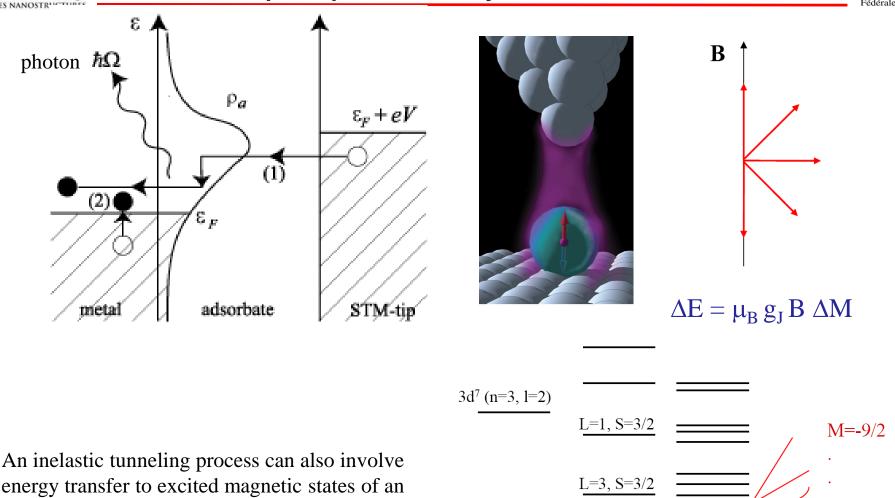
ΔΕ

Ĵ

B

M = 9/2

J=9/2



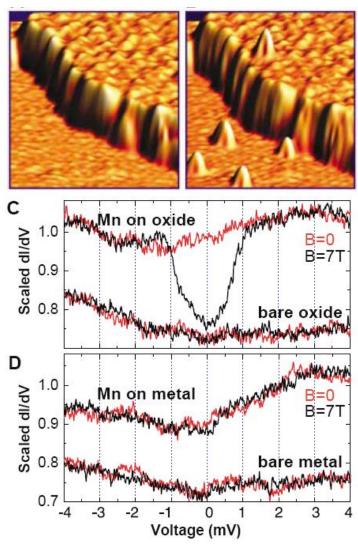
energy transfer to excited magnetic states of an atom (spin-flip). The threshold energy for spin-flip processes depends on the environment of magnetic atoms, that is, the coordination of adjacent atoms and their chemical composition, and the magnetic field.





# $Mn/Al_2O_3/Ni_3Al(111)$

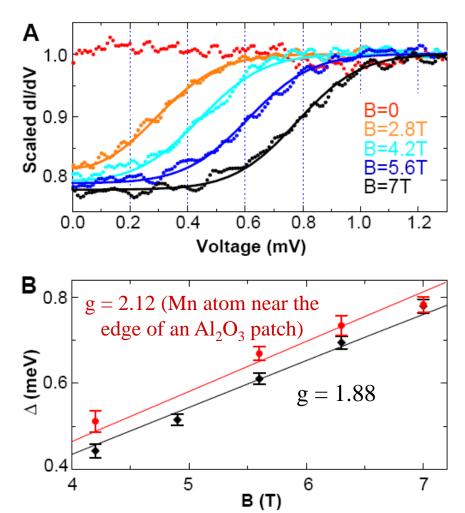




A.J. Heinrich *et al.*, Science **306**, 466 (2004).

