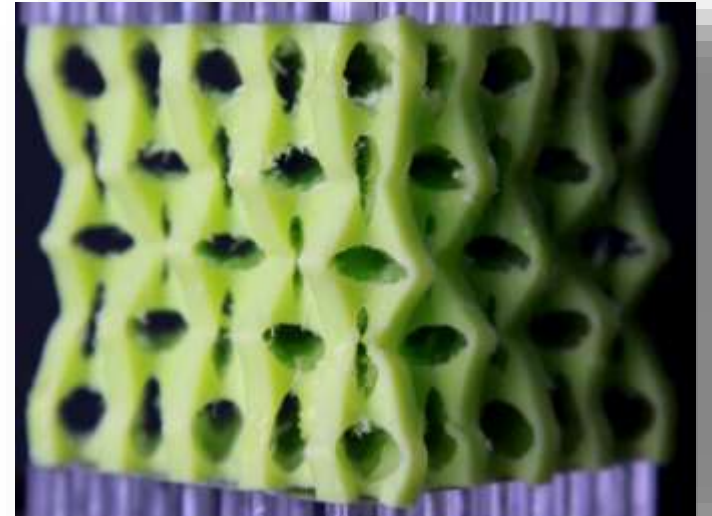
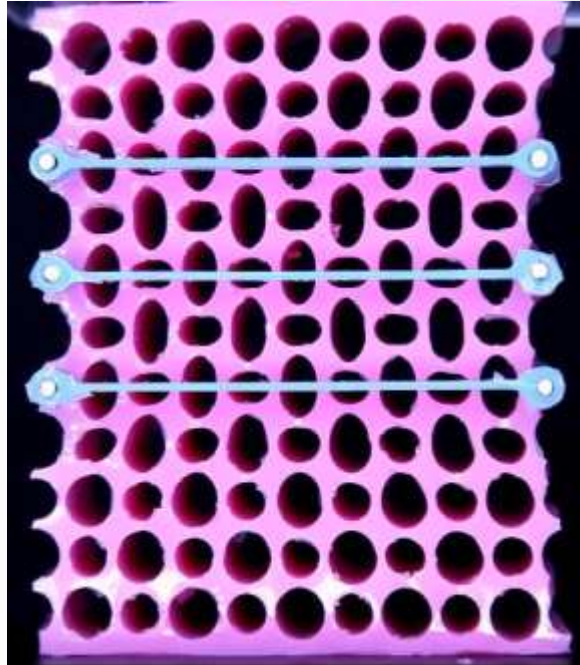
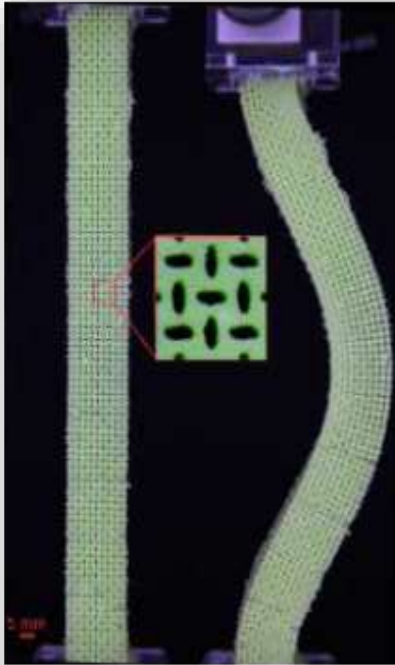


