

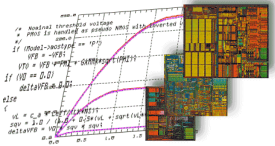
Tunneling Mechanism

Intrinsic Gate Current

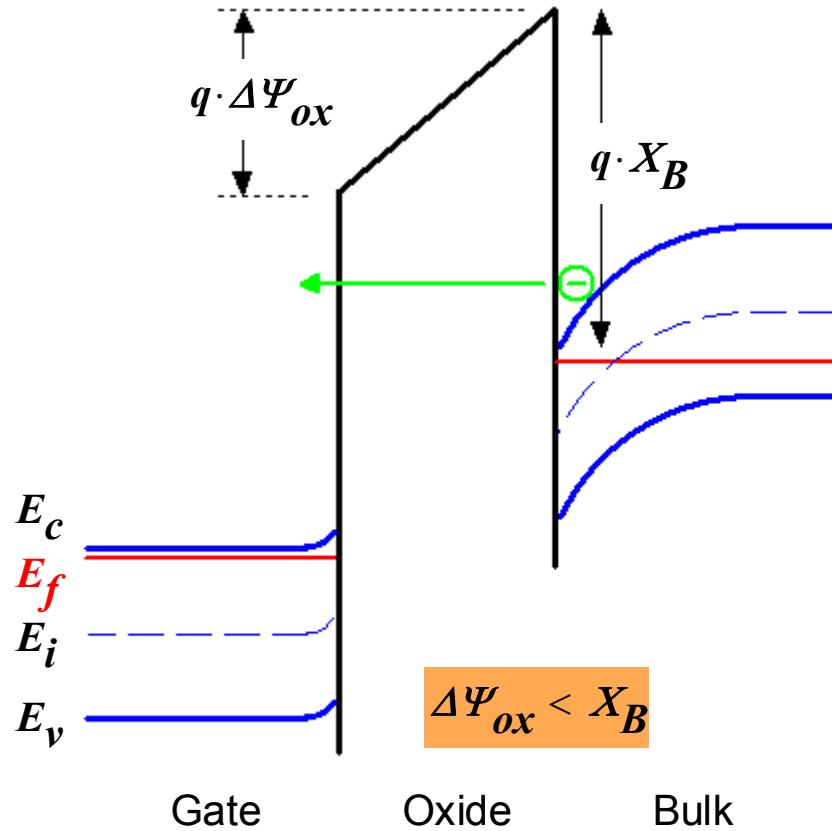
- Intrinsic Gate Current in Inversion
- Gate Current Partitioning
- Gate Current in Accumulation

G/S & G/D Overlap Currents

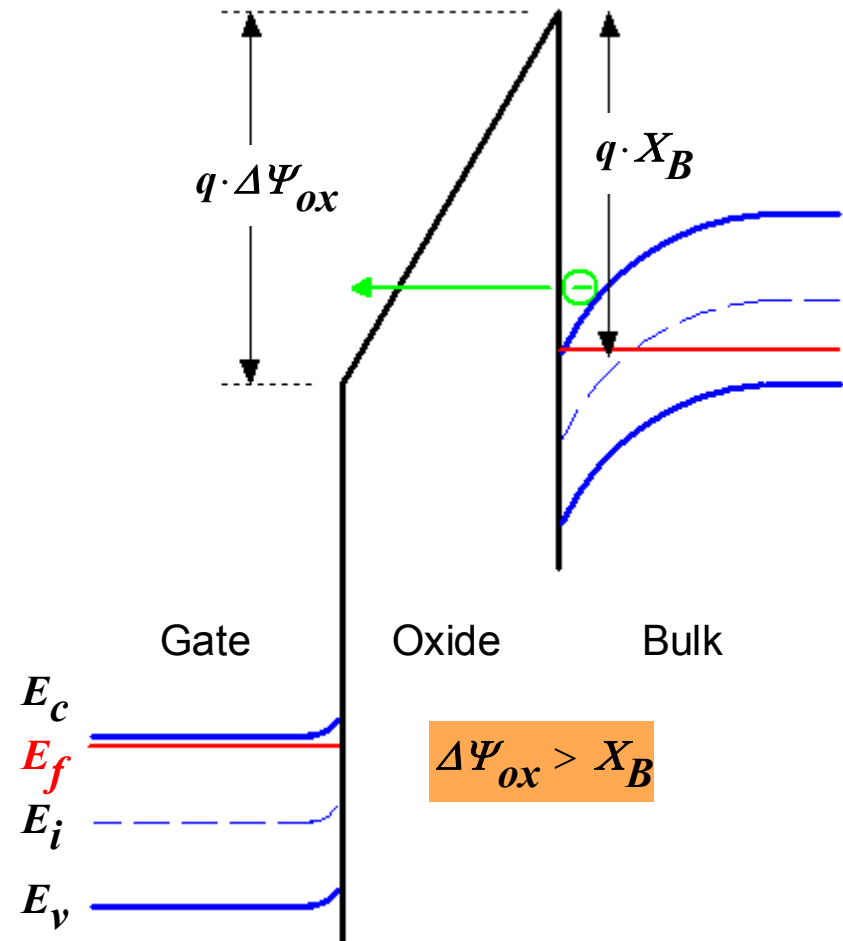
Total Gate Current

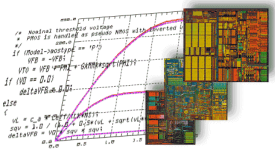


Direct Tunneling



Fowler-Nordheim Tunneling

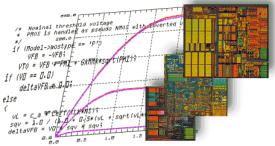




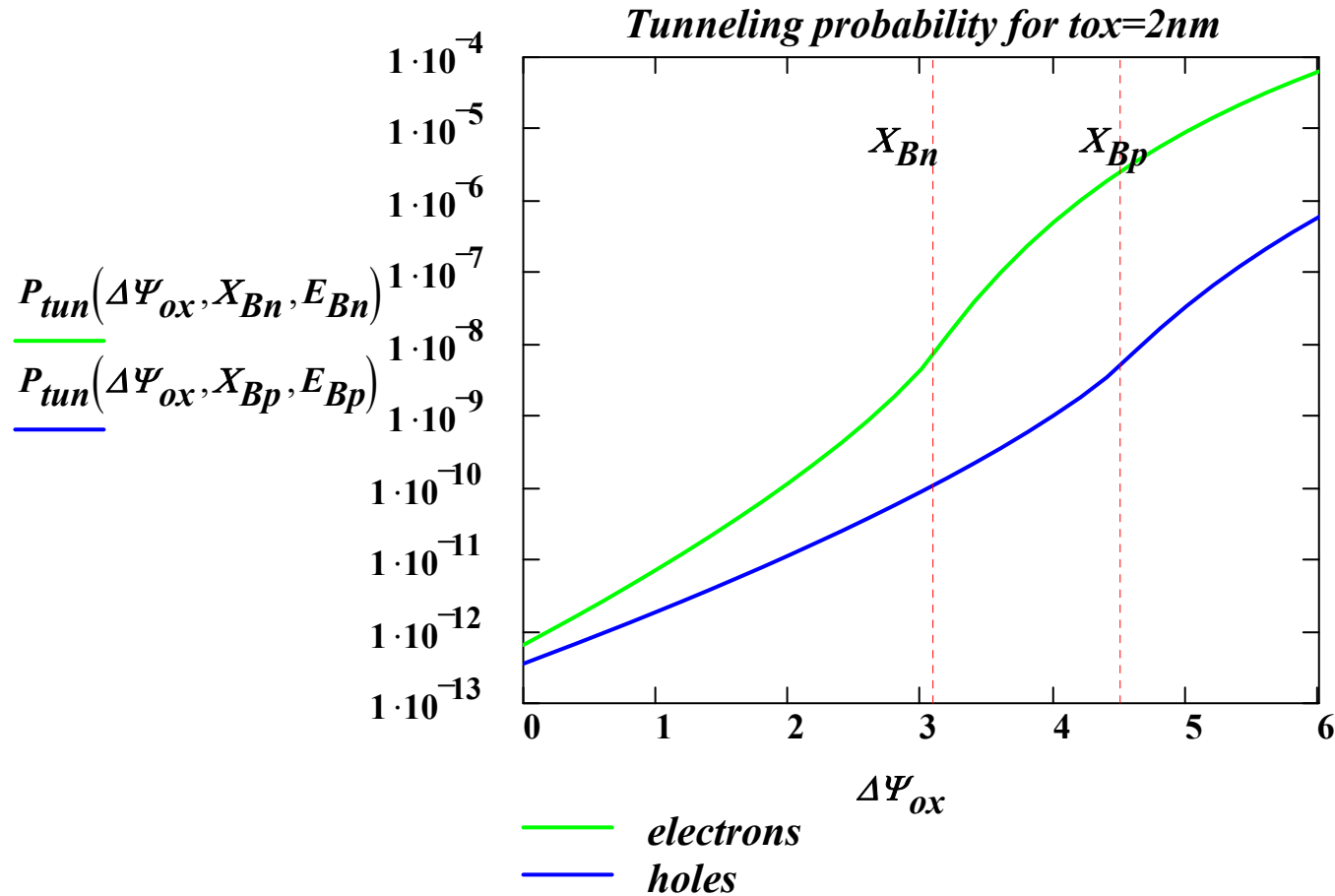
Tunneling Probability

$$P_{tun}(\Delta\Psi_{ox}, X_B, E_B) = \begin{cases} e^{-\frac{E_B \cdot t_{ox}}{X_B} \left(\frac{1}{1 + \sqrt{1 - \frac{|\Delta\Psi_{ox}|}{X_B}}} + \sqrt{1 - \frac{|\Delta\Psi_{ox}|}{X_B}} \right)} & \text{if } |\Delta\Psi_{ox}| < X_B \quad \text{(direct tunneling)} \\ e^{-\frac{E_B \cdot t_{ox}}{|\Delta\Psi_{ox}|}} & \text{otherwise} \quad \text{(FN tunneling)} \end{cases}$$

where X_B is the Si-SiO₂ barrier height and E_B is a characteristic electric field.



Tunneling Probability



electrons:

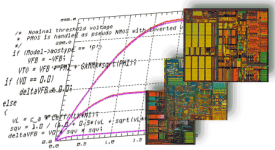
$$X_{Bn} = 3.1 V$$

$$E_{Bn} = 29 \frac{V}{nm}$$

holes:

$$X_{Bp} = 4.5 V$$

$$E_{Bp} = 43 \frac{V}{nm}$$



EKV3.0: Gate Current Modeling

Intrinsic Gate Current in Inversion

1/3

Gate Current Density :

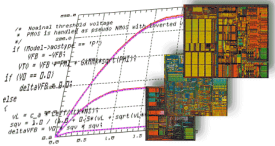
$$J_{gc} = \frac{K_G}{\varepsilon_{ox}} \cdot \frac{\Delta\Psi_{ox}}{t_{ox}} \cdot Q_i \cdot P_{tun}(\Delta\Psi_{ox}, X_B, E_B) \quad [pA / \mu m^2]$$

Voltage Drop across the Oxide :

$$\Delta\Psi_{ox} = \frac{Q_g}{C_{ox}} = \frac{V_G - \Phi_{ms} - \Psi_s}{\frac{1}{2} + \sqrt{\frac{1}{4} + \frac{V_G - \Phi_{ms} - \Psi_s}{\Gamma_g^2}}} = \frac{V_G - \Phi_{ms} - \Psi_P + \frac{-Q_i}{n_q \cdot C_{ox}}}{\frac{1}{2} + \sqrt{\frac{1}{4} + \frac{V_G - \Phi_{ms} - \Psi_P + \frac{-Q_i}{n_q \cdot C_{ox}}}{\Gamma_g^2}}}$$

- in normalised form :

$$\Delta\psi_{ox} = \frac{v_g - \phi_{ms} - \psi_p + 2 \cdot q}{\frac{1}{2} + \sqrt{\frac{1}{4} + \frac{v_g - \phi_{ms} - \psi_p + 2 \cdot q}{\gamma_g^2}}}$$



Total Intrinsic Gate Current :

$$I_{GC} = W \int_0^L J_{gc} dx = I_{G0} \cdot \int_0^1 q \cdot \Delta\psi_{ox} \cdot P_{tun} d\xi$$

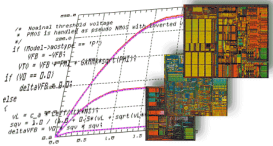
with $I_{G0} = 2 \cdot n_q \cdot K_G \cdot \frac{W \cdot L}{t_{ox}} \cdot U_T^2$ and $\xi = \frac{x}{L}$

- linear expansion of $q \cdot \delta\psi_{ox}$ and P_{tun} around $\xi = 0$, then integrate over ξ :

$$\frac{I_{GC}}{I_{G0}} = i_{GC} \approx i_{go} \cdot \int_0^1 (1 + a \cdot \xi) \cdot e^{b \cdot \xi} d\xi \approx i_{go} \cdot \frac{2 + a}{2 - b}$$

where i_{go} , a and b are evaluated at source ($q = q_s$) :

$$i_{go} = q_s \cdot \Delta\psi_{ox} \cdot P_{tun} \quad a = \frac{dq}{d\xi} \cdot \left(\frac{1}{q} + \frac{1}{\Delta\psi_{ox}} \cdot \frac{d\Delta\psi_{ox}}{dq} \right) \quad b = \frac{d}{d\xi} \ln(P_{tun}(\xi))$$



Current Partitioning

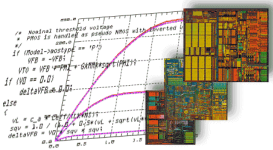
- Gate-to-channel current I_{GC} is to be partitioned into gate-to-source and gate-to-drain currents I_{GS} and I_{GD} , respectively
- 1st-order perturbation approximation :
charge distribution along the channel is not changed significantly by the gate current

$$I_{GS} = W \cdot \int_0^L \left(1 - \frac{x}{L}\right) \cdot J_{gc} dx \qquad I_{GD} = W \cdot \int_0^L \frac{x}{L} \cdot J_{gc} dx$$

- then :

$$\frac{I_{GS}}{I_{G0}} = i_{GS} \approx i_{go} \cdot \int_0^1 (1 - \xi) \cdot (1 + a \cdot \xi) \cdot e^{b \cdot \xi} d\xi \approx \frac{i_{go}}{2} \cdot \frac{3 + a}{3 - b}$$

$$\frac{I_{GD}}{I_{G0}} = i_{GD} = i_{GC} - i_{GS}$$



EKV3.0: Gate Current Modeling

Intrinsic Gate Current in Accumulation

1/1

NMOS :

- N+ gate: accumulation layer of electrons
- P- bulk: accumulation layer of holes

PMOS :

- P+ gate: accumulation layer of holes
- N- bulk: accumulation layer of electrons

Oxide energy barrier is higher for holes than for electrons \Rightarrow electron tunneling is dominant

$$J_{gb} = \frac{K_G}{\epsilon_{ox}} \cdot \frac{\Psi_{ox}}{t_{ox}} \cdot Q_g \cdot P_{tun}(\Delta\Psi_{ox}, X_B, E_B)$$

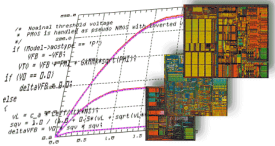
$$Q_g = \frac{\epsilon_{ox}}{t_{ox}} \cdot \Delta\Psi_{ox}$$

$$I_{GB} = -K_G \cdot \frac{W \cdot L}{t_{ox}^2} \cdot \Delta\Psi_{ox}^2 \cdot P_{tun}$$

$$J_{gb} = \frac{K_G}{\epsilon_{ox}} \cdot \frac{\Psi_{ox}}{t_{ox}} \cdot (-Q_b) \cdot P_{tun}(\Delta\Psi_{ox}, X_B, E_B)$$

$$-Q_b = Q_g + Q_{ox} = \frac{\epsilon_{ox}}{t_{ox}} \cdot \Delta\Psi_{ox} + Q_{ox}$$

$$I_{GB} = -K_G \cdot \frac{W \cdot L}{t_{ox}^2} \cdot \Delta\Psi_{ox} \cdot \left(\Delta\Psi_{ox} + \frac{Q_{ox}}{C_{ox}} \right) \cdot P_{tun}$$



EKV3.0: Gate Current Modeling

Intrinsic Gate Currents

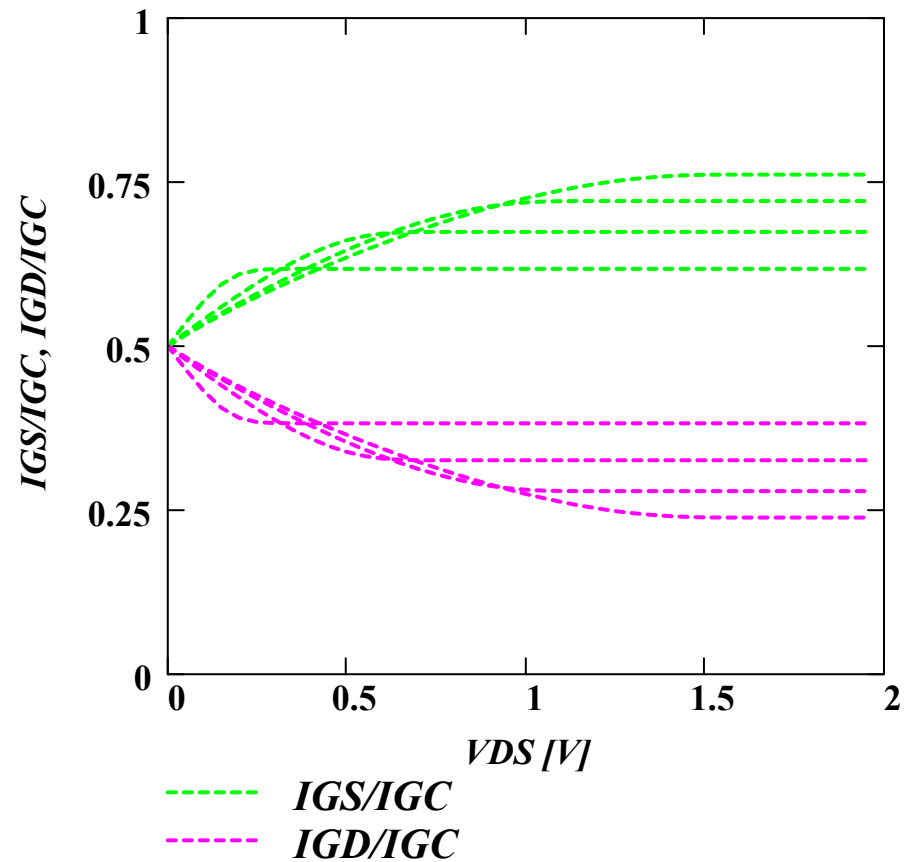
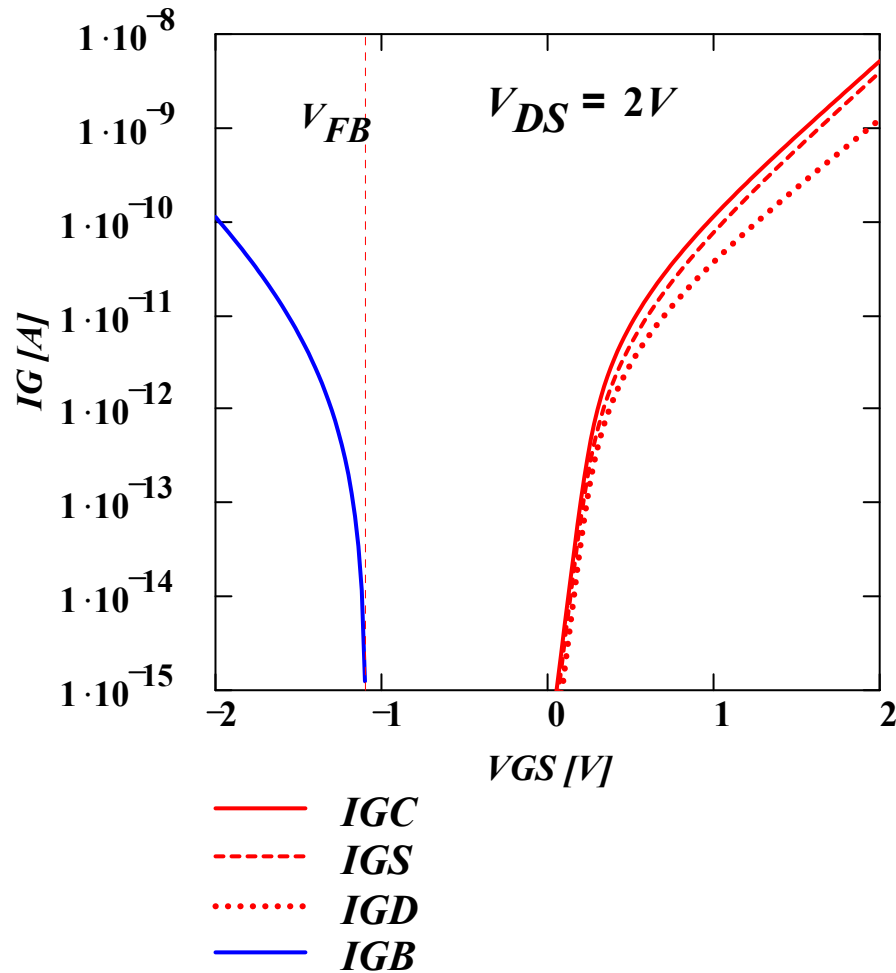
$W = 10 \mu m$

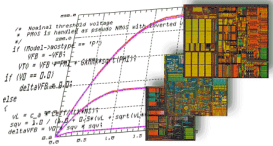
$L = 0.6 \mu m$

$t_{ox} = 2 nm$

$\Gamma_b = 0.39\sqrt{V}$

$\Gamma_g = 5.0\sqrt{V}$





EKV3.0: Gate Current Modeling

Source/Gate & Drain/Gate Overlap Currents

1/2

S/G & D/G Overlap Simplified Characteristics :

- D/G & S/G flatband voltage :

$$V_{FB.ov}$$

- D/G & S/G equivalent oxide thickness :

$$t_{ox.ov}$$

- polysilicon gate modulation factor :

$$\Gamma_{g.ov} = \sqrt{2 \cdot q \cdot \epsilon_{si} \cdot N_g} \cdot \frac{t_{ox.ov}}{\epsilon_{ox}}$$

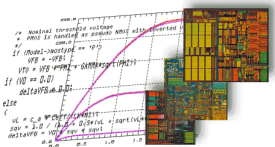
- D & S diffusion modulation factor :

$$\Gamma_{s.ov} = \Gamma_{d.ov} = \sqrt{2 \cdot q \cdot \epsilon_{si} \cdot N_{LDD}} \cdot \frac{t_{ox.ov}}{\epsilon_{ox}}$$

$$\Delta\Psi_{ox.ov}(V_{GS}) = \begin{cases} \frac{V_{GS} - V_{FB.ov}}{\frac{1}{2} + \sqrt{\frac{1}{4} + \frac{V_{GS} - V_{FB.ov}}{\Gamma_{g.ov}^2}}} & \text{if } V_{GS} > V_{FB.ov} \\ \frac{V_{GS} - V_{FB.ov}}{\frac{1}{2} + \sqrt{\frac{1}{4} + \frac{V_{FB.ov} - V_{GS}}{\Gamma_{s.ov}^2}}} & \text{otherwise} \end{cases}$$

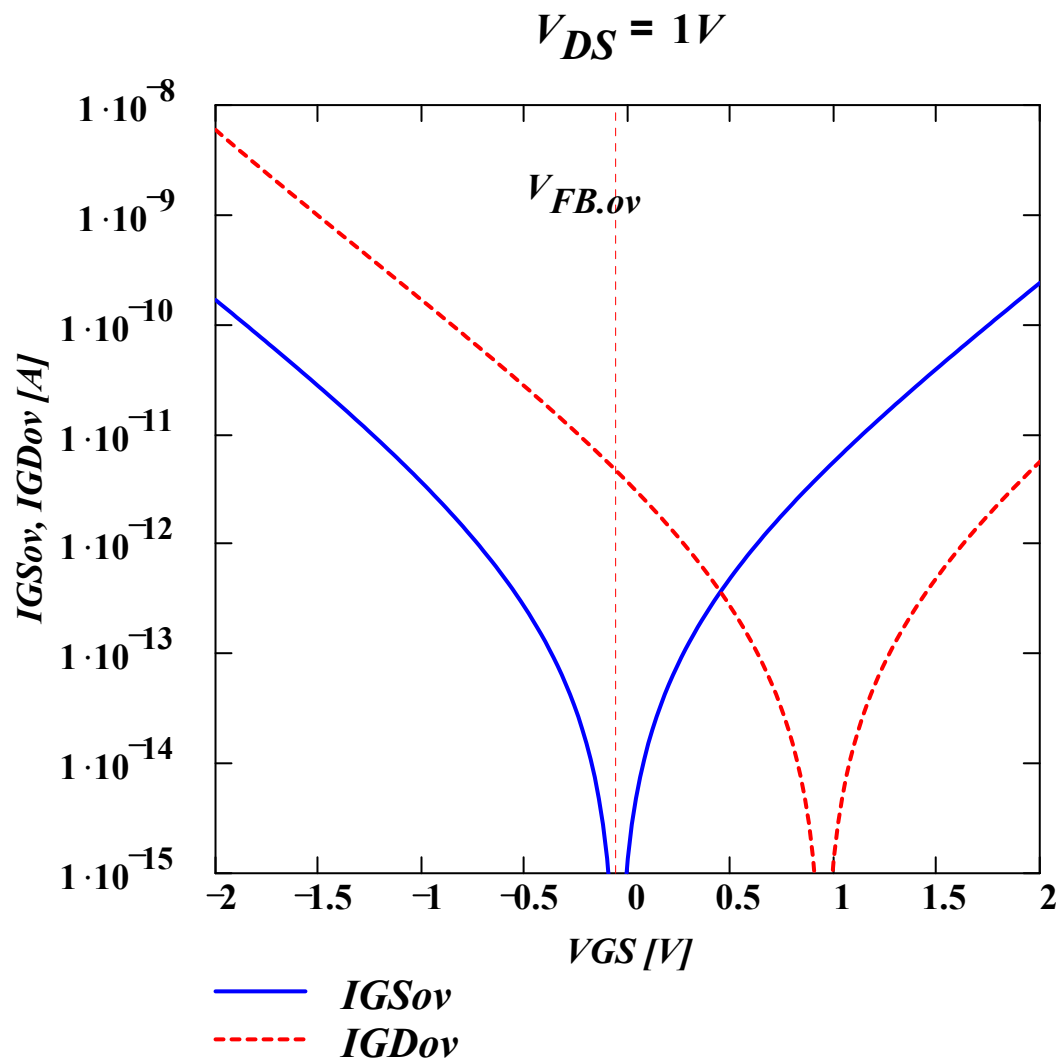
depletion at gate & accumulation at source

accumulation at gate & depletion at source



EKV3.0: Gate Current Modeling

Source/Gate & Drain/Gate Overlap Currents



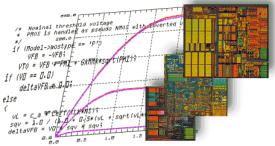
$t_{ox.ov} = 2\text{ nm}$

$W = 10\ \mu m$

$L_{ov} = 10\text{ nm}$

$\Gamma_{s.ov} = 5.0\sqrt{V}$

$\Gamma_{g.ov} = 5.0\sqrt{V}$



EKV3.0: Gate Current Modeling

Total Gate Current