Shift of the spin-flip conductance step with magnetic field

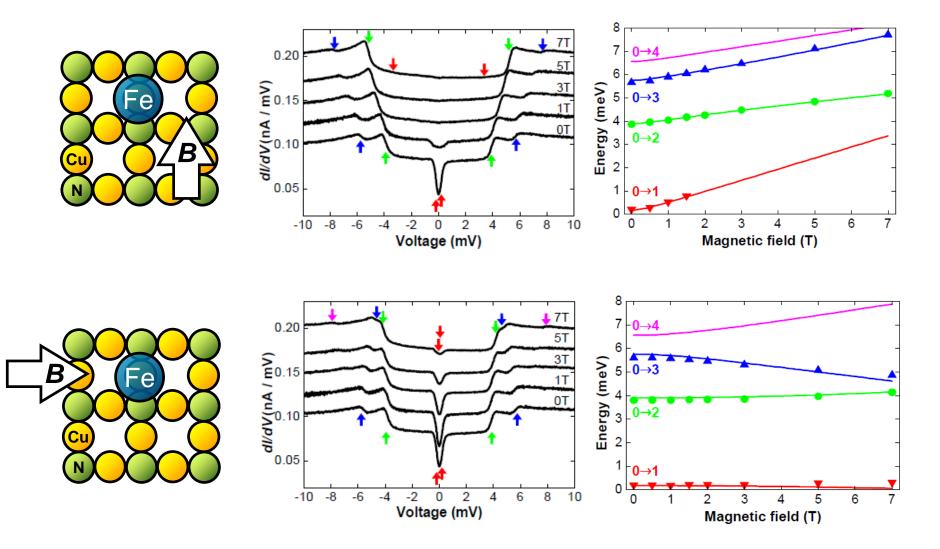
 $\Delta E = g_J \, \mu_B \, B$ 







#### Spectra depend on B field direction -> anisotropy

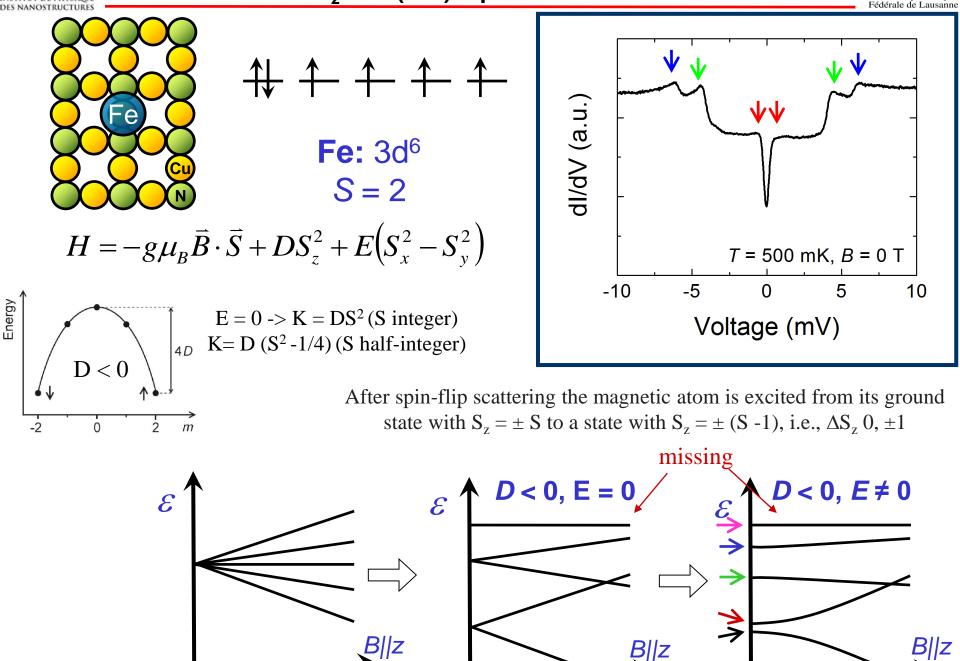


Hirjibehedin *et al.*, Science **317**, 1199 (2007)



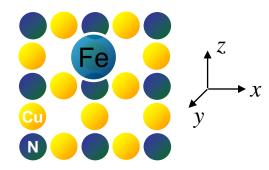
#### Fe/Cu<sub>2</sub>N/Cu(001): spin Hamiltonian











$$H = g\mu_B \vec{B} \cdot \vec{S} + DS_z^2 + E(S_x^2 - S_y^2)$$

$$S = 4\mu_B, D = -1.55 \text{ meV}, E = 0.3 \text{ meV}$$

Calculate the eigenvectors  $|\Psi_i\rangle$  and eigenvalues  $E_i$  of H for a given B

