

# APPLYING KALMAN FILTERING ON A QUADRUPEDED ROBOT

Lucian Cucu

*Professor:*  
A. Ijspeert

*Supervisors:*  
A. Sproewitz,  
A. Tuleu



# Main objectives

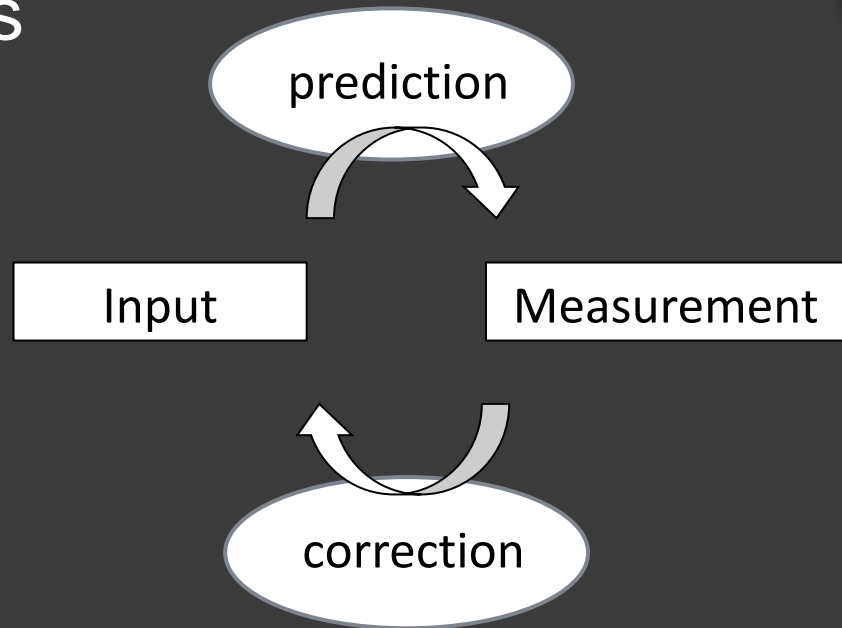
- ⦿ Instantaneous pitch and roll angle estimate (of CoM)
- ⦿ Instantaneous forward and upward acceleration (of CoM)

# The Kalman filter: a reminder

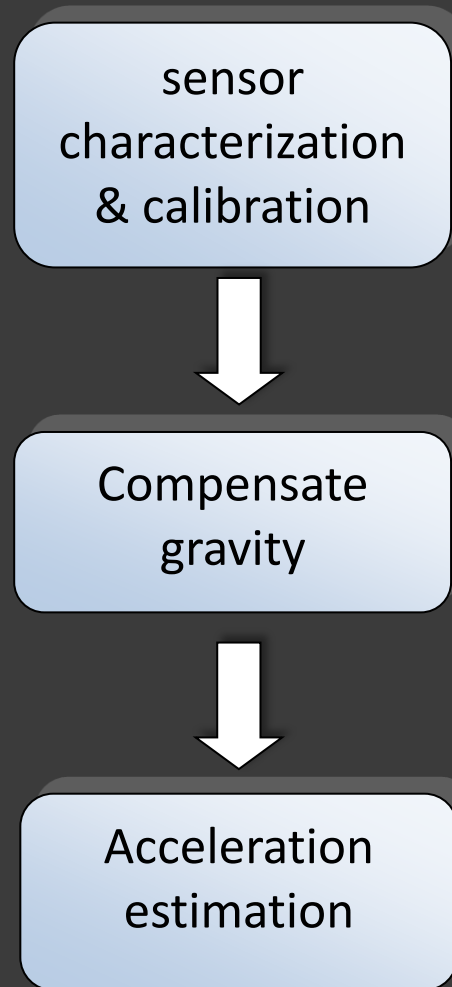
- Multiple data sources

- Each data is noisy

- Final estimate more precise than any of the data



# Project outline



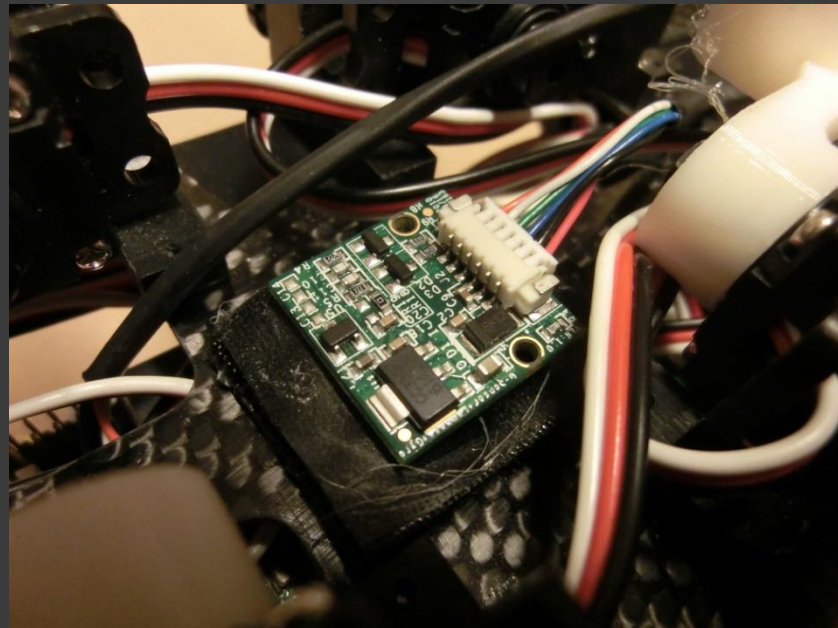
# Hardware

- 9 DOF IMU mounted near the CoM

- 3 axis acceleromoter
- 3 axis gyro
- 3 axis compass

- MoCap

- 12 camera system
- “Absolute” reference



sensor  
calibration



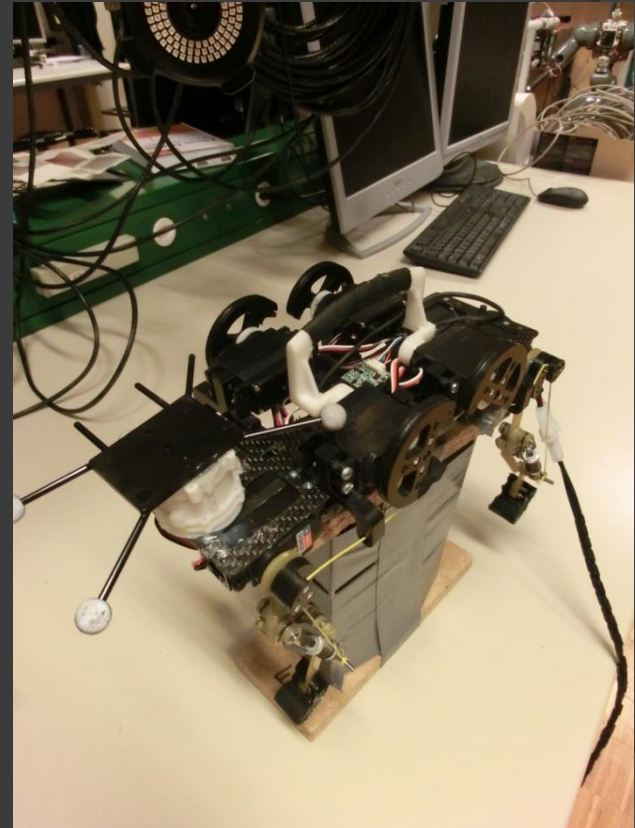
Compensate  
gravity



Acceleration  
estimation

# Hardware

- Quadruped robot: Cheetah- Cub
  - open loop control
  - no sensor input
  - IR markers on the back
  - trot gait



