

---

**The problem can be submitted until Mai 10, 12 :00 noon, either at the exercise session or into the box in front of MA C1 563.**

---

**Student(s)**<sup>1</sup> :

**Question 1 :** *The question is worth 5 points.*

0  1  2  3  4  5

*Reserved for the corrector*

Given a graph  $G$ , a perfect matching of  $G$  is a matching which covers all the vertices (equivalently, a matching of cardinality  $|V|/2$ ).

Suppose you are given an oracle that, given a graph  $G$ , tells you whether  $G$  has a perfect matching or not. Show how to use this oracle to determine the maximum cardinality matching of a graph  $G(V, E)$ . The total number of calls to the oracle (to find the cardinality of the maximum matching, and then to find the matching itself) should be at most  $|V| + |E|$ .

---

1. You are allowed to submit your solutions in groups of at most three students.