Eigenstate	+2>	<b> +1</b> ⟩	<b> +0</b> ⟩	$ -1\rangle$	I–2>	Eigenvalues
_		<i>B</i> =	0 T			
Ψο	0.697	0	-0.166	0	0.697	-6.93 meV
$\Psi_1$	0.707	0	0	0	-0.707	-6.74 meV
Ψ2	0	0.707	0	-0.707	0	-3.08 meV
Ψ3	0	0.707	0	0.707	0	-0.58 meV
Ψ4	0.117	0	0.986	0	0.117	0.19 meV
		<i>B</i> =	7 T			
Ψo	0.021	0	-0.097	0	0.995	
Ψ1	0.987	0	-0.157	0	-0.036	
Ψz	0	0.402	0	-0.916	0	
Ψ <sub>3</sub>	0	0.916	0	0.402	0	
Ψ4	0.159	0	0.983	0	0.092	

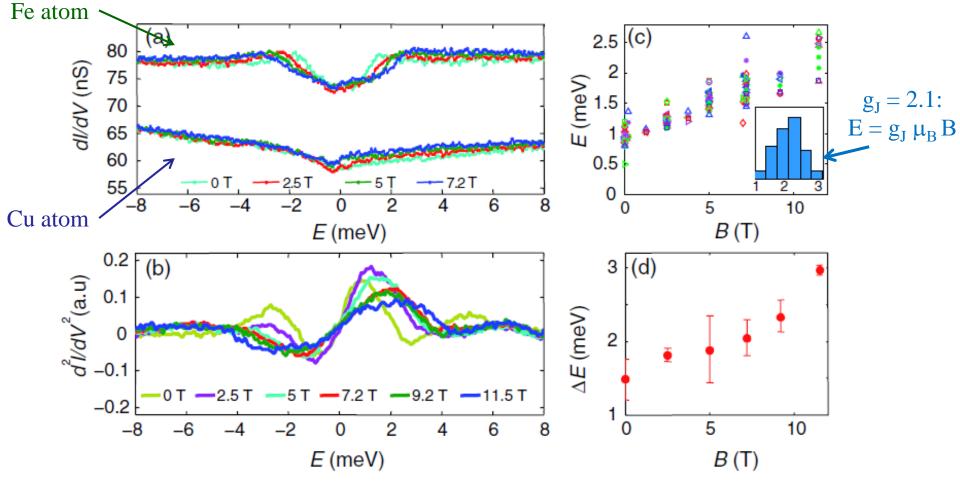
- S integer,  $E \neq 0$  -> quantum tunneling: at B = 0 the ground state ( $\psi_0$ ) has  $S^* = 0$ 

- B splits the states and restore a moment: at  $B = 7T S^* = -2$ 





Conceptually spin-flip excitation should be observed only on atom with localized electrons, but .....



Interaction with the metallic substrate:

- Fe is a d<sup>6</sup> -> L = 2, S = 2, m<sub>J</sub> = 6  $\mu_B$  with  $g_J = 1.5$  but experimetally  $m_J \sim 3.5 \mu_B$  with  $g_J = 2.1$ -  $\tau \sim h/(\Delta E) = 200$  fsec (B = 0 T) -> very short spin-lifetime