# From Flexible Mechanical Metamaterials... ...to Machine Materials



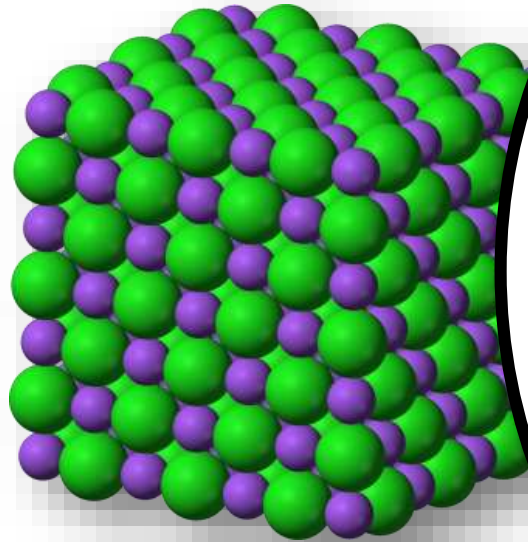
Corentin Coulais

# What is a Material?

Constituent

$^{79}\text{Au}$

Structure

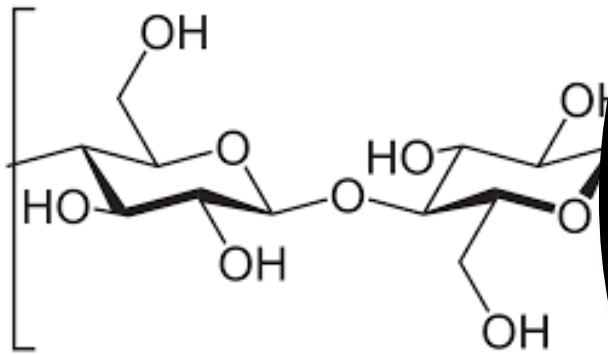


Function

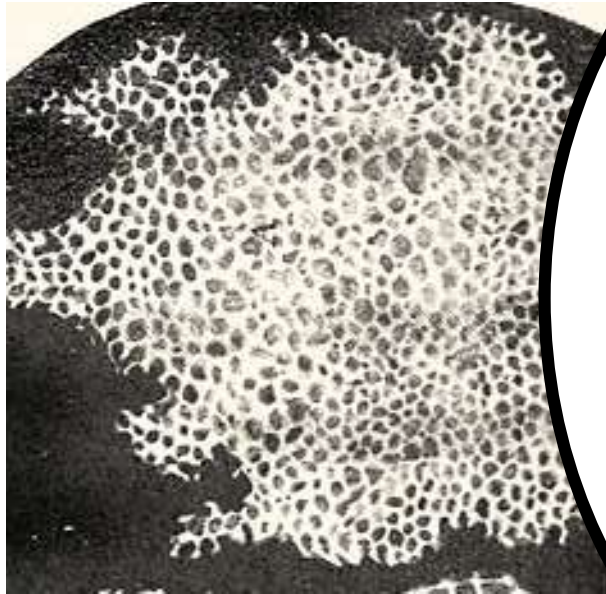


# What is a Material?

Constituent



Structure

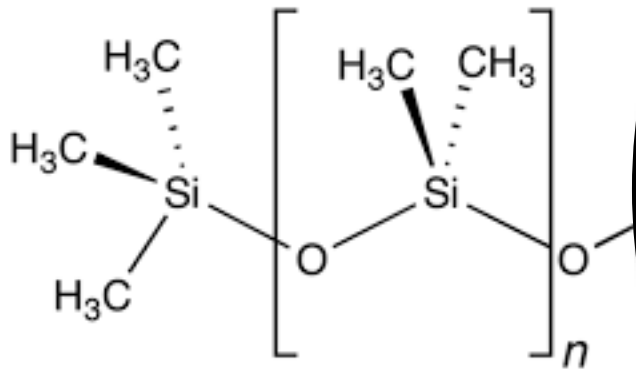


Function

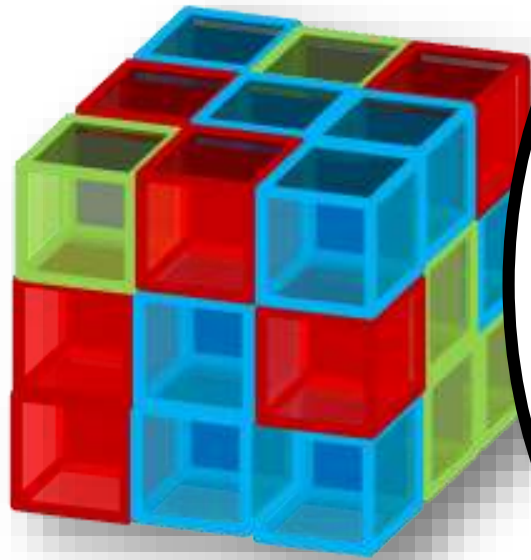


# Designer Matter

Constituent



Structure



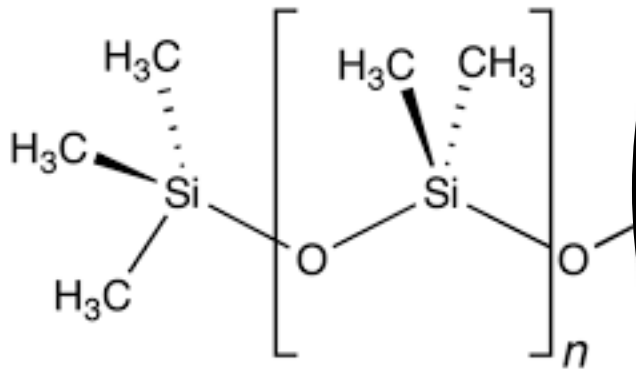
Function

*Anything You Like!*

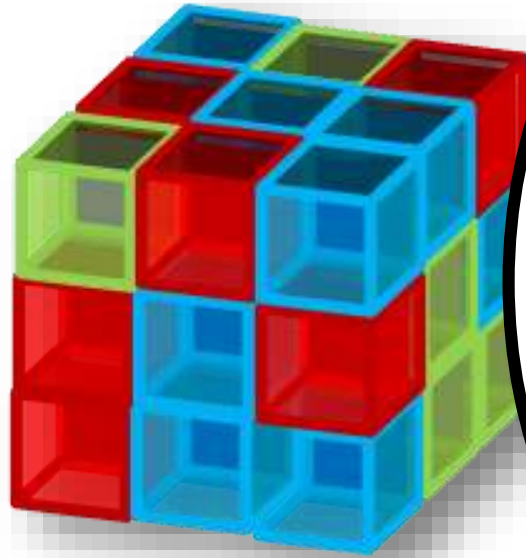


# Machine Matter

Constituent



Structure

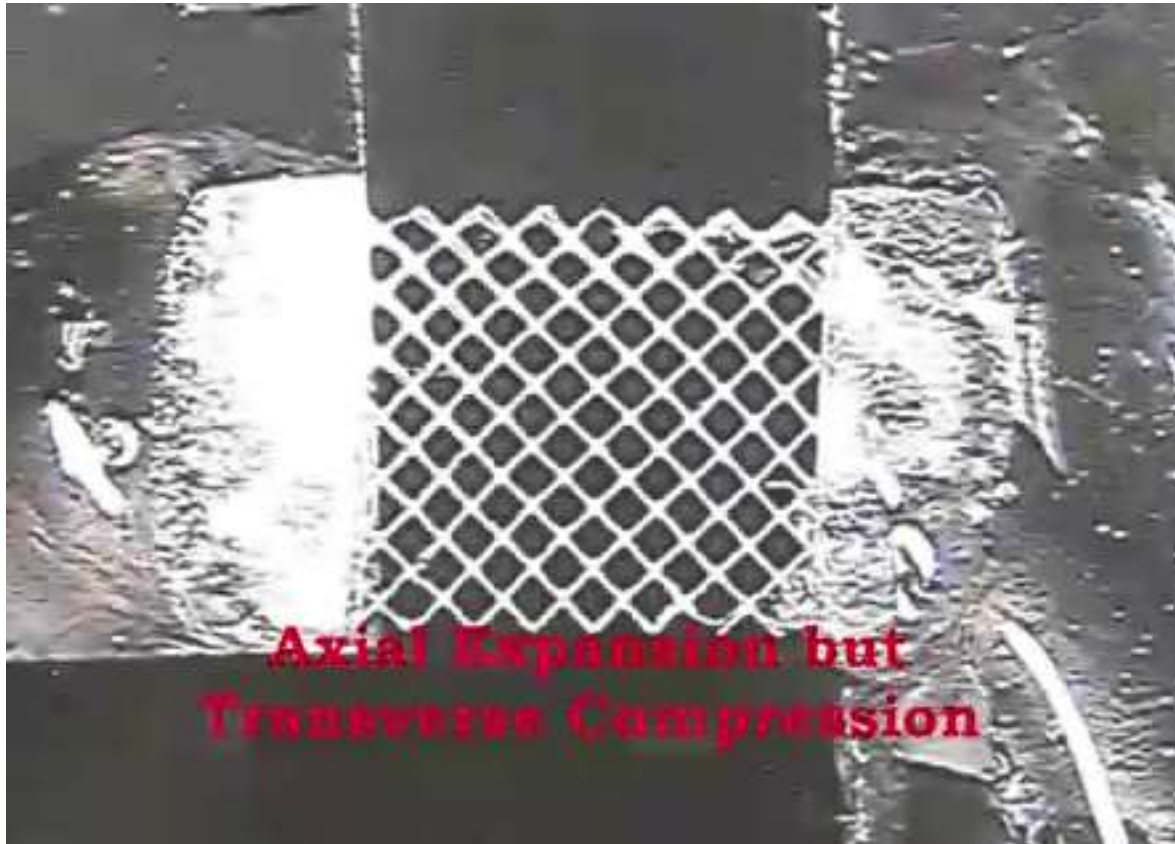


Function

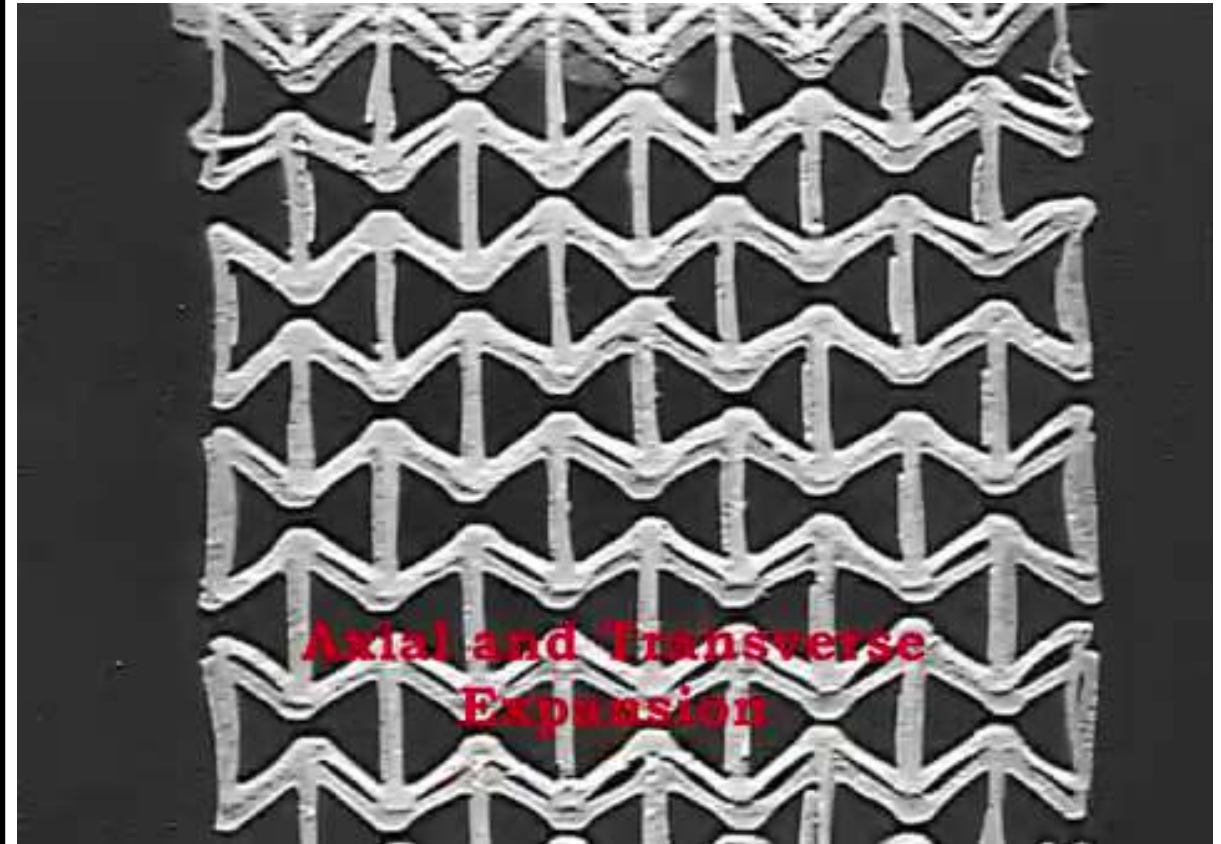


# Mechanical Metamaterials: Poisson's ratio

Positive



Negative (*Auxetic*)



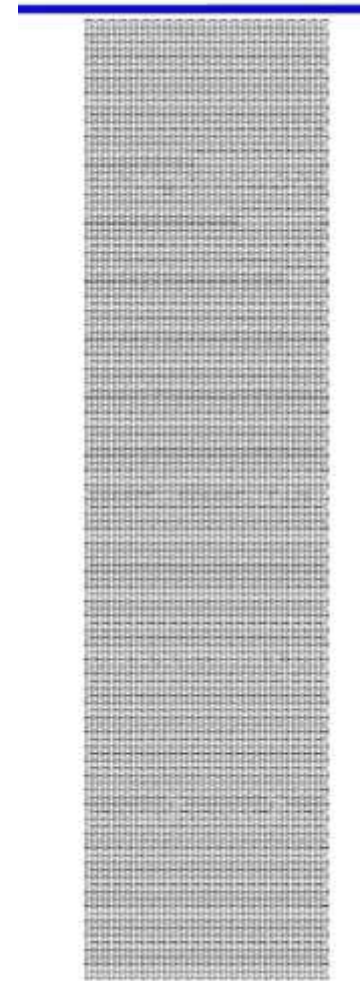
Lakes, Science **235** 1038 (1987)

