

Practical exercises
Optimization Methods in Finance
Fall 2009

Practical exercise (Bonus project - 4 points)

Implement the branch and bound algorithm. More precisely implement a method

`void branchAndBound(Vector<double> c, Matrix<double> A, Vector<double> b)`
in C++ (or in Matlab) that solves

$$\begin{aligned} \max c^T x \\ Ax &\leq b \\ x &\in \mathbb{Z}^n \end{aligned}$$

using the branch and bound algorithm (and outputs the found solution).

Hints:

1. You can use any LP library to solve the relaxations (as you did for the Frank-Wolfe algorithm).
2. We recommend to test your instance with a small example, say from exercise 6.1.
3. If for a fractional solution x^* one has several variables $x_i^* \notin \mathbb{Z}$ you can branch on an arbitrary such i .

The details for the submission are as follows:

1. Send your (compilable) C++/Matlab code till **26.01.09** to yanick.raja@epfl.ch.
2. The submission has to contain the solutions for the following 2 integer programs:

$$\begin{aligned} \max \quad & (5, 6, 10, 10, 8, 10, 10, 10, 9, 10)^T x && (IP1) \\ & (4788, 3703, 8104, 8357, 5089, 6832, 9723, 7054, 3680, 6088)x \leq 10000 \\ & -x_i \leq 0 && \forall i = 1, \dots, 10 \\ & x_i \in \mathbb{Z} && \forall i = 1, \dots, 10 \end{aligned}$$

$$\begin{array}{r}
 \max(1.1, 1.2, 1.3, 1.4, 1.5, 1.6)^T x \quad (IP2) \\
 \left(\begin{array}{cccccc}
 1 & 0 & 0 & 1 & 0 & 0 \\
 0 & 0 & 0 & 1 & 0 & 1 \\
 0 & 1 & 0 & 1 & 0 & 0 \\
 0 & 1 & 0 & 0 & 1 & 0 \\
 1 & 1 & 0 & 0 & 0 & 1 \\
 0 & 0 & 1 & 0 & 1 & 1 \\
 0 & 0 & 1 & 1 & 0 & 0 \\
 -1 & 0 & 0 & 0 & 0 & 0 \\
 0 & -1 & 0 & 0 & 0 & 0 \\
 0 & 0 & -1 & 0 & 0 & 0 \\
 0 & 0 & 0 & -1 & 0 & 0 \\
 0 & 0 & 0 & 0 & -1 & 0 \\
 0 & 0 & 0 & 0 & 0 & -1
 \end{array} \right) x \leq \left(\begin{array}{c}
 1 \\
 1 \\
 1 \\
 1 \\
 1 \\
 1 \\
 1 \\
 0 \\
 0 \\
 0 \\
 0 \\
 0 \\
 0
 \end{array} \right) \\
 x_1, \dots, x_6 \in \mathbb{Z}
 \end{array}$$

Good luck and merry Christmas.