A. A. Khajetoorians et al., Phys. Rev. Lett. 106, 037205 (2011)



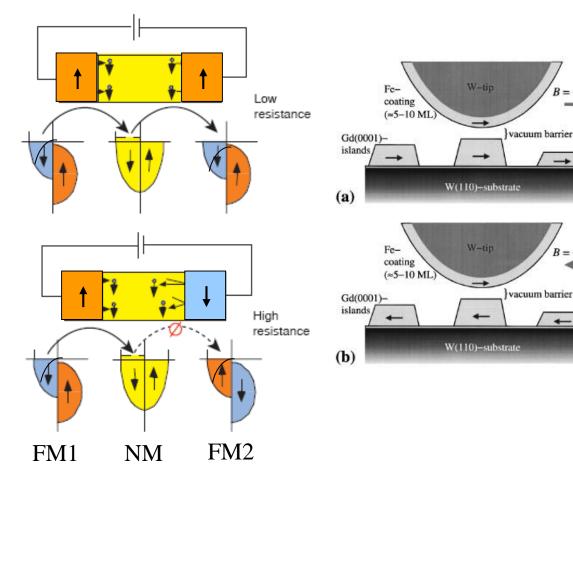
= +4.3 mT

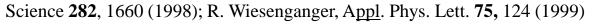
B = -4.3 mT

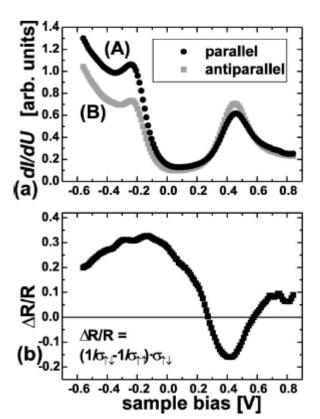
-



# Ferromagnetic (FM) - nonmagnetic (NM) ferromagnetic (FM) junction



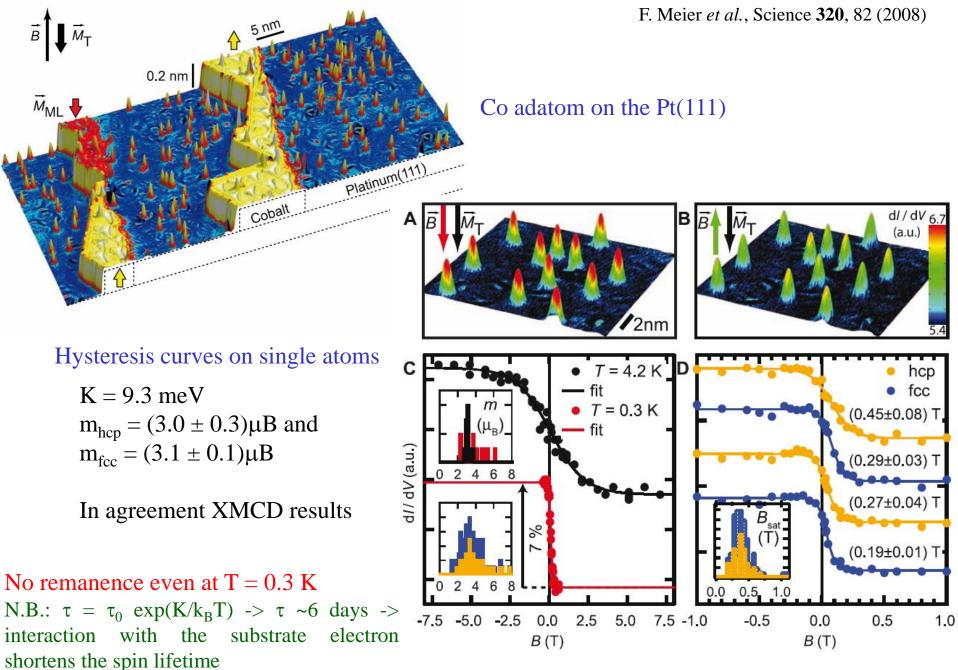






#### Co/Pt(111): spin polarized STM



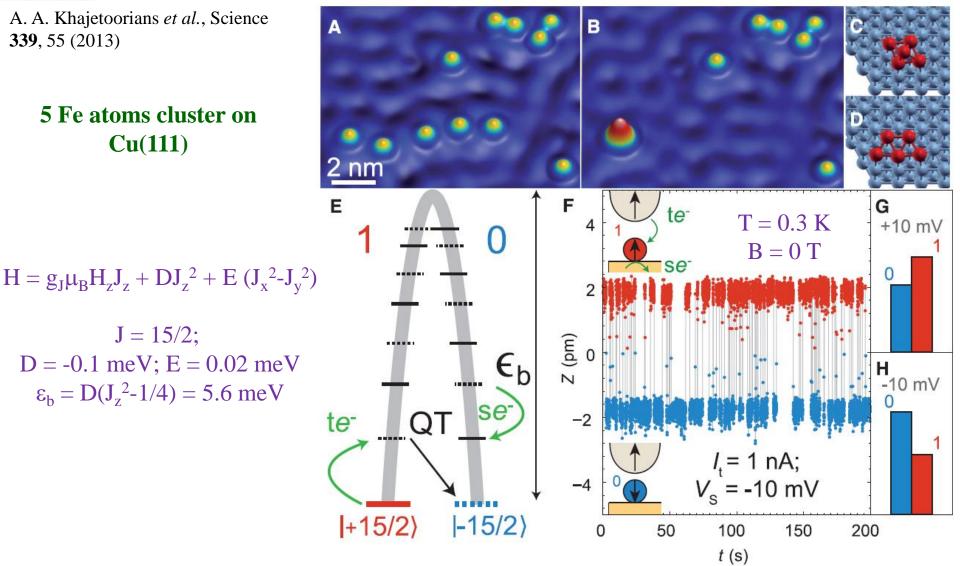




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# Artificial constructed quantum magnet: read for exercise





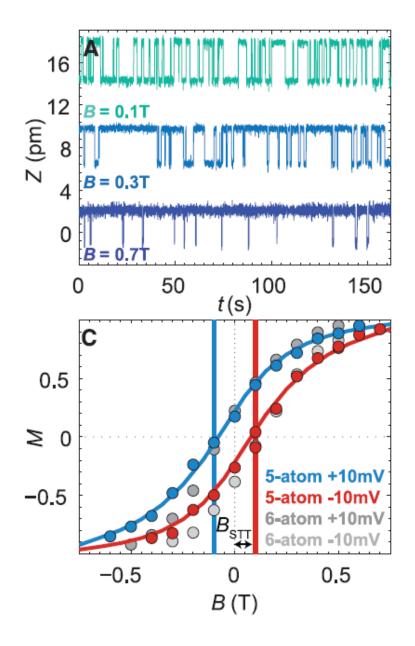
Destabilizing interactions:

- QT (due to E = 0.02 meV)
- spin-flip due to tunneling e<sup>-</sup> (te<sup>-</sup>)
- spin-flip due to conduction e<sup>-</sup> (se<sup>-</sup>)

Without destabilizing interactions  $\epsilon_{\rm b} = 217 \text{ kT } !!!$  $\tau = \tau_0 \exp(\epsilon_{\rm b}/kT) \sim 10^{84} \text{ s } !!!$ 







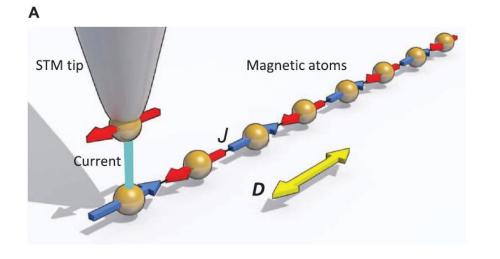
The magnetic field stabilizes one of the two ground states

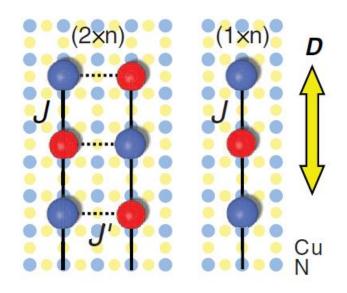
#### Remanence observed at T = 0.3K

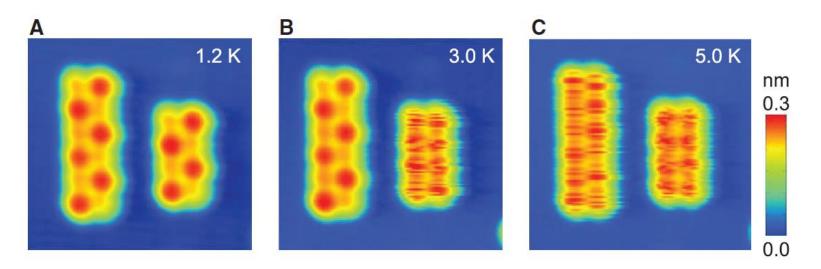
A. A. Khajetoorians et al., Science 339, 55 (2013)