# Applications of Auxetics?

## Prosthetics and Wear-Tech

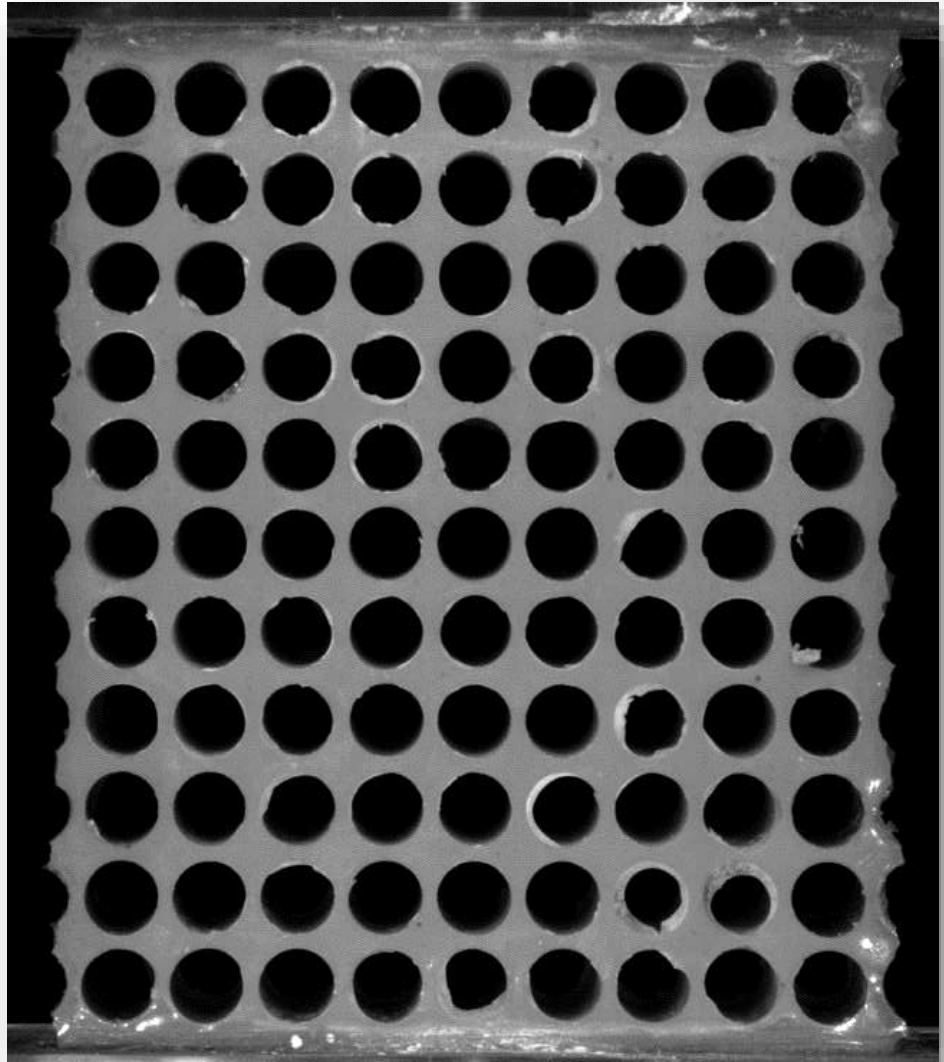


## Shock Damping

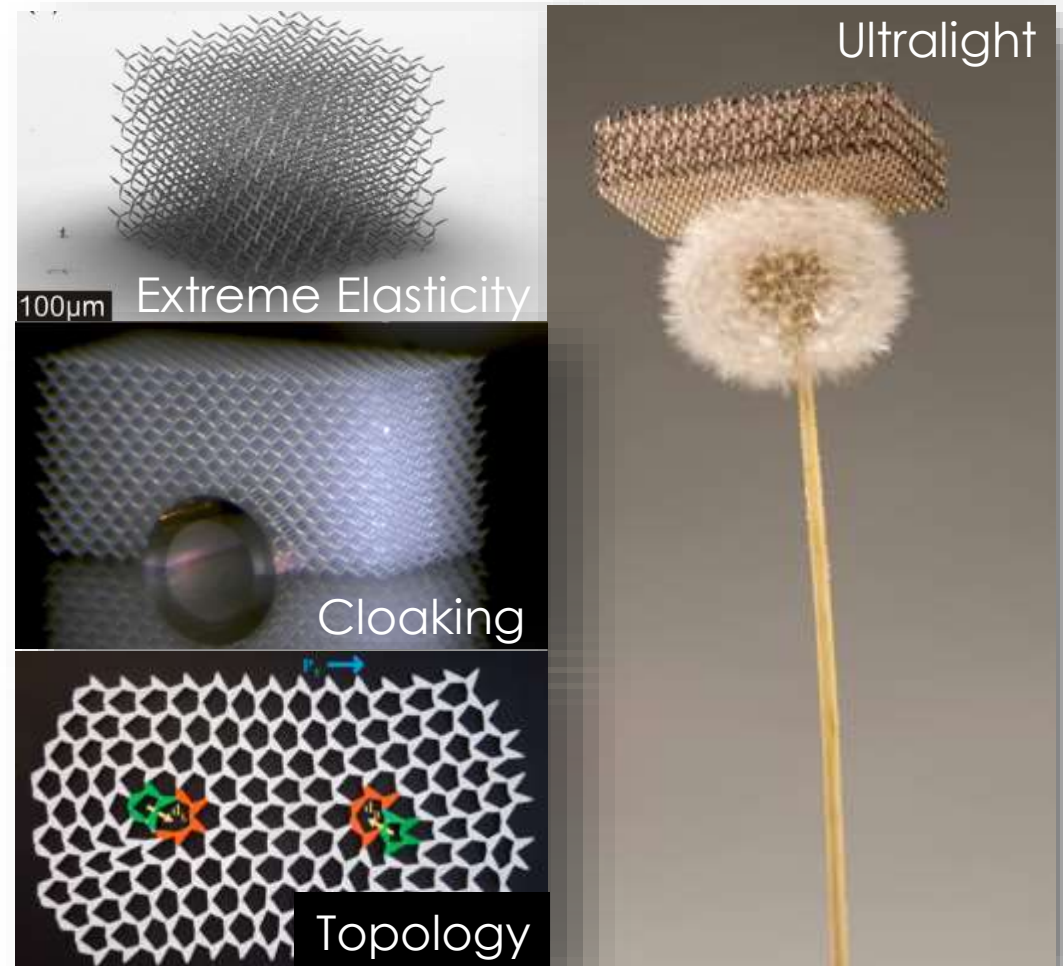




# Mechanical Metamaterials

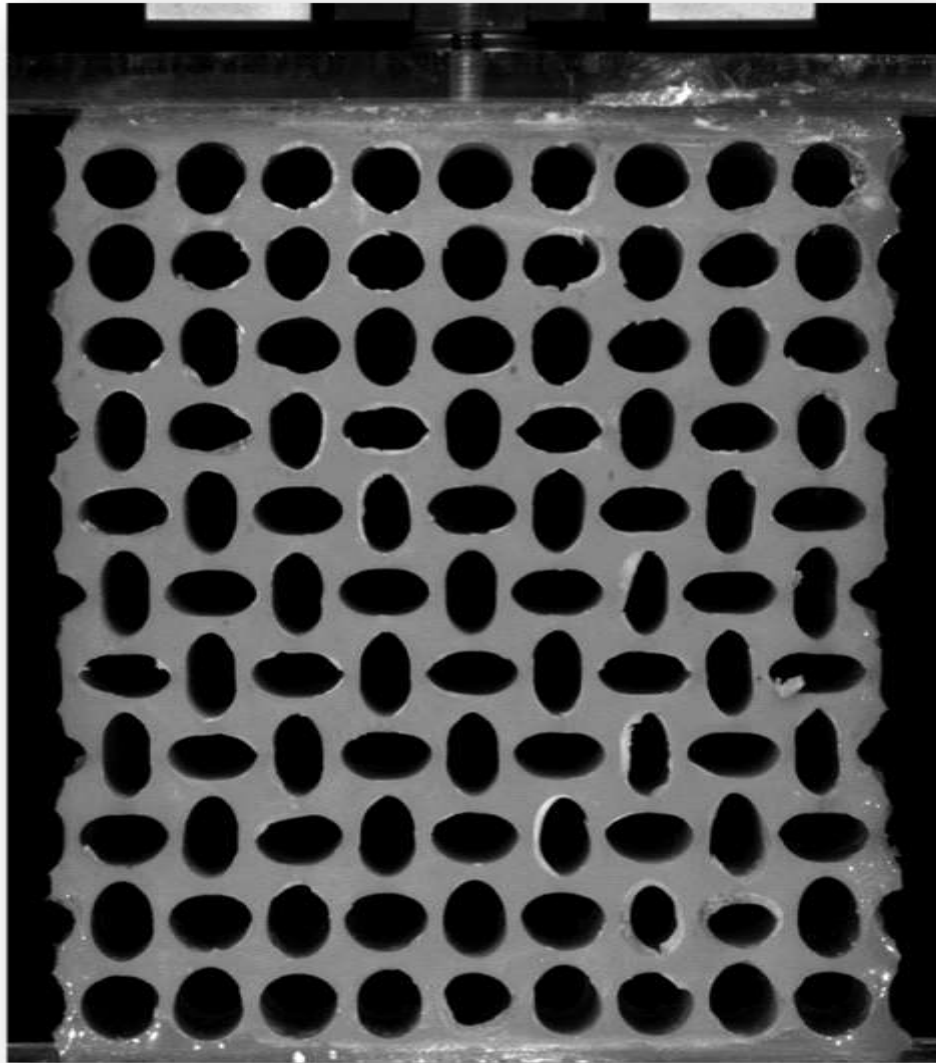


Mullin et al, PRL 2007

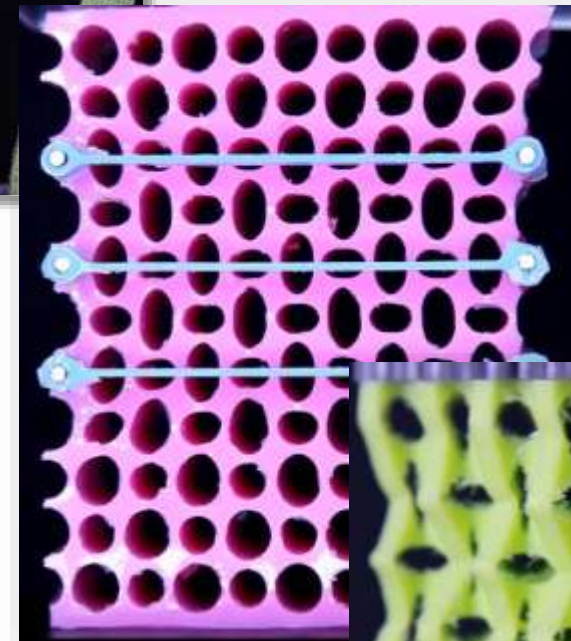
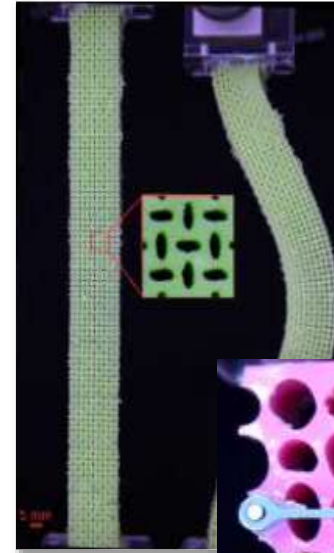




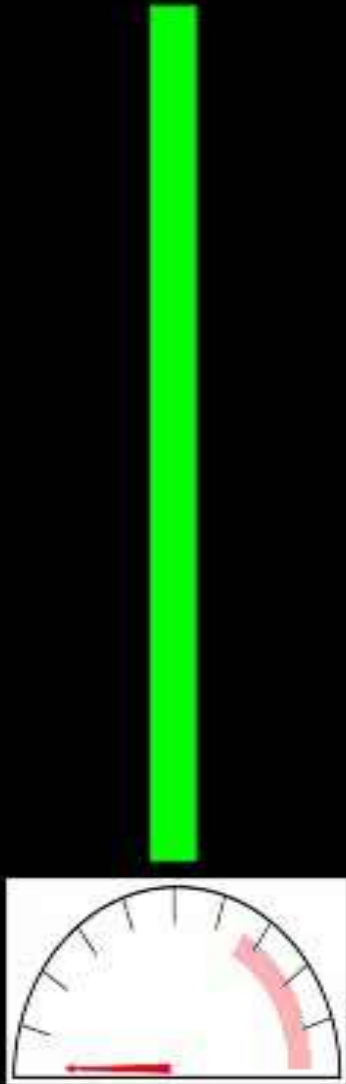
# Nonlinear Mechanical Metamaterials



Mullin et al, PRL 2007



# Metabeam: Tunable Nonlinearity



# Metabeam: Tunable Nonlinearity



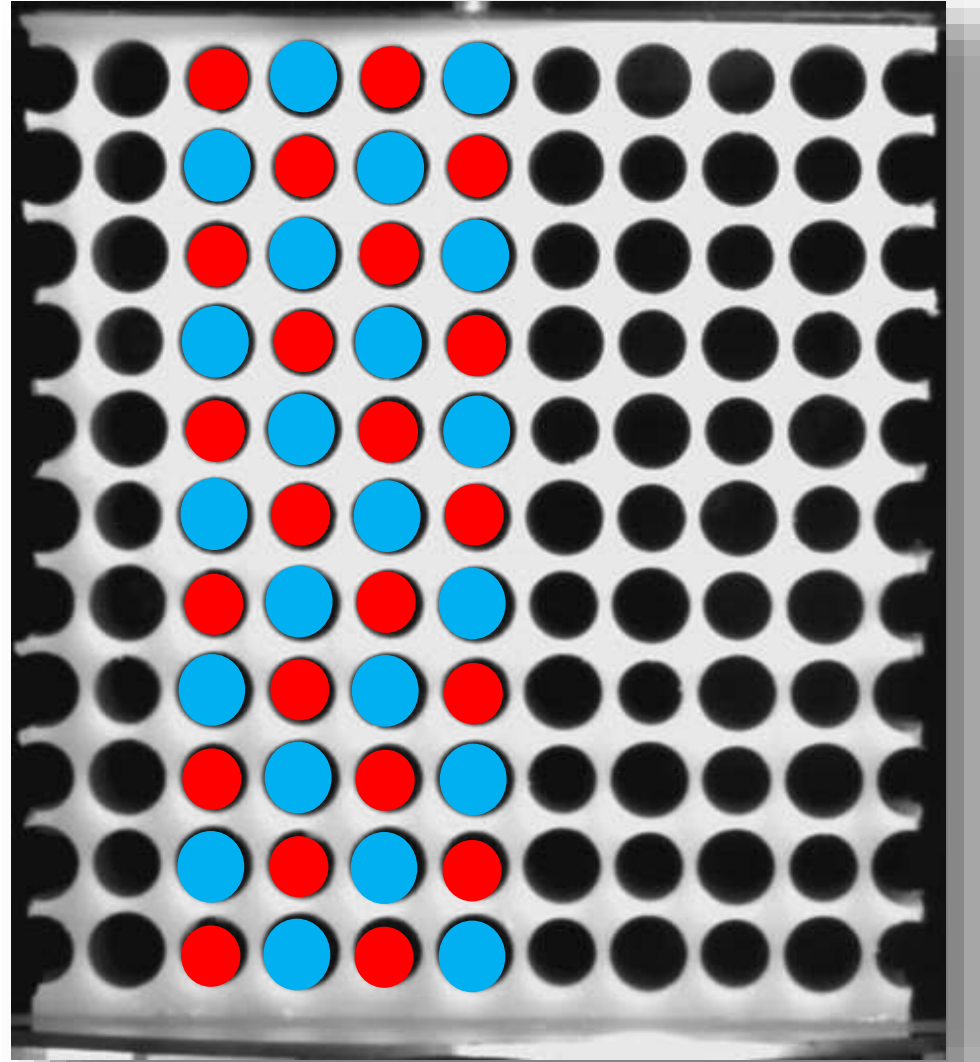
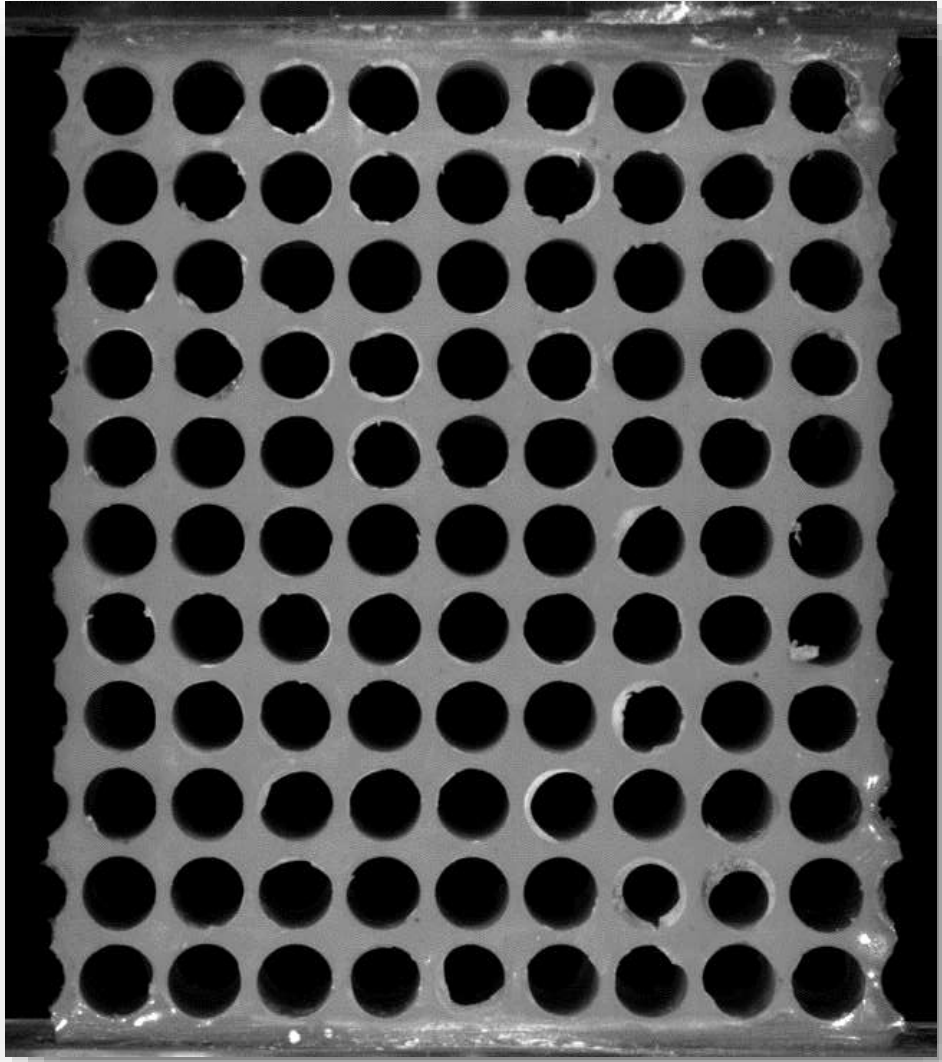
C. Coulais, B. Overvelde, L. Lubbers, K. Bertoldi, M. van Hecke, *PRL* **115** 044301 (2015)

C. Coulais, under review for *Intl. J. Solids Struct.* (2015)

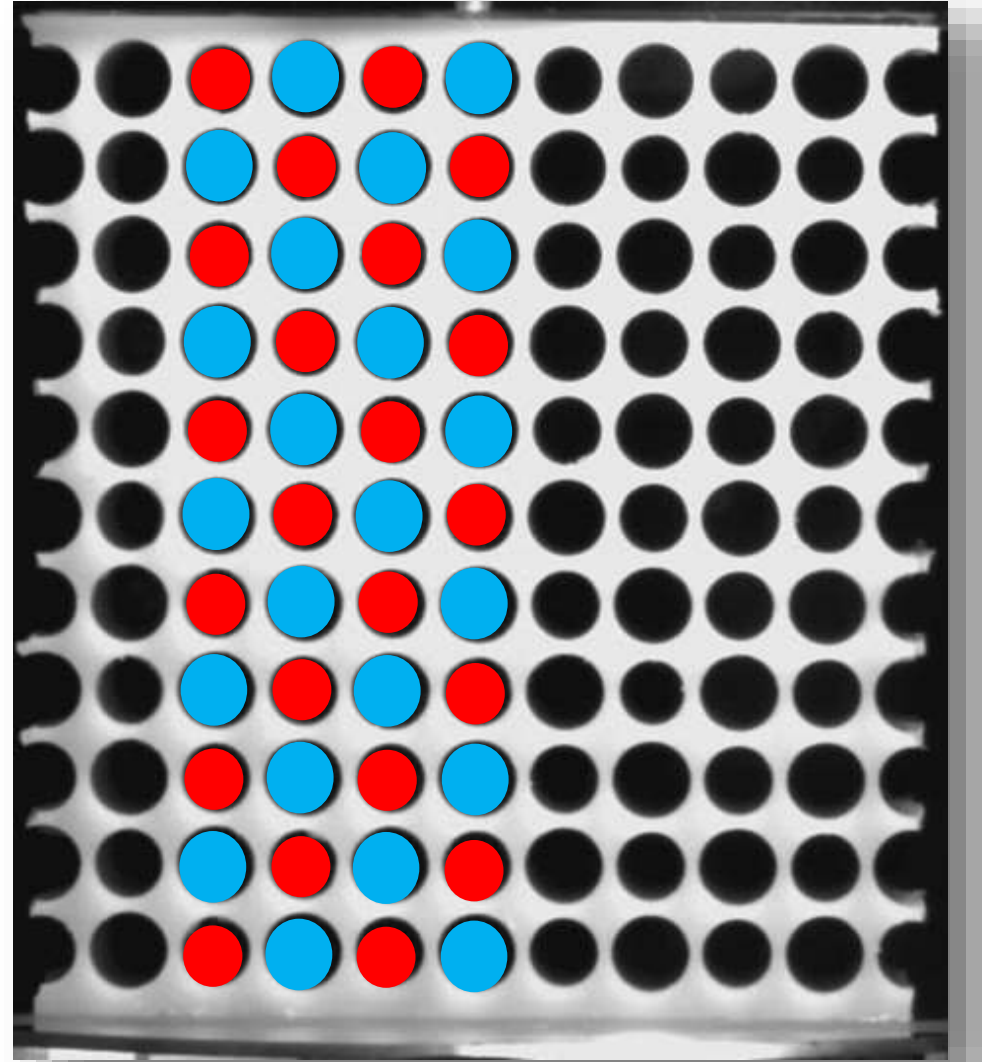
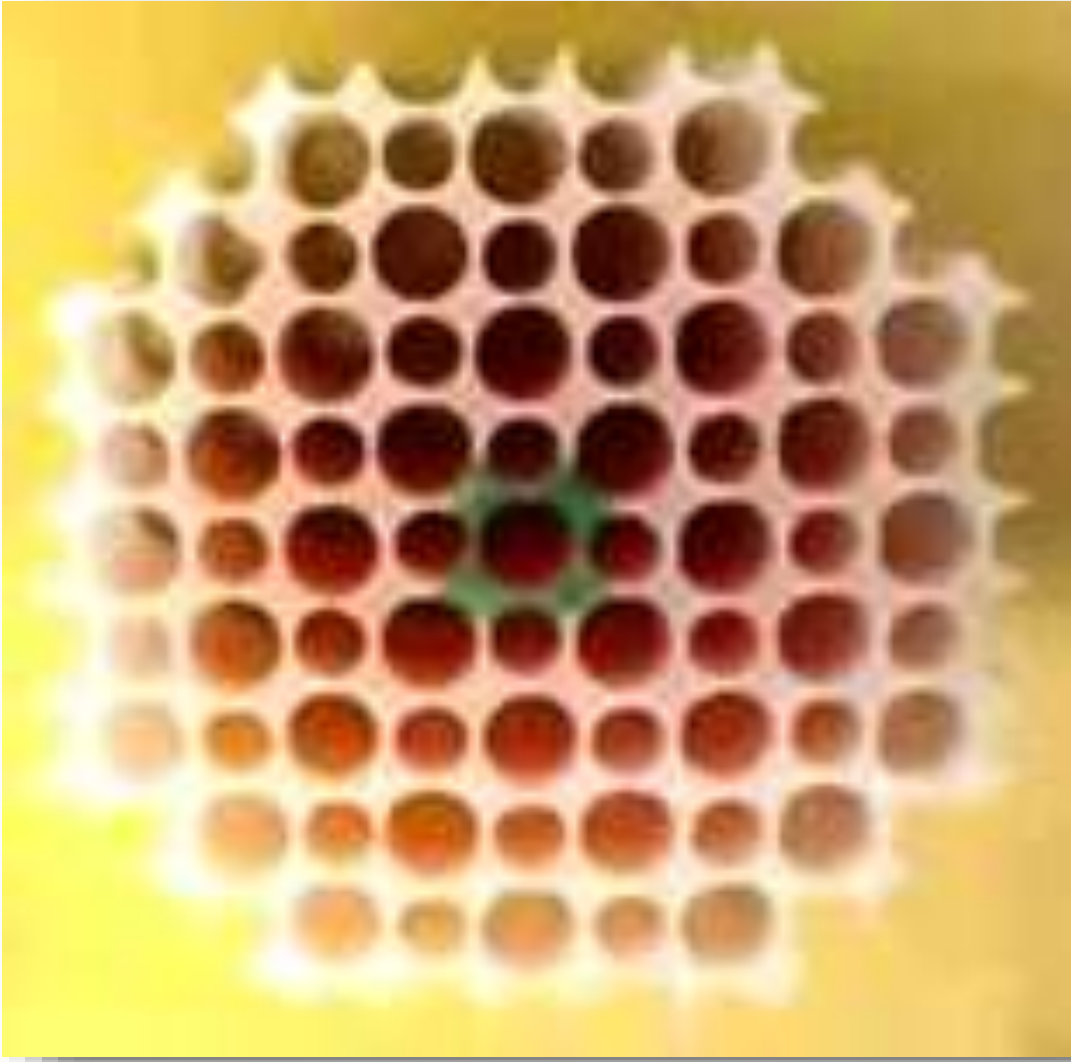
L. Lubbers, M. van Hecke and C. Coulais, in preparation (2016)



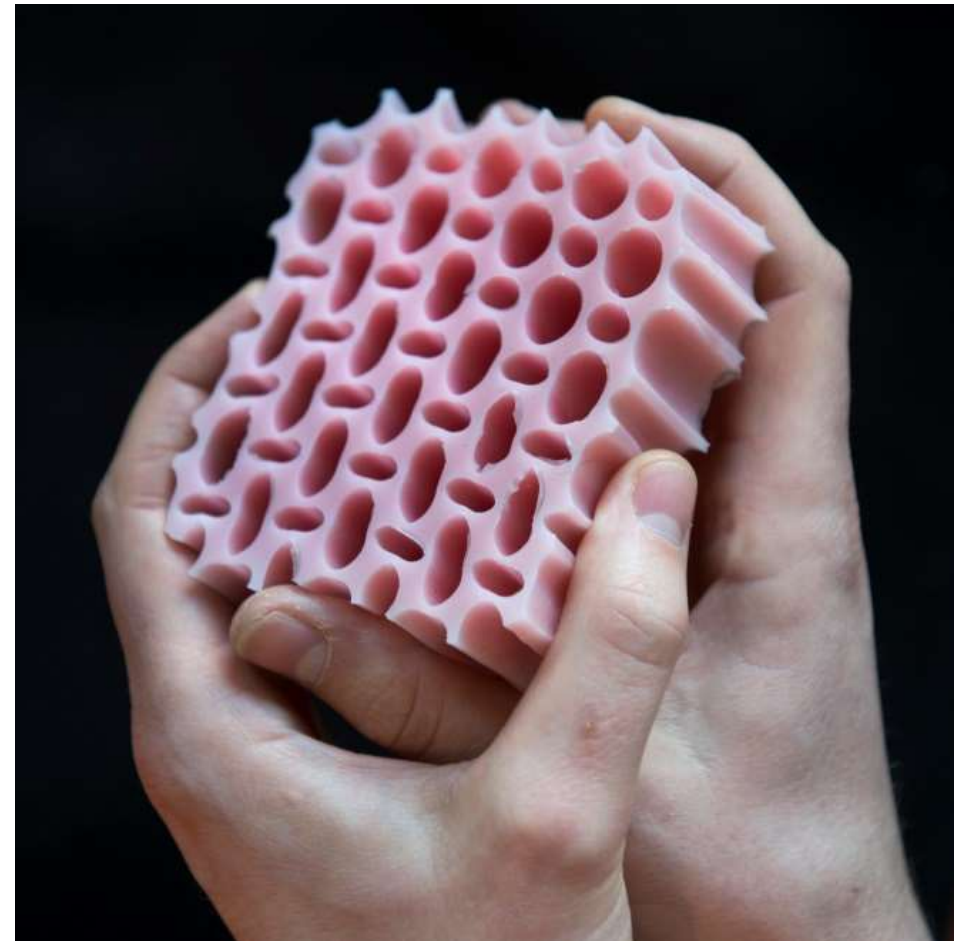
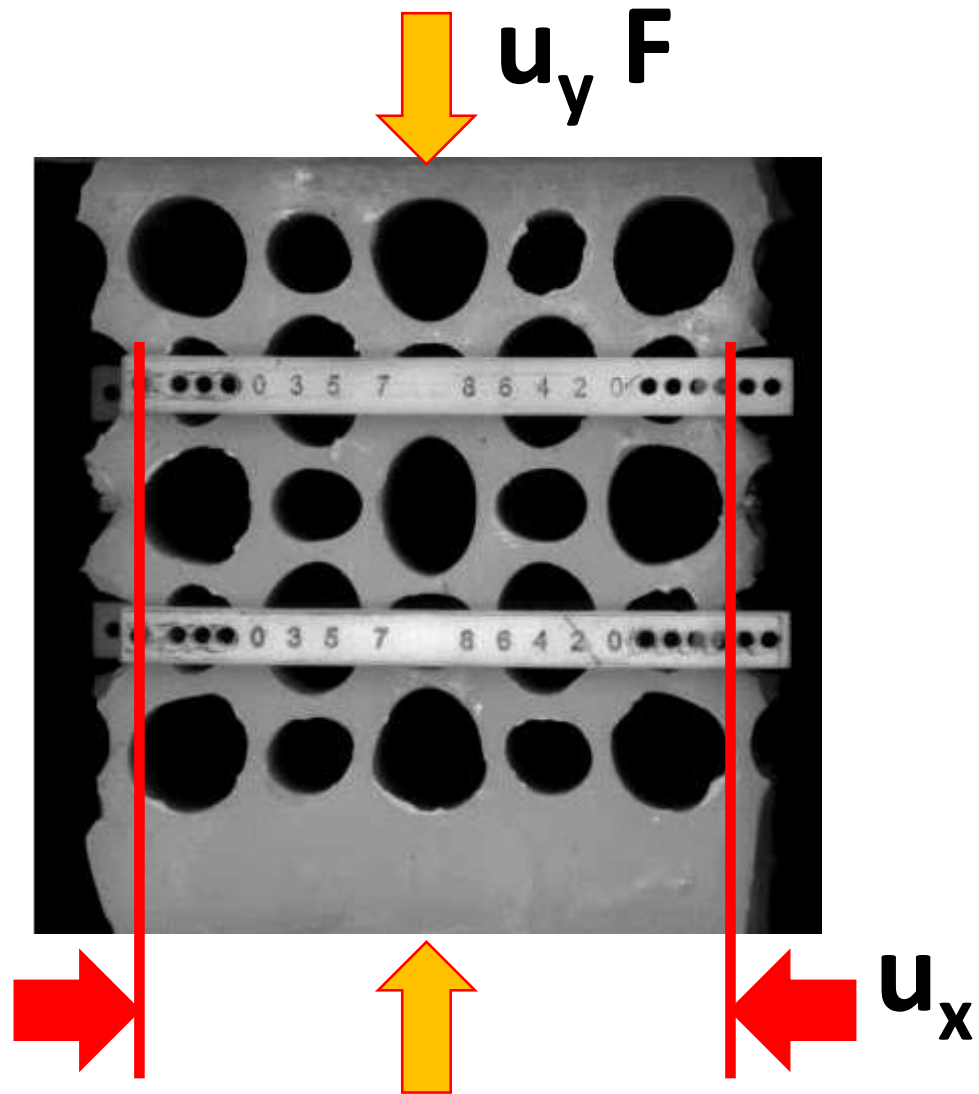
# Holey Sheets



# Holey Sheets

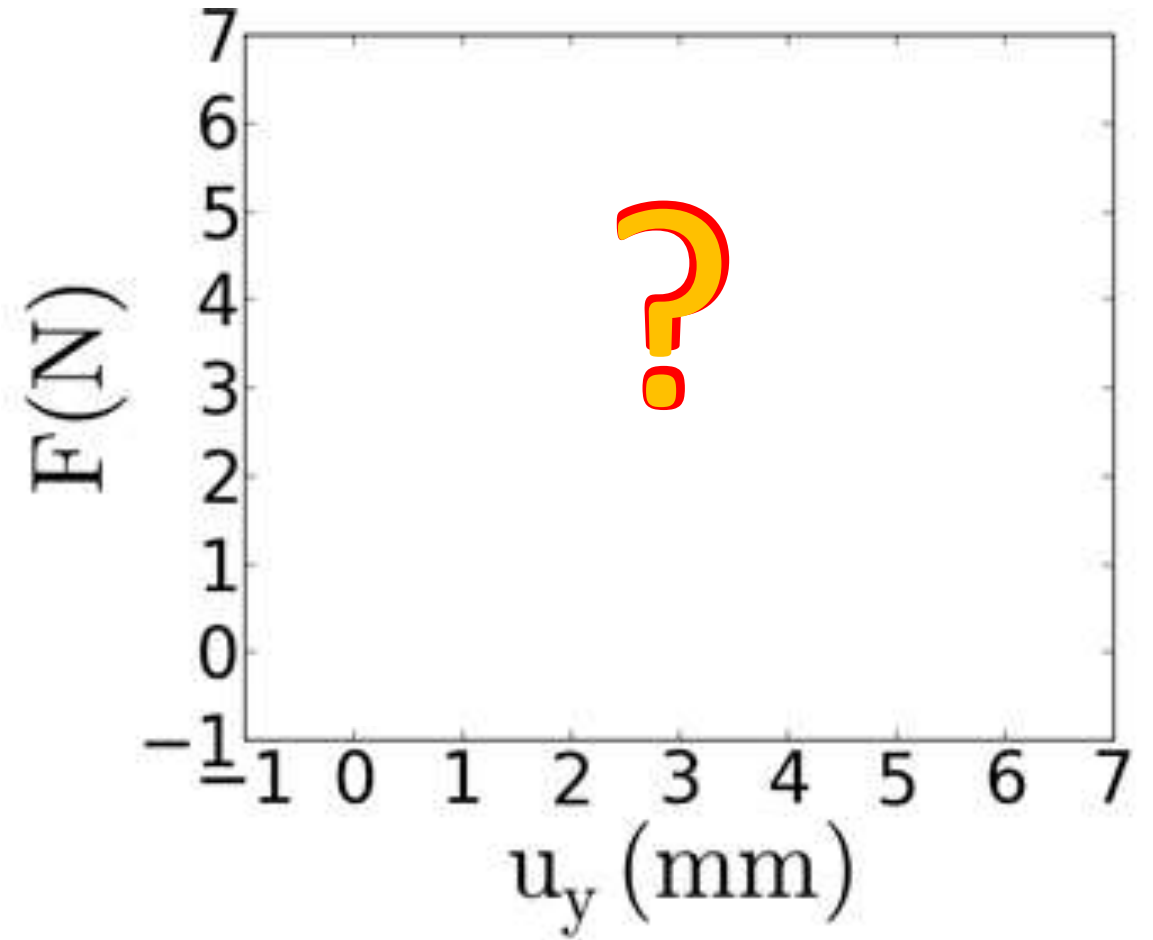
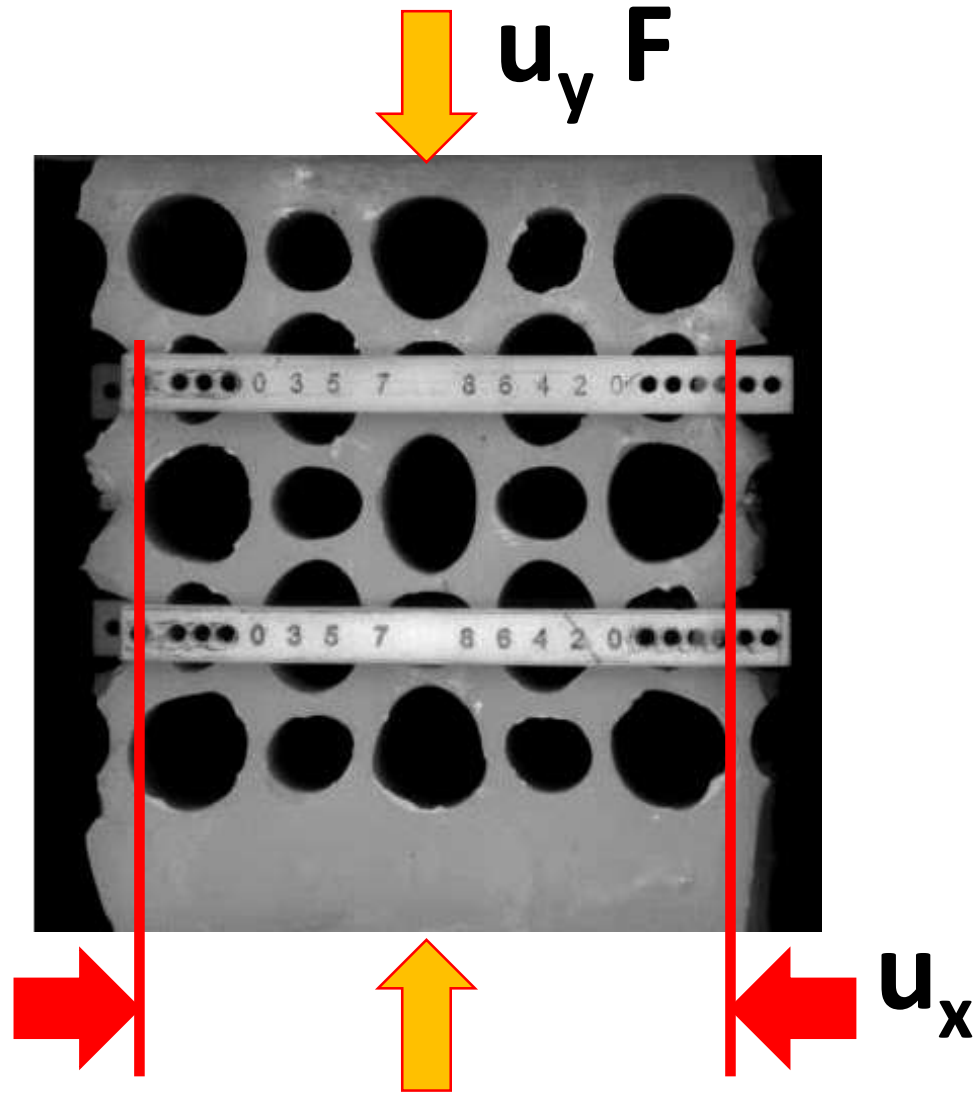


# Programmable through Clamping

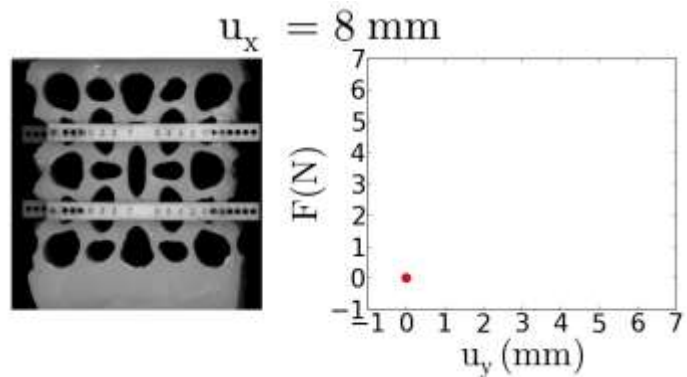
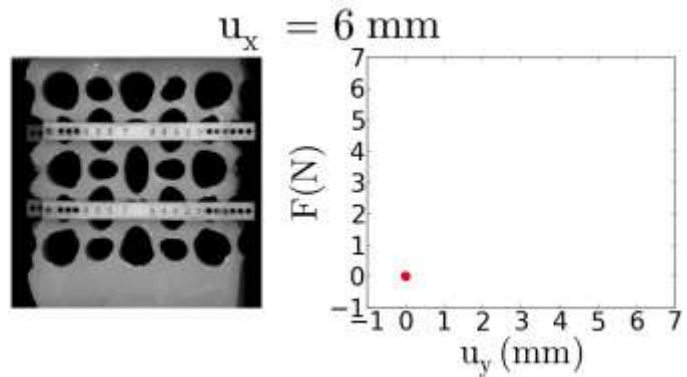
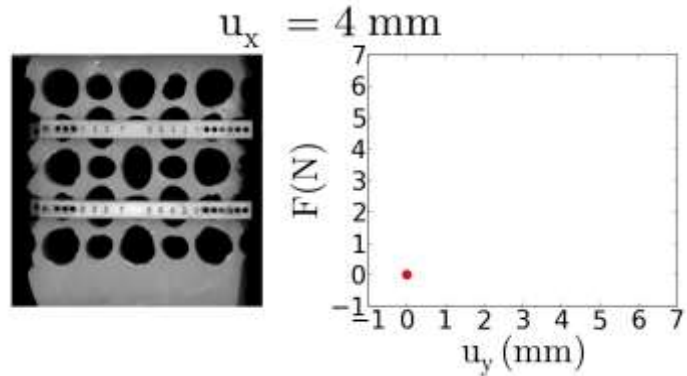




# Programmable through Clamping

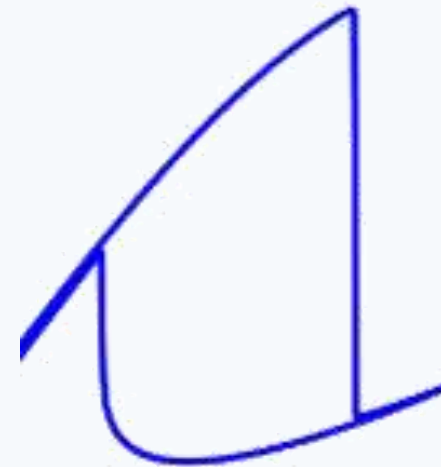


# Programmable through Clamping

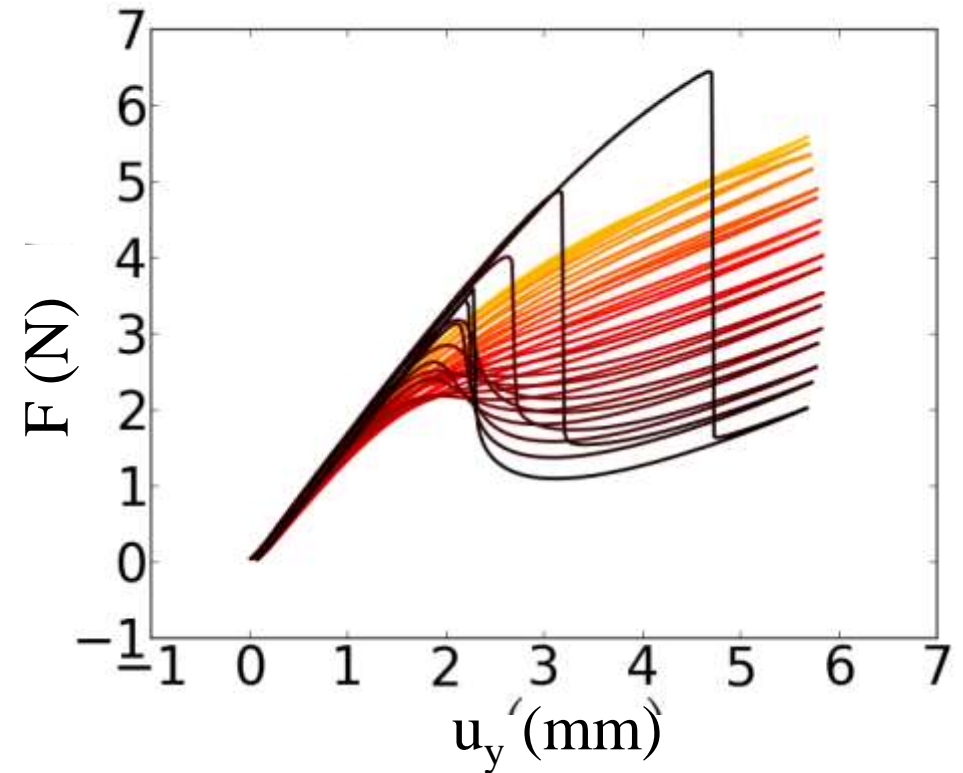
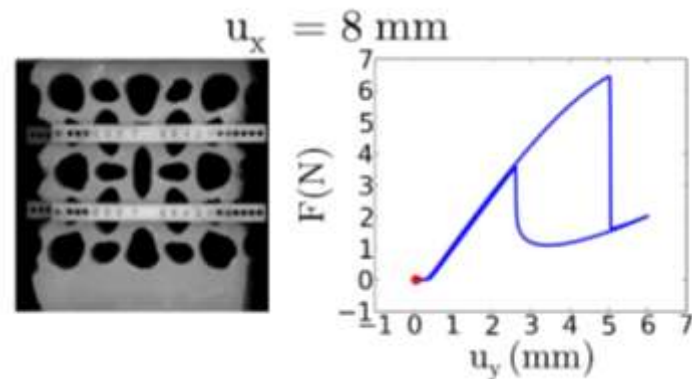
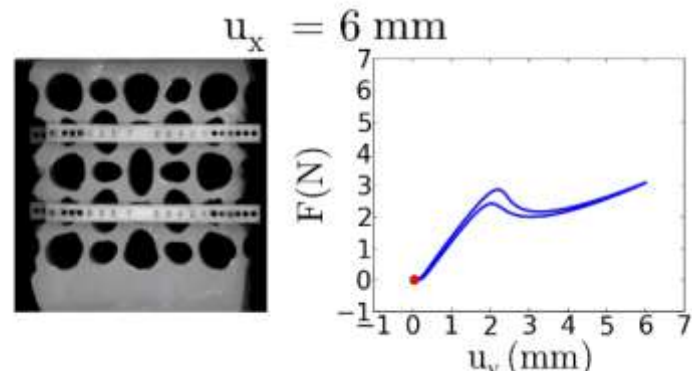
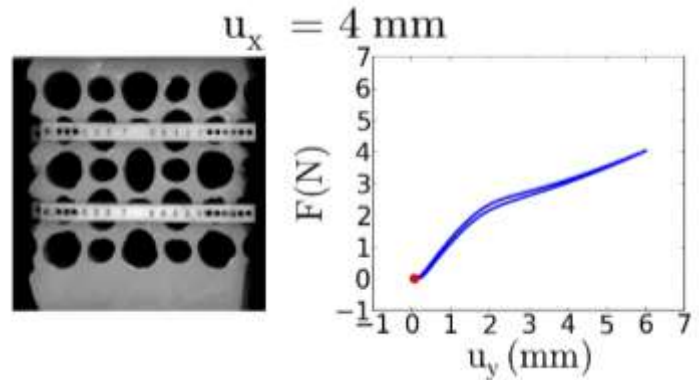


## Hysteresis

## Dissipation!



# Programmable through Clamping

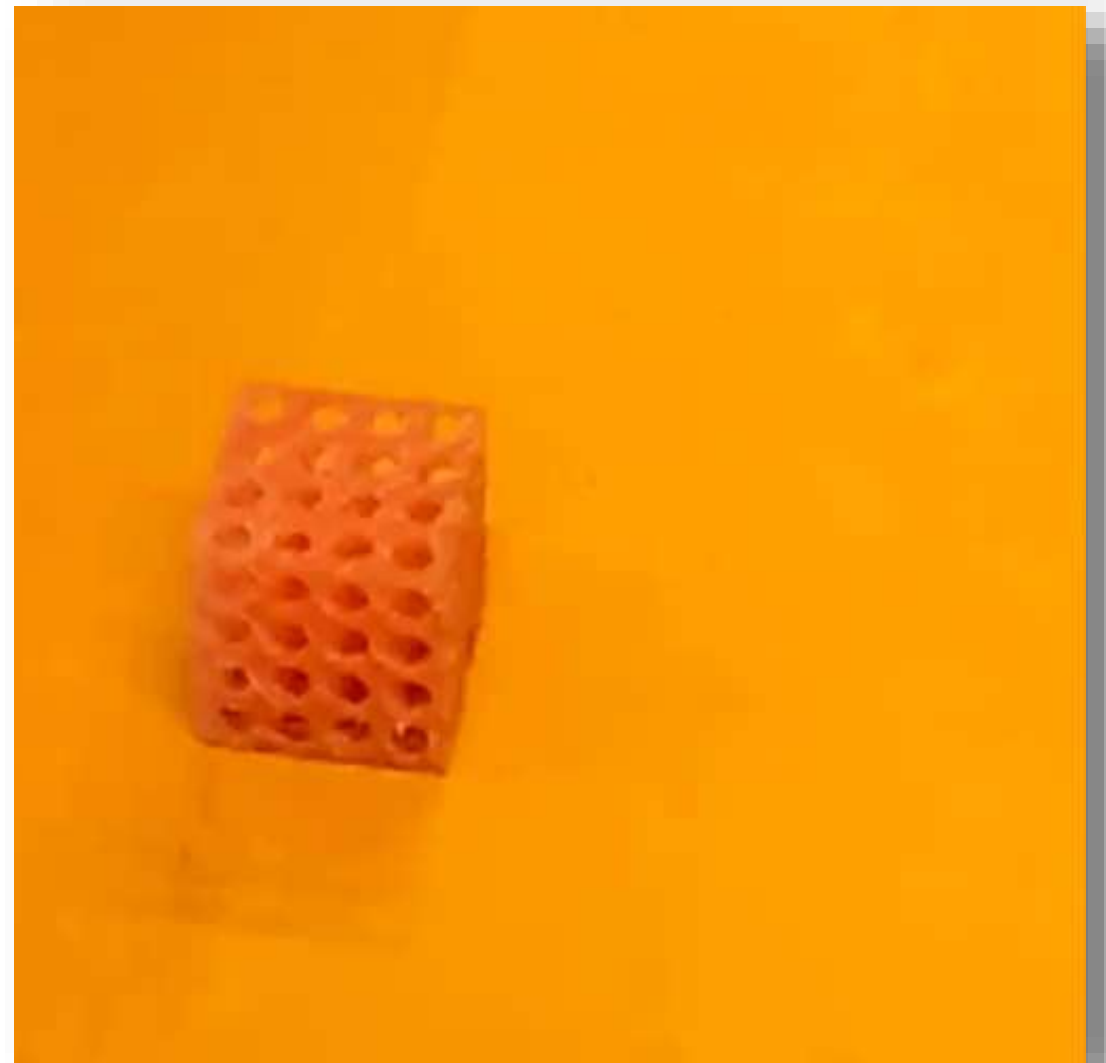
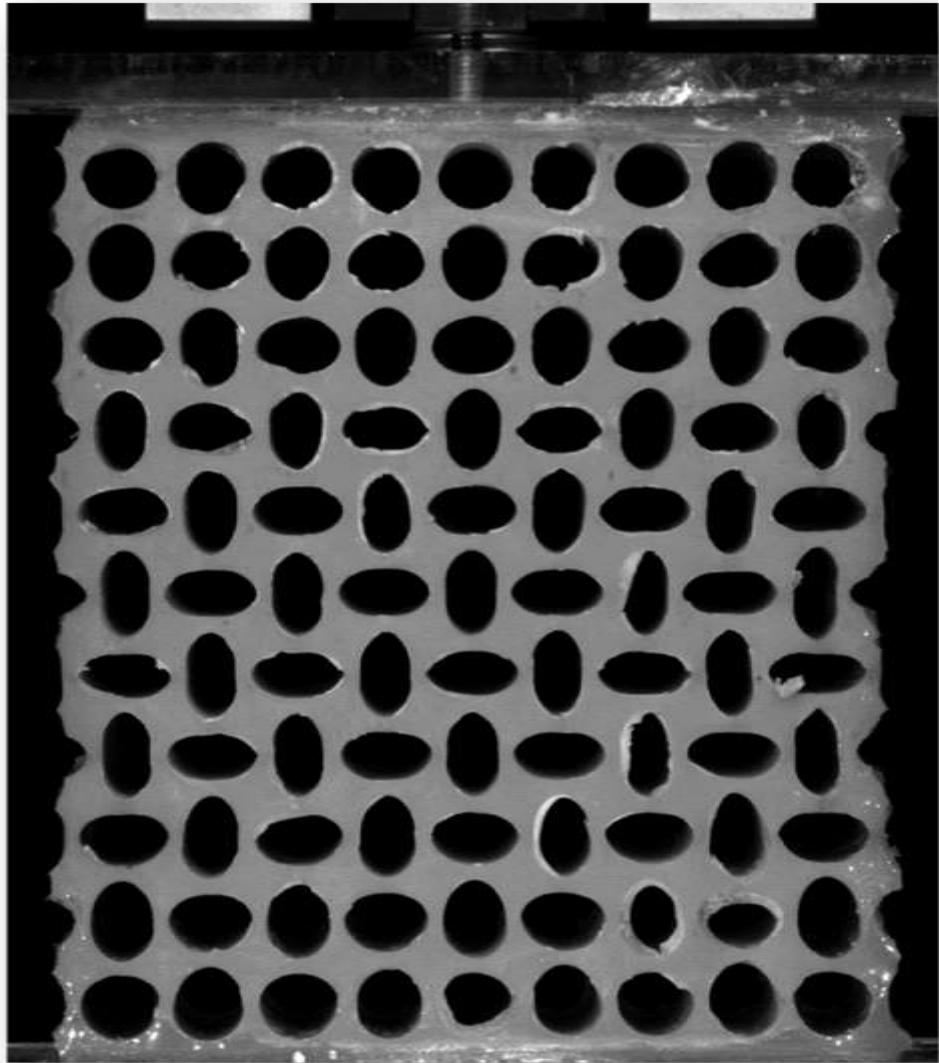


Florijn, Coulais, van Hecke, *PRL* **113** 175503 (2014)

Florijn, Coulais, van Hecke, in preparation (2016)

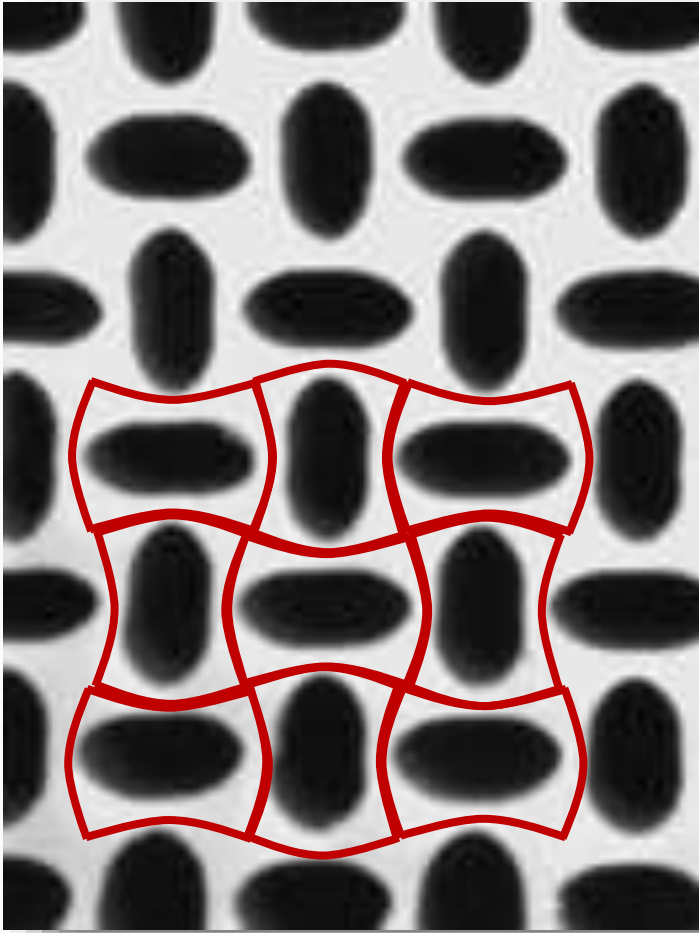


# 3D Metamaterials ?