*The Cheetah-cub*

sensor  
calibration



Compensate  
gravity



Acceleration  
estimation

# IMU Characterization

- ◎ Bias
- ◎ Scale factors
- ◎ Misalignment factors
- ◎ Temperature effect, Bias drift, etc.

sensor  
characterization &  
calibration



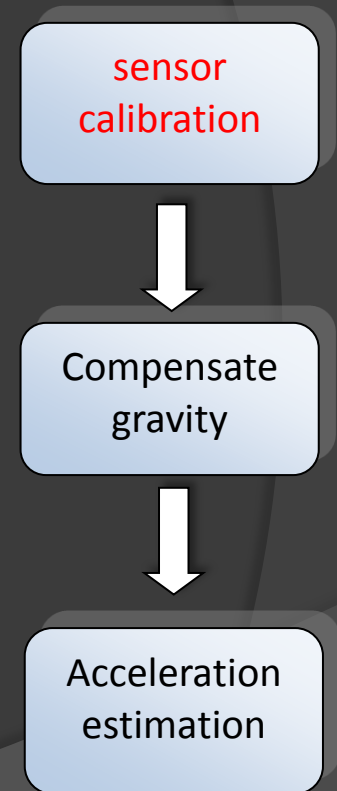
Setup of a  
comparison  
environment



Kalman  
filtering

# IMU Characterization

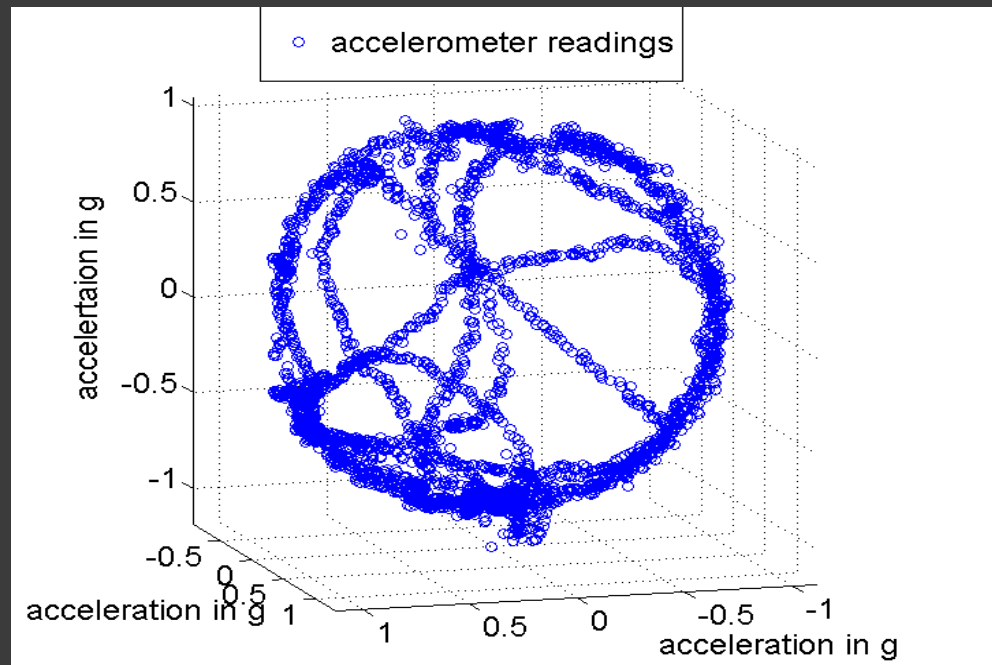
- 3 different “in-field” methods tested
- Ellipsoid method is preferred





# IMU Characterization

- 3 different methods tested
- Ellipsoid method is preferred



sensor  
calibration



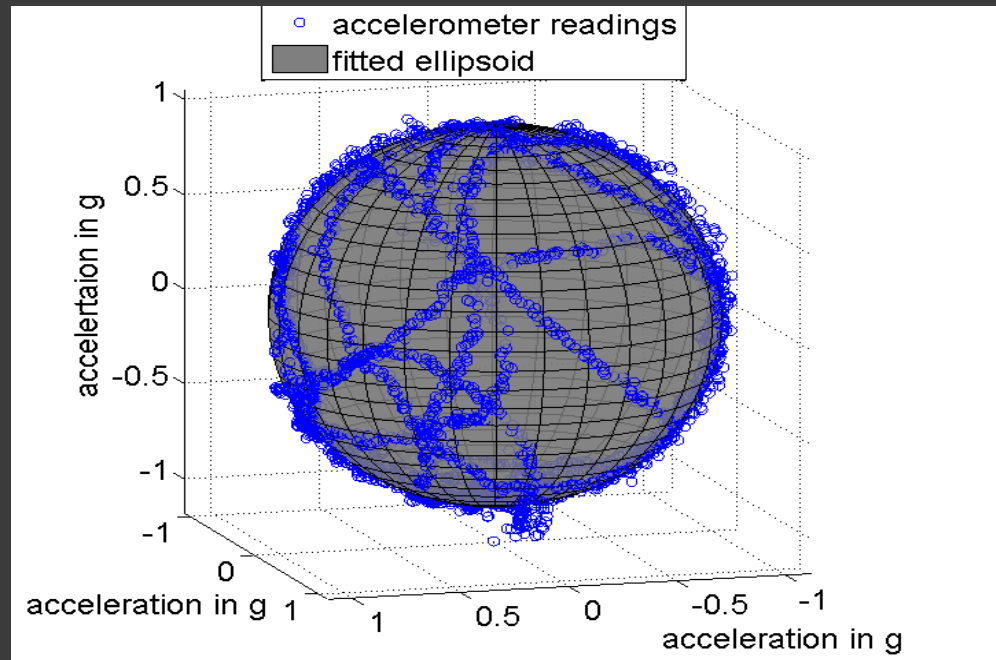
Compensate  
gravity



Acceleration  
estimation

# IMU Characterization

- 3 different methods tested
- Ellipsoid plot is preferred



sensor  
calibration



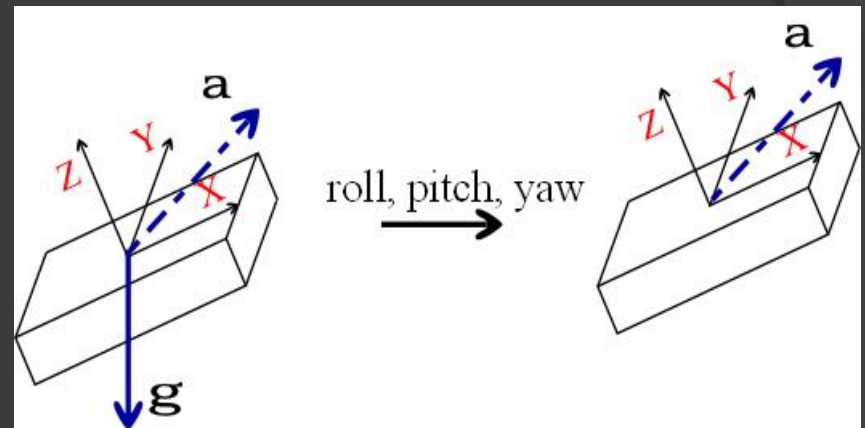
Compensate  
gravity



Acceleration  
estimation

# Achieving gravity compensation

- 1<sup>st</sup> step: estimate orientation with a 1<sup>st</sup> Kalman filter
- 2<sup>d</sup> step: remove gravity
- 3<sup>rd</sup> step: compare validity of results with MoCap



sensor  
calibration



Compensate  
gravity



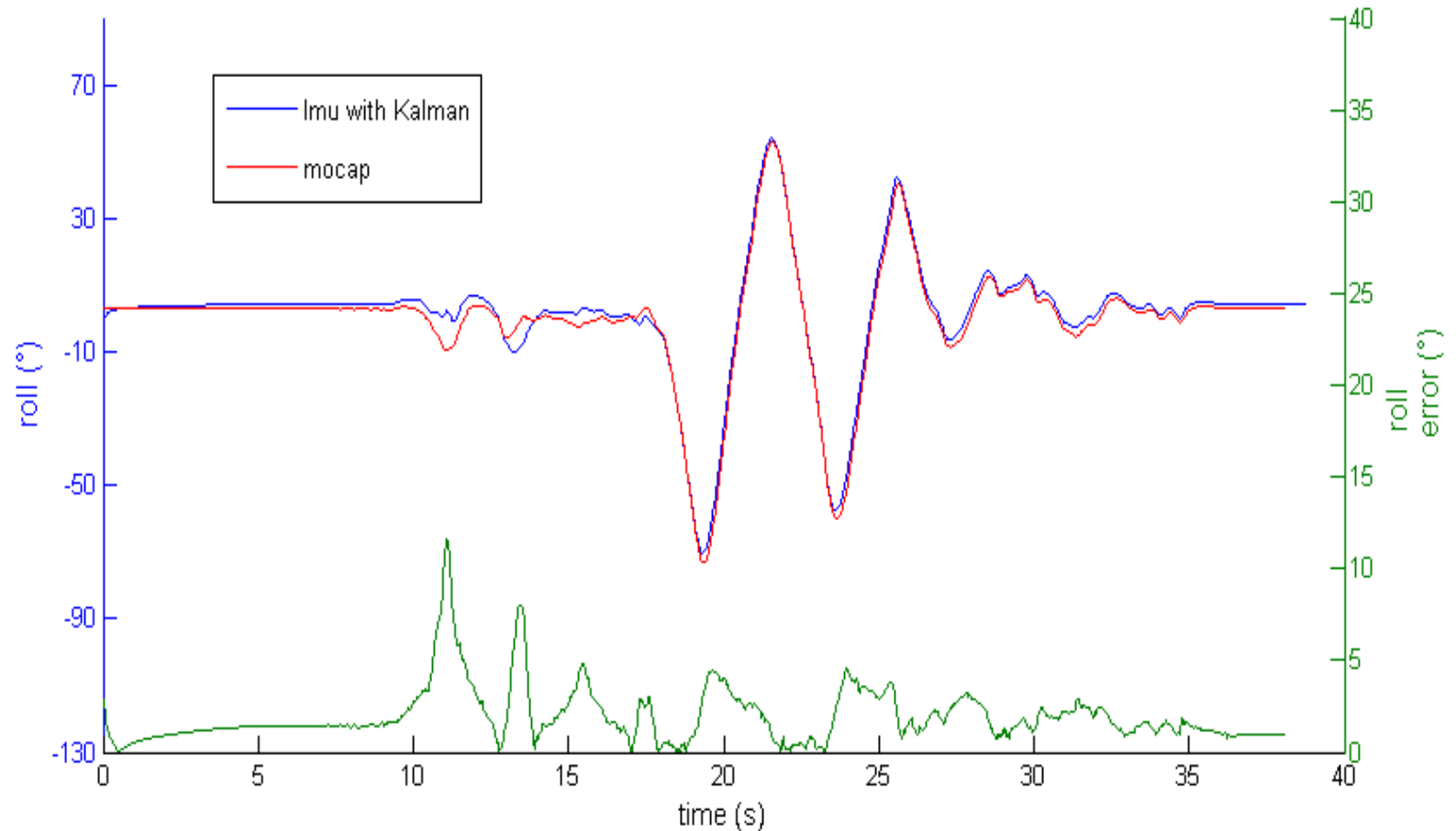
Acceleration  
estimation

# Kalman filter for attitude estimation

- Kalman filter to combine sensor data
- Gyroscope for prediction
- Accelerometer for correction

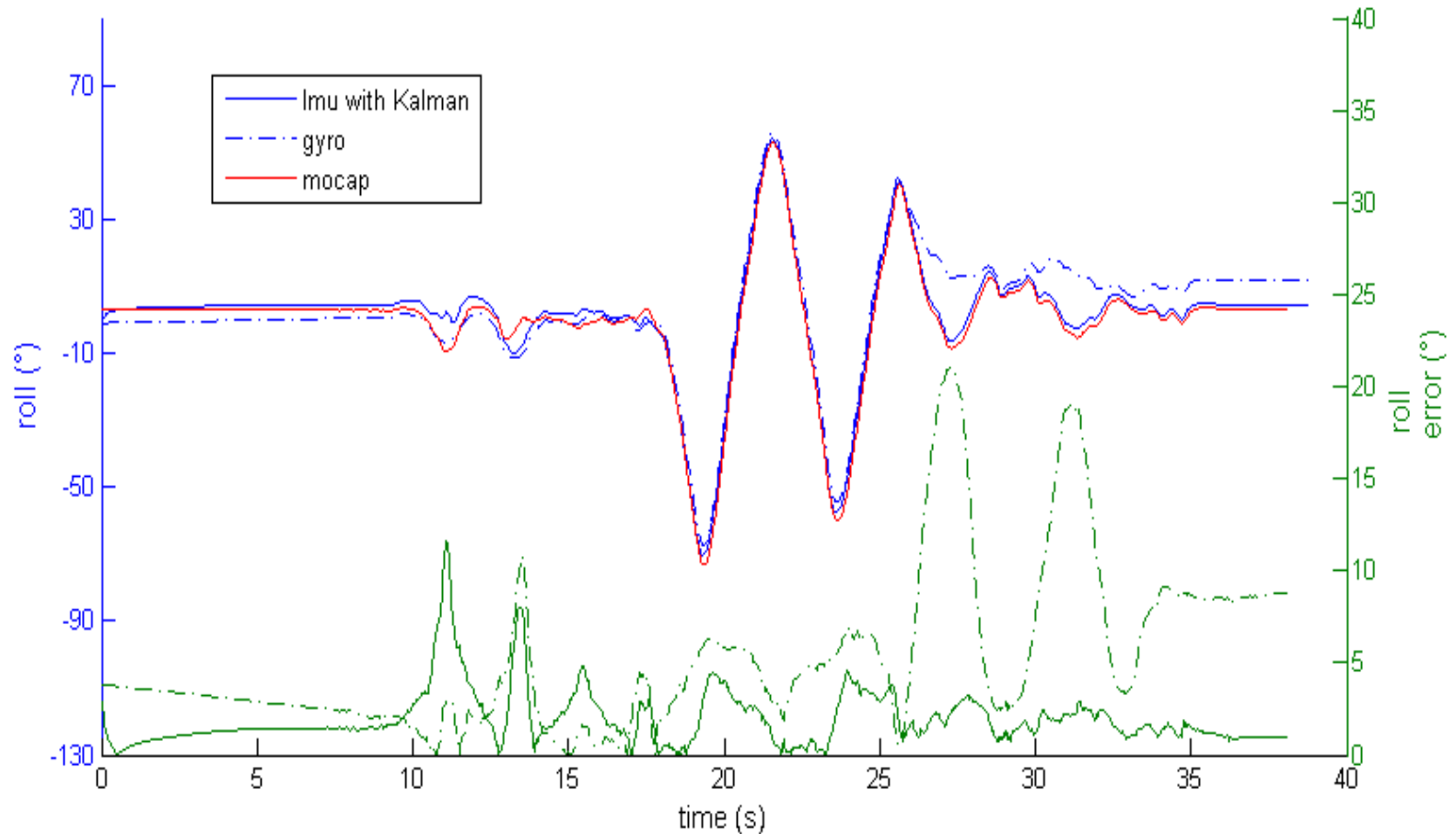


# Comparing results with Mocap data



Overall RMSE:  $\sim 2.4^\circ$

# Comparing results with Mocap data

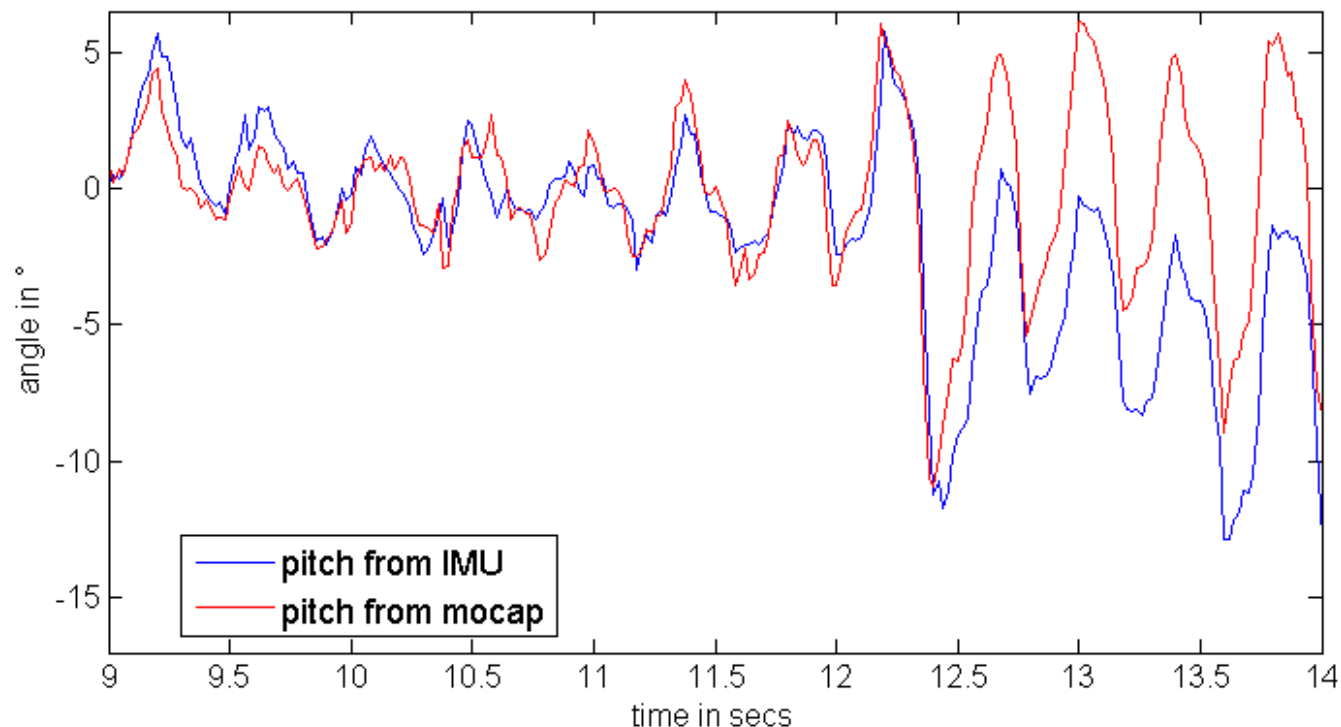


Overall RMSE:  $\sim 2.4^\circ$  (IMU) and  $\sim 7.5^\circ$  (only gyro)

# Comparing results with Mocap data

## Pitch angle during a Cheeeth run

AFTER applying the relative rotation matrix



sensor  
calibration



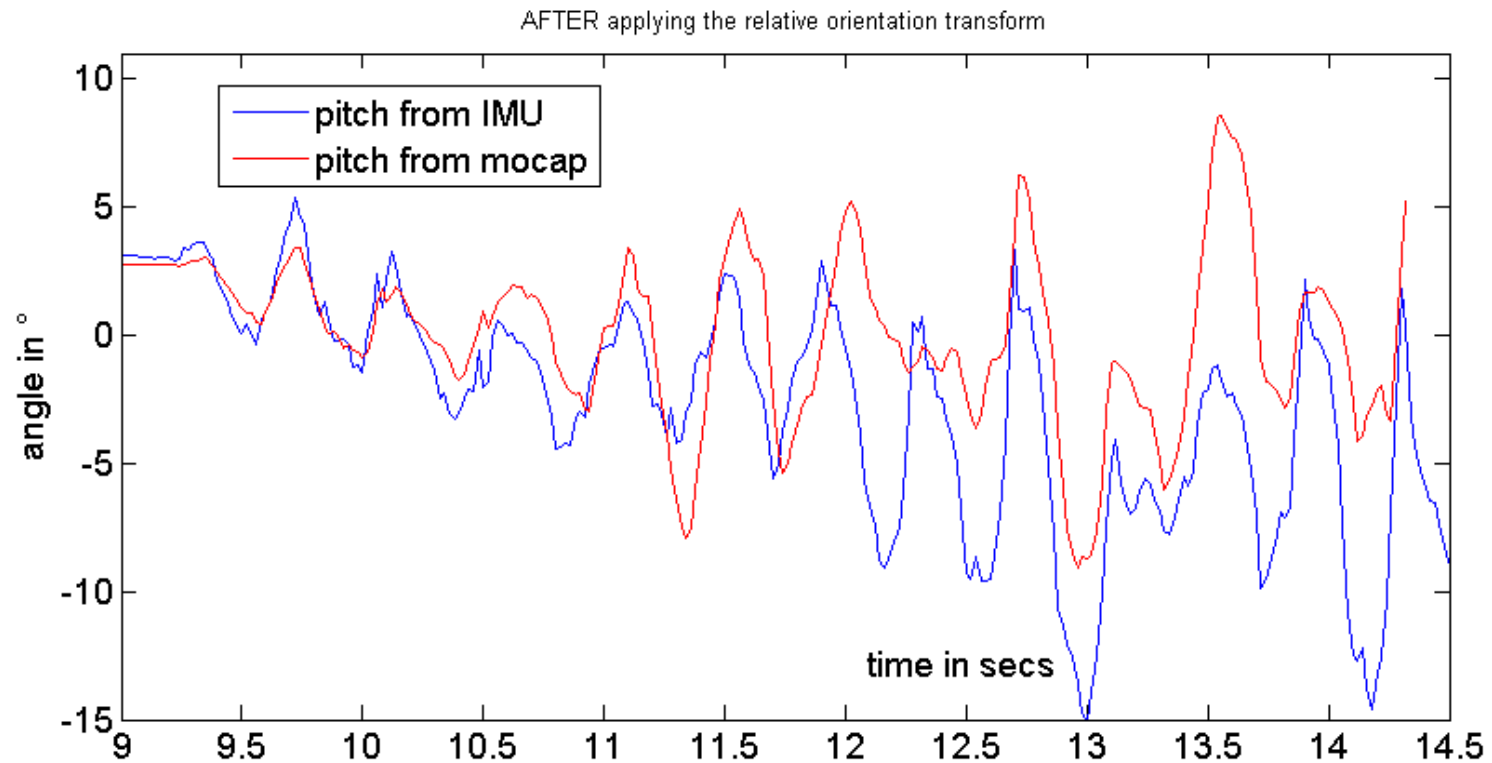
Compensate  
gravity



Acceleration  
estimation

# Comparing results with Mocap data

## Pitch angle during a Cheeath run



sensor  
calibration



Compensate  
gravity

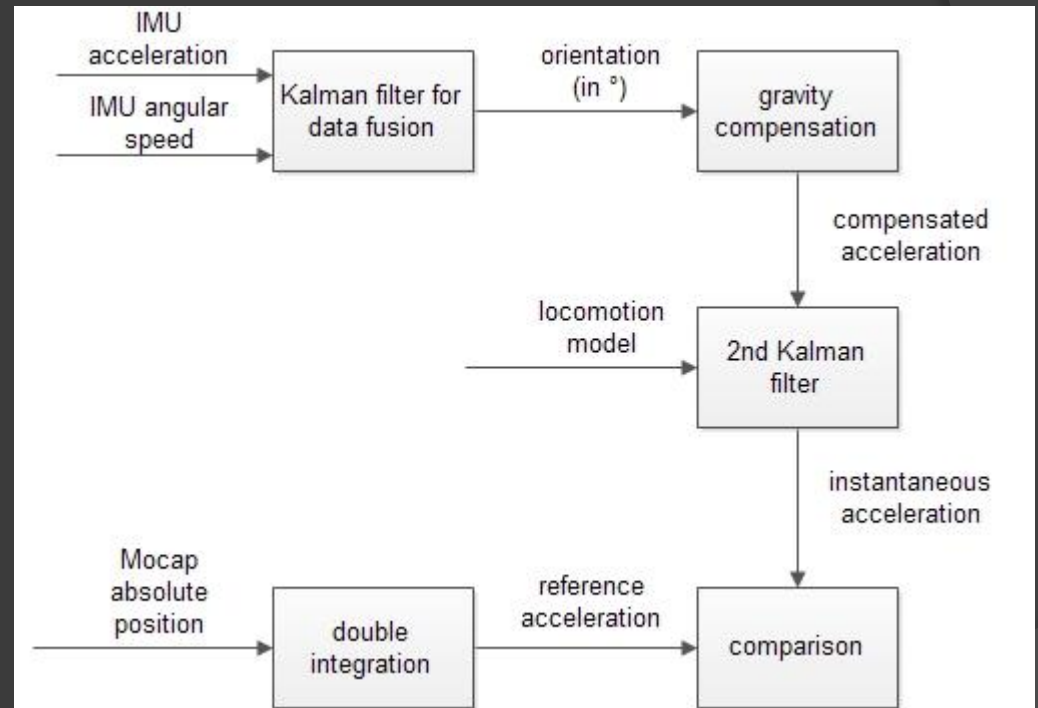


Acceleration  
estimation



# Acceleration estimation

- 2<sup>nd</sup> Kalman filter
- Locomotion model for prediction
- Measured and compensated acceleration for correction



sensor  
calibration



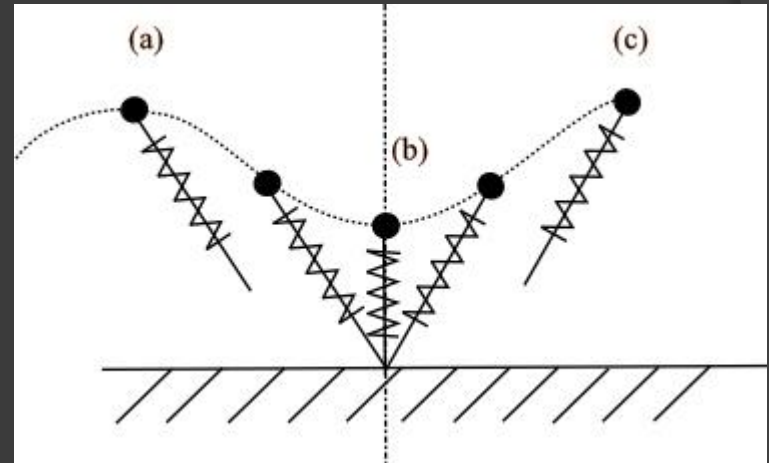
Compensate  
gravity



Acceleration  
estimation

# Locomotion model

- Imagine leg as simple spring
- Assume a symmetric and periodic trajectory
- Assume acceleration a sine wave with specific to the gait
- Amplitude and offset computed manually



sensor  
calibration

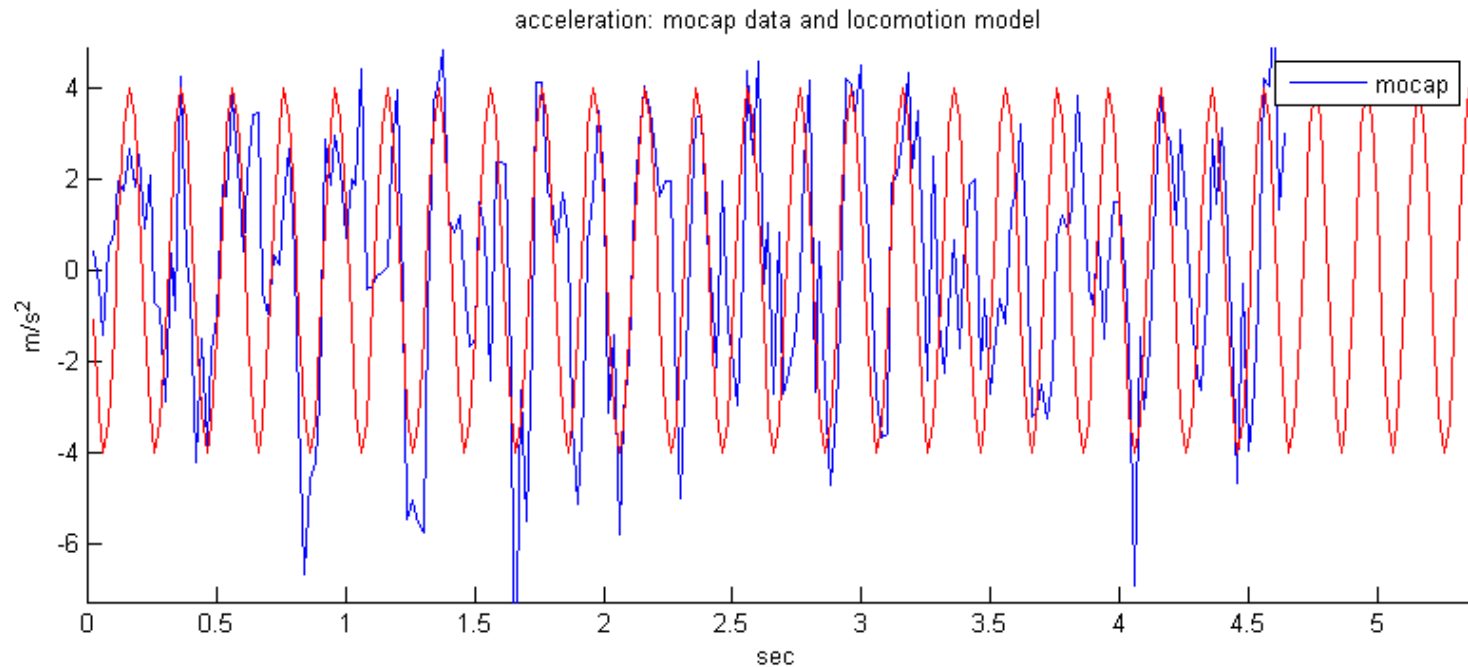


Compensate  
gravity



Acceleration  
estimation

# Locomotion model vs MoCap data



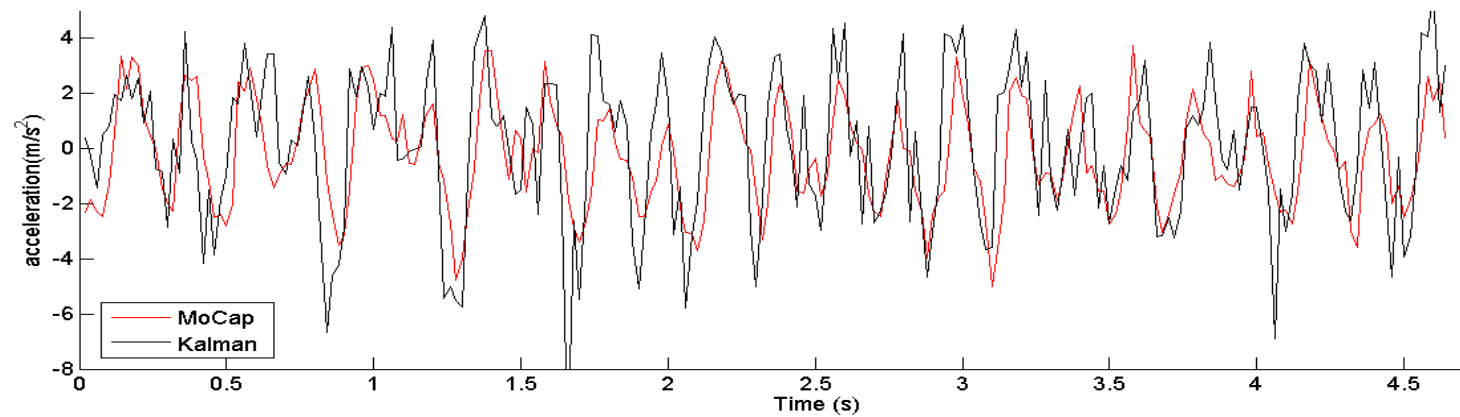
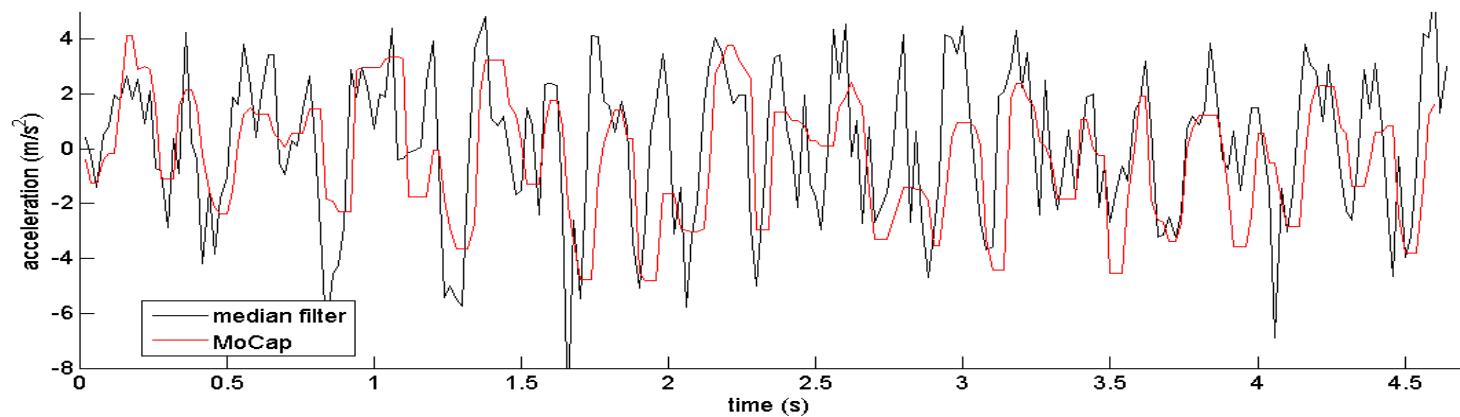
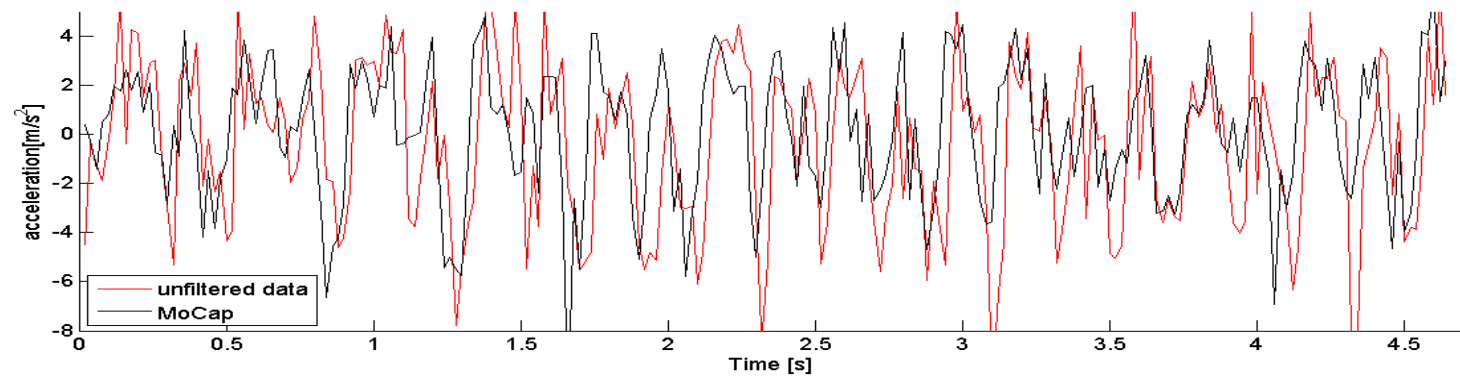
sensor  
calibration



Compensate  
gravity



Acceleration  
estimation



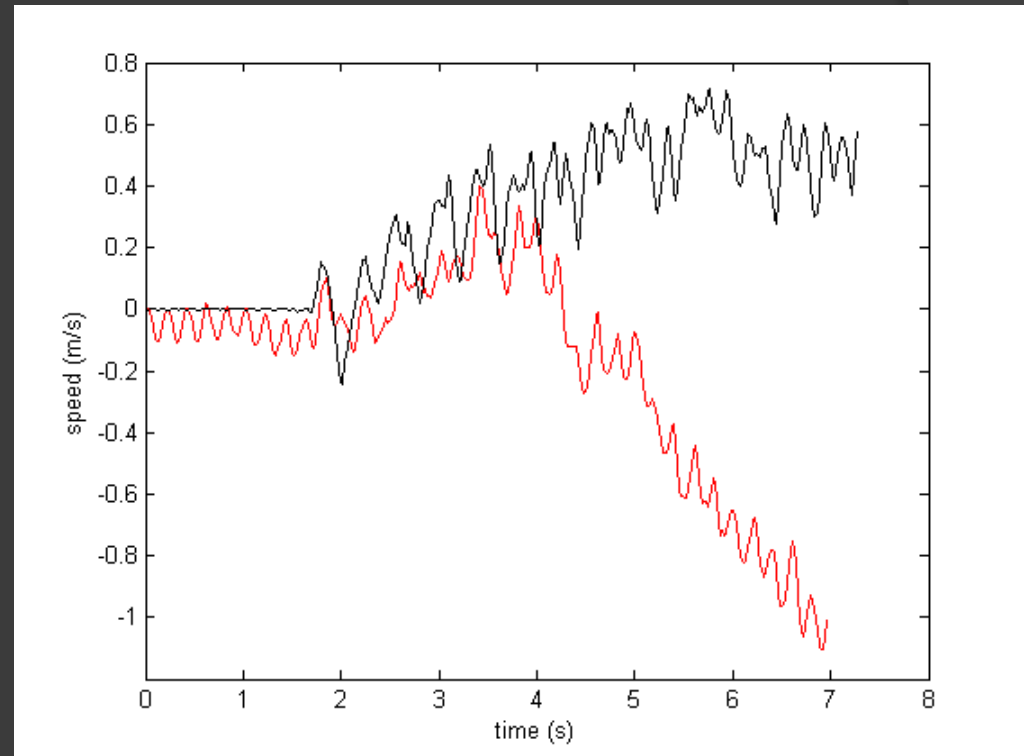
# Results

Evaluation Method	Butterworth Low-pass	Median filter	Kalman filter
<i>Correlation</i>	$0.28 \pm 0.06$	$0.514 \pm 0.04$	<b><math>0.591 \pm 0.04</math></b>
<i>SNR(dB)</i>	$-1.21 \pm 0.4$	$0.71 \pm 0.4$	<b><math>1.5 \pm 0.5</math></b>
<i>RMSE</i>	$2.93 \pm 0.2$	$2.35 \pm 0.2$	<b><math>2.13 \pm 0.02</math></b>

- Results are computed from 6 runs
- Kalman filter outperforms standard filters, but results are not outstanding

# Speed estimation ?

- Mocap speed average  
~ 0.4 m/s
- Bias, noise and other errors make a speed estimation from sole integration difficult



sensor  
calibration

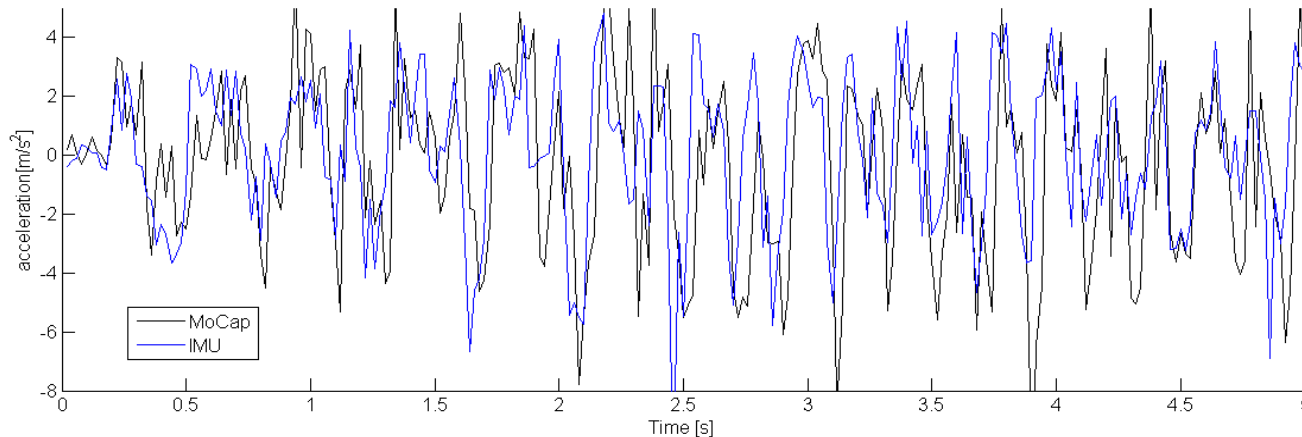


Compensate  
gravity

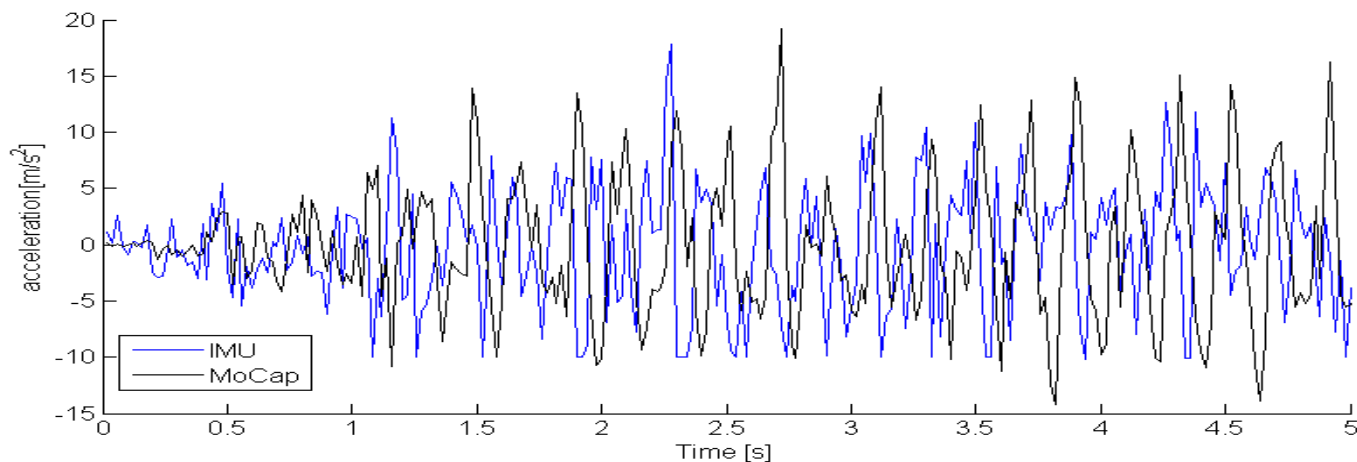


Acceleration  
estimation

# Acceleration estimation on Z axis ?



Acceleration on Y axis



Acceleration on Z axis

# Conclusion

- ⦿ Considerable time is required for IMU calibration
- ⦿ Pitch and roll estimation OK with big amplitudes but bias too important at low amplitude movements
- ⦿ Kalman filter for acceleration estimation less successful but outperforms standard filters
- ⦿ A speed estimation is still not feasible
- ⦿ More and better sensors and more elaborate Kalman design is required

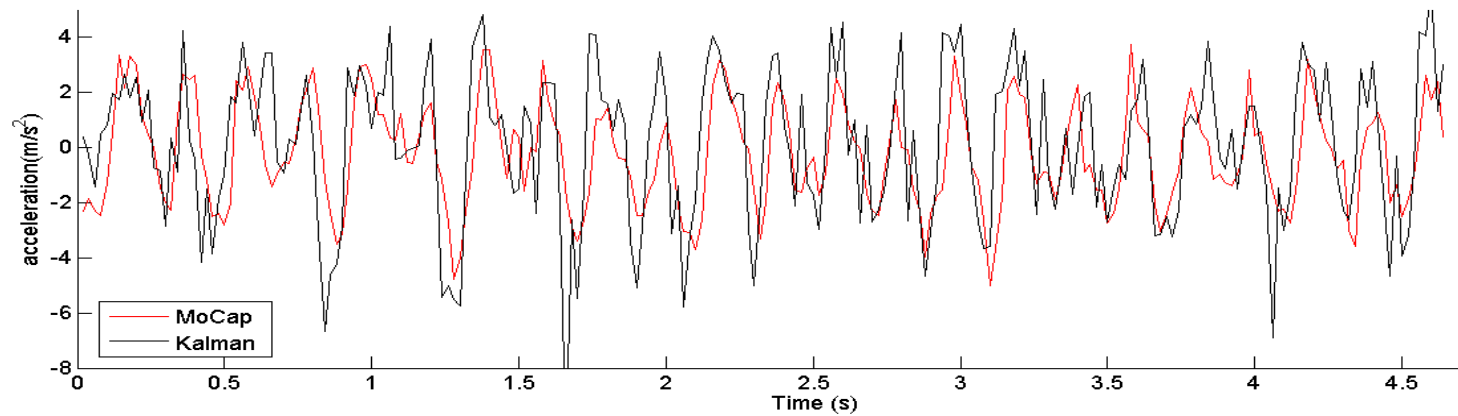
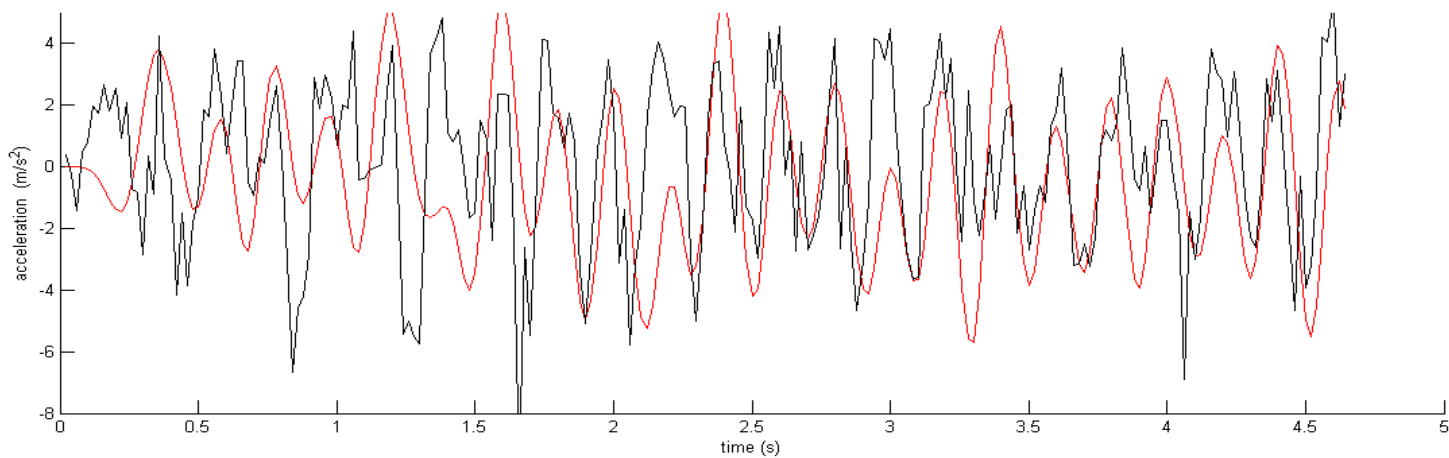
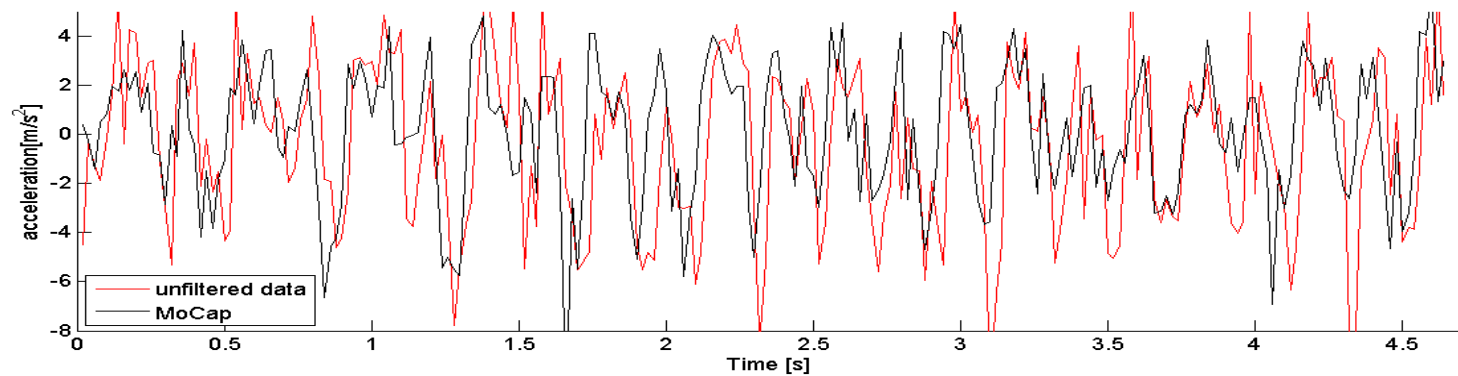


Thank you !

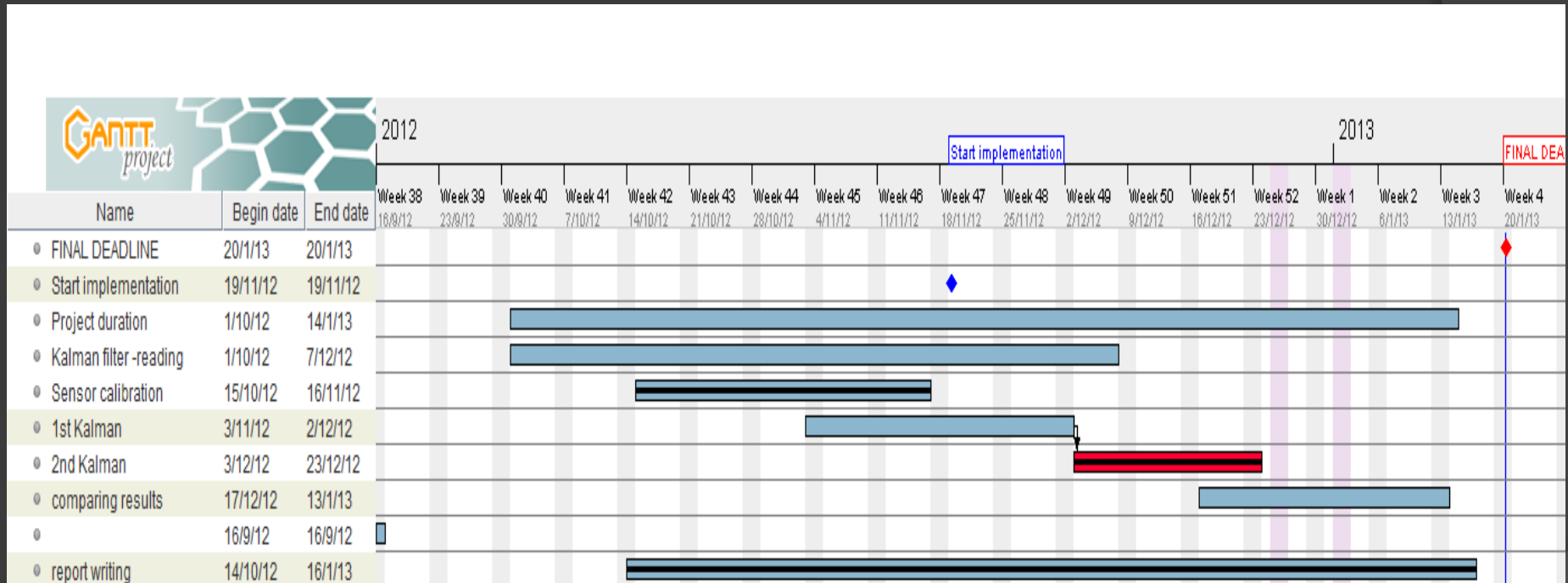
# Annexe

## ◎ Future Work:

- Find better Kalman models, better hardware, calibrate better
- Implement in real time



# Gantt chart



# SNR (signal/noise ratio)

- $\text{snr} = 20 \cdot \log_{10}(\text{norm}(Y)/\text{norm}(Y-X))$
- With  $Y$  = MoCap signal and  $X$  IMU signal