2: Ultrasound imaging and x-rays

- 1. How does ultrasound imaging work?
- 2. What is ionizing electromagnetic radiation? Definition of ionizing radiation
- 3. How are x-rays produced?

Bremsstrahlung Auger electron

After this course you

- 1. understand the basic principle of ultrasound imaging
- 2. Are able to estimate the influence of frequency on resolution and penetration.
- 3. are capable of calculating echo amplitudes based on acoustic impedance;
- 4. know which parts of the electromagnetic spectrum are used in bio-imaging
- 5. know the definition of ionizing radiation;
- 6. understand the principle of generation of ionizing radiation and control of energy and intensity of x-ray production;

Fund Biolmag 2016

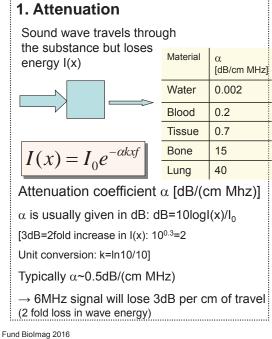
2-1. What are the main fates of US waves in matter?

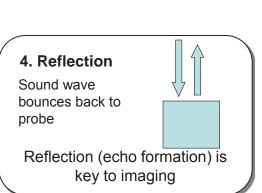
2. Refraction

Sound wave bends

at an oblique angle

as it hits an interface





3. Scatter

Sound wave

directions

dispersed in all

What is the basic principle of US imaging?

The basic principle of imaging using sound waves:

- 1. Emit sound pulse (length [1-5 µs] is a multiple of cycle time 1/f)
- 2. Measure time and intensity of echo
- 3. Reconstruct using known wave propagation velocity c

Distance of tissue boundary from probe (transducer)

Ultrasound: frequency f=1-20MHz (not 20kHz)

transducer =λf]

Sound wave propagation velocity c [c= λf]

- \sim 330m/s (air) = 0.33 mm/ μ s
- ~1.45-1.6 mm/ μ s (tissue) \Rightarrow (1cm~7 μ s) (increases with density ρ , bone ~ 4 mm/ μ s)

Distance=speed x time/2

Fund Biolmag 2016

2-4

What determines the resolution in US imaging?



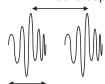
Gap: Separate echoes



Overlap: No Gap, No separate echoes

$$\left\{ \begin{array}{l}
 T_1 = 2x_1/c \\
 T_2 = 2x_2/c
 \end{array} \right\} \Delta T = T_1 - T_2 = 2\Delta x/c$$

min. echo separation, e.g., $\Delta T \ge 2 \Delta t$



Pulse duration $\Delta t = N/f$

Wavelength $\boldsymbol{\lambda}$ determines minimal resolution

- 1. To have defined frequency: Pulse length = N/f $\propto \lambda$
- 2. Separation of return echoes, e.g. $\Delta T > 2$ pulse length
- 1. Resolution
 - increases with f
- 2. Penetration (cf. attenuation)

decreases with f

Fund Biolmag 2016

When does an acoustic echo occur?

Acoustic impedance and reflection ratio

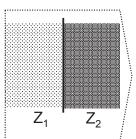
Acoustic impedance Z

Definition:

Z= ρ **c** [kg/m²s=rayls]

Amount of reflected wave energy $I_{ref}=I_0R_I$

At interface between objects with different acoustical properties



Reflection coefficient

$$R_I = \left(\frac{Z_1 - Z_2}{Z_1 + Z_2}\right)^2$$

Tissue	Z (rayls)				
Air	0.0004 × 10 ⁶				
Lung	0.18×10^{6}				
Fat	1.34×10^{6}				
Water	1.48×10^{6}				
Kidney	1.63×10^{6}				
Blood	1.65×10^{6}				
Liver	1.65×10^{6}				
Muscle	1.71×10^{6}				
Skull bone	7.8×10^{6}				

Probability of reflection + transmission is = 1:

Transmission

$$T_I = 1 - R_I$$

Fund Biolmag 2016

2-6

What are the reflection coefficients R_I between tissues?

R _I	Fat	Muscle	Skin	Brain	Liver	Blood	Cranial bone	Plexi- glass
Water	0.047	0.02	0.029	0.007	0.035	0.007	0.57	0.35
Fat		0.067	0.076	0.054	0.049	0.047	0.61	0.39
Muscle			0.009	0.013	0.015	0.02	0.56	0.33
Skin				0.022	0.006	0.029	0.56	0.32
Brain					0.028	0.00	0.57	0.34
Liver						0.028	0.55	0.32
Blood							0.57	0.35
Cranial bone								0.29



Dolphin fetus
Fund Biolmag 2016

Reflection by solid material
e.g. bone-tissue interface
⇒ Shadow formation: ~45% of energy transmitted

100%

(T_I=1-R_I)

2

2-2. What is the optimal choice of US frequency?

SNR

Resolution

Resolution:

 Δx decreases with increasing frequency f : $\infty 1/f$

⇒ Resolution ∞ f

SNR:

Signal returned from an echo-generating tissue interface at distance x from transducer

$$S(f,\alpha,x) = S_0 e^{-\alpha k f 2x} R_{I_{\text{constant}}}$$
 is constant

f: US frequency (experimental parameter)

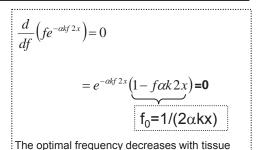
α: attenuation coefficient (tissue parameter)

Find the optimal f ...

⇒ Maximize f·S Maximum is where derivative with respect to f is zero

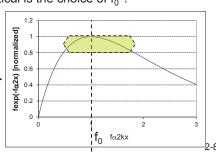
 $\frac{d(fS(f,\alpha,x))}{df} = R_I S_0 \frac{d}{df} f e^{-\alpha k f 2x}$

Fund Biolmag 2016



How critical is the choice of f₀?

depth and with increasing absorption



Ex. 3-D US Imaging & Contrast agents

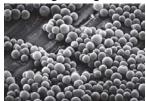
3D US Physical Principle:

- 1. the transducer is moved during exposure (linear shift, swinging, rotation)
- 2. received echoes are stored in the memory
- 3. the image in the chosen plane is reconstructed mathematically





Contrast agents: gas-filled Bubbles



Gas: most contrast (plus resonance and higher harmonic imaging) (see tiny $Z \rightarrow$ total reflection, $R_1 \sim 1$)

How can Ultrasound detect moving blood?

Doppler effect

Motion (Doppler): Frequency shift f_D of moving tissue, results in shifted US frequency (demodulation for detection) (where is this also used?)

Doppler frequency shift f_D

$$f_D = \frac{2f_0 v_0 \cos \alpha}{c}$$

- c: speed of US, e.g. 1500 m/s v_0 : speed of source, e.g. 50 cm/s
- f_0 : frequency of moving source, e.g. 5MHz
- α: Rel. angle at which blood is moving

Example:

 $f_D = 2.5.10^6 \text{ [Hz] } 0.5 \text{ [m/s]/} 1500 \text{ [m/s]}$

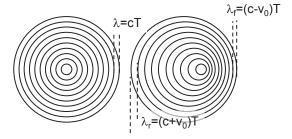
- ~ 3kHz
- $\sim 0.05\%$ of f_0

Fund Biolmag 2016

stationary

Source moving with v₀

In a period T, source moves closer by v₀T





2-11

2-3. Basis of x-ray imaging

useful relationships Electromagnetic radiation

 $\mathbf{c} = \lambda \mathbf{v}$ (c = speed of light = 3.10^8 m/s)

 $E = hv = hc/\lambda$ (h = Planck's Constant)

h= $2\pi \cdot 10^{-34}$ Js

 $= 4.10^{-18} \text{keVs}$

1eV = energy of e- in acquired in 1V electric field

 $E = hc/\lambda$

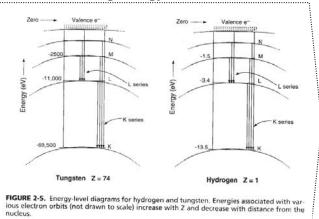
= 1.2keV/nm

2-13

With which elements of matter does EM radiation interact mainly?

(in imaging mainly with electrons)

Electron binding energy



Binding energy

- 1. decreases with shell distance
- increases with Z (Why?)

Lowest K-shell binding e-energy:

 $E_{K}^{min} = 13.6 eV (^{1}H)$

 $h_V > E_K^{min}$: ionizing

 $h_V < E_K^{min}$: non-ionizing

Electron (some useful constants)

$$m_e$$
 = mass = $9 \cdot 10^{-31}$ kg
 q_e = charge = $1.6 \cdot 10^{-19}$ C (As)
Rest energy $m_e c^2$ = 511 keV

Fund Biolmag 2016

Ionizing radiation is above 13.6 eV

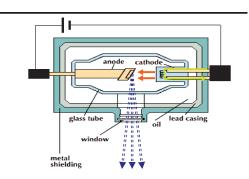
2-1

2-4. How are x-rays generated (scheme)?

Negatively charged cathode = electron source Electrical current (filament current) heats up the cathode (why is that necessary?) Electrons are liberated and accelerated by electric field (Energy of e = q\Delta V)

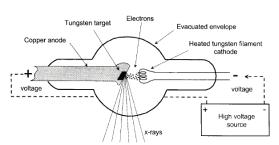
Anode = metal target (tungsten)
accelerated electrons hit anode ⇒
generate X-rays

(tube current with voltage difference up to $150\ kV$)



Intensity of beam = Power/Area

- 1. Number of X-rays (proportional to tube current)
- Energy of X-rays hν (proportional to voltage)



2-16

Emission of x-rays I: What is Bremsstrahlung?

Consider the interaction of e- with stationary atom as collision :

 $p_i = p_f + p_{photon}$

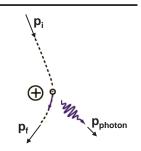
Coulomb:

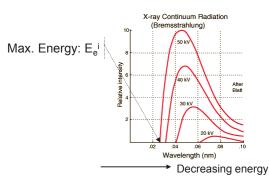
a ~
$$q_e Z/m_e r^2$$

 $P_{Brems} = q_e^2 a^2/6\pi\epsilon_0 c^3$

No info on directionality of radiation

(but maximum energy is defined, how?)





Elastic scattering:

Probability ~ Z²/E_{e-}²

Inelastic scattering: v release

Probability ~ Z²

High Z: Tungsten is a good target

Fund Biolmag 2016

2-17

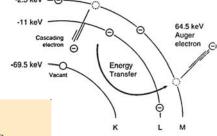
Emission of x-rays II: What are Characteristic (fluorescent) X-rays?

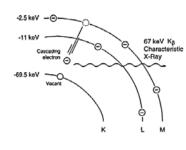
Impacting e-liberates inner shell e-

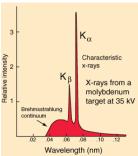
- 1. Atom is excited (higher energy state)
- 2. Vacancy
- 3. Filled by outer shell electron (cascading)
- 4. Emission of characteristic x-ray

Auger emission

The excited atom can also reduce energy by liberating an additional e- (Auger e-):







2-18

Fund Biolmag 2016