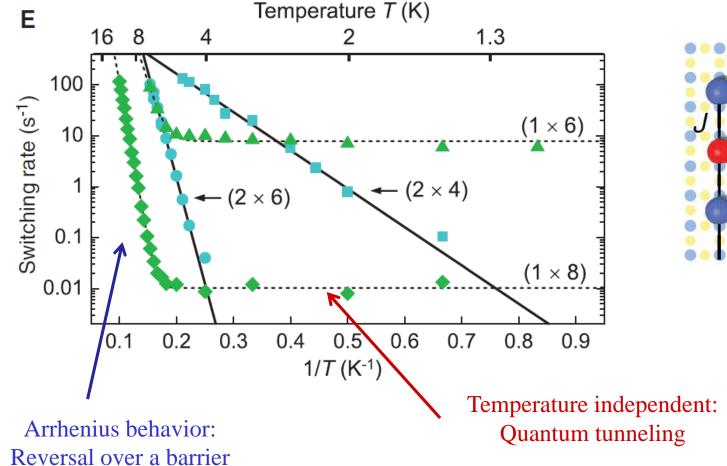


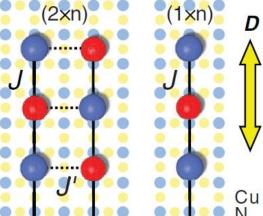
S. Loth et al., Science 335, 196 (2012)



### Antiferromagnetic bits







Experimentally, quantum tunneling is reduced by:

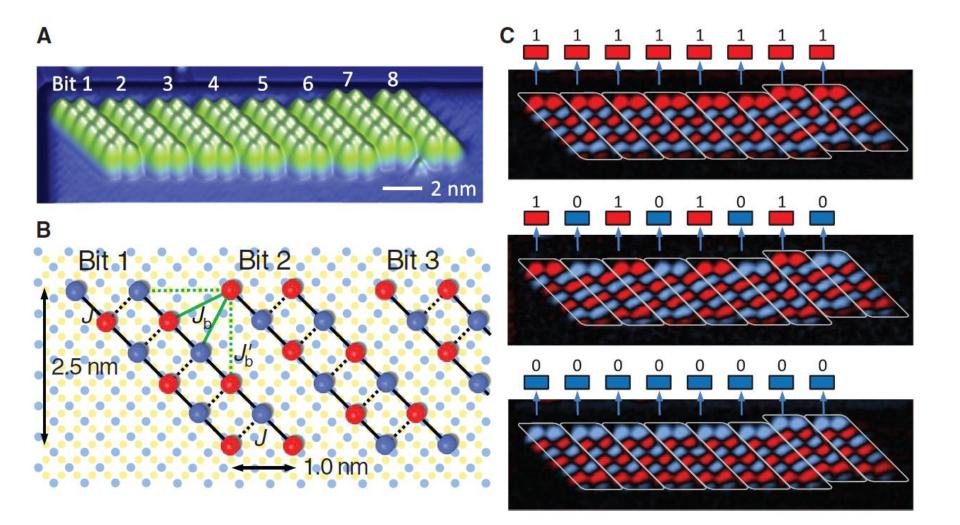
a) increasing the length or

b) by exchange coupling two lines

S. Loth et al., Science 335, 196 (2012)





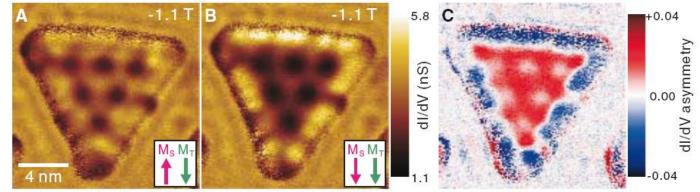


S. Loth *et al.*, Science **335**, 196 (2012)

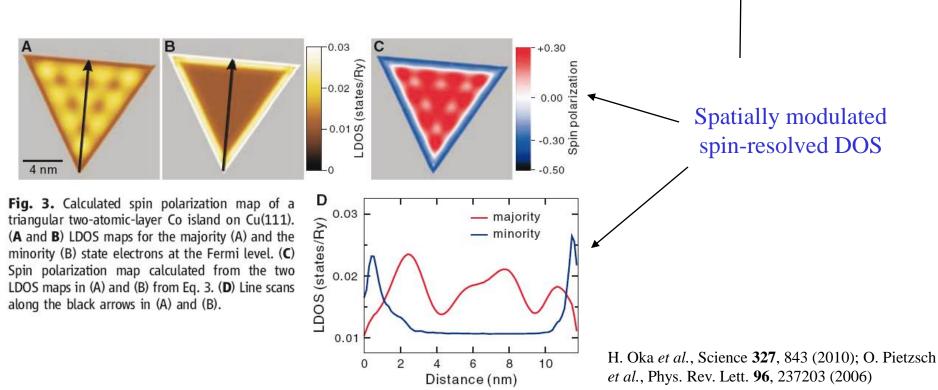




**Fig. 2.** (**A** and **B**) Two *dl/dV* images of the Co island in Fig. 1, the basis for the *dl/dV* asymmetry map in (C). Both images were recorded at B = -1.1 T, but with different magnetization configurations between the magnetic tunneling tip and the Co island: antiparallel (A) and parallel (B). The insets represent the antiparallel (AP) and parallel (P) configurations. V = +0.03 V,  $V_{stab} = +0.5$  V, and I = 1.0 nA, where V is the bias



voltage at which the dl/dV signal is recorded and  $V_{stab}$  is the bias voltage to stabilize the tip before the feedback loop is opened (10). (C) dl/dV asymmetry map calculated using Eq. 1 from the images in (A) and (B).

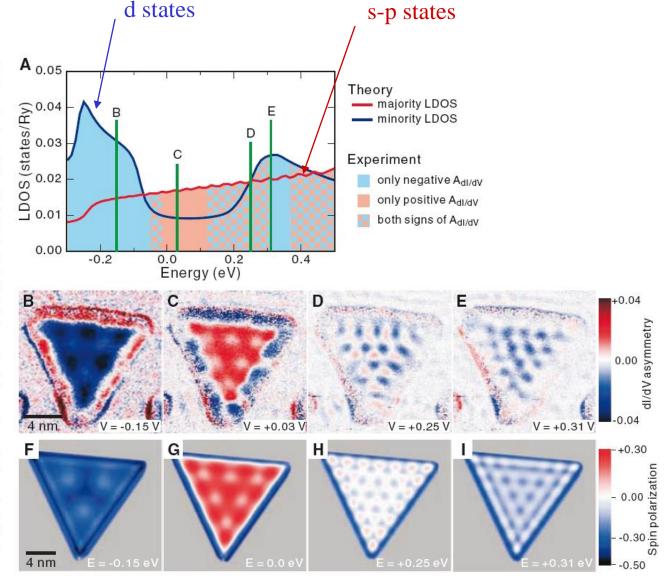






The dominant spin character depends on the energy

Fig. 4. Energy dependences of the measured *dl/dV* asymmetry maps and calculated spin polarization maps of the Co islands. (A) Calculated spin-resolved LDOS of a twoatomic-layer Co film on Cu(111). (B to E) Experimental *dl/dV* asymmetry maps measured on the Co island of Fig. 1. The *dl/dV* asymmetry maps are calculated from two dl/dV images measured at AP and P states from Eq. 1. Measurement conditions of dl/dV images: B = -1.1 T,  $V_{\text{stab}} =$ +0.5 V, / = 1.0 nA. (F to I) Calculated spin polarization maps of the triangular Co island. The spatial dependence of the spin polarization as defined by Eq. 3 is shown by the maps, which are calculated from two LDOS maps for the majority and the minority states. Vertical green lines in (A) correspond to the energy positions where the dl/dV asymmetry maps are obtained. A color map in (A) indicates the energy area where experimental results for the inner part of the Co island show only positive (blue), only negative (red), or both signs (lattice pattem with blue and red) of the dl/dV asymmetry in the dl/dV asymmetry maps.



H. Oka et al., Science 327, 843 (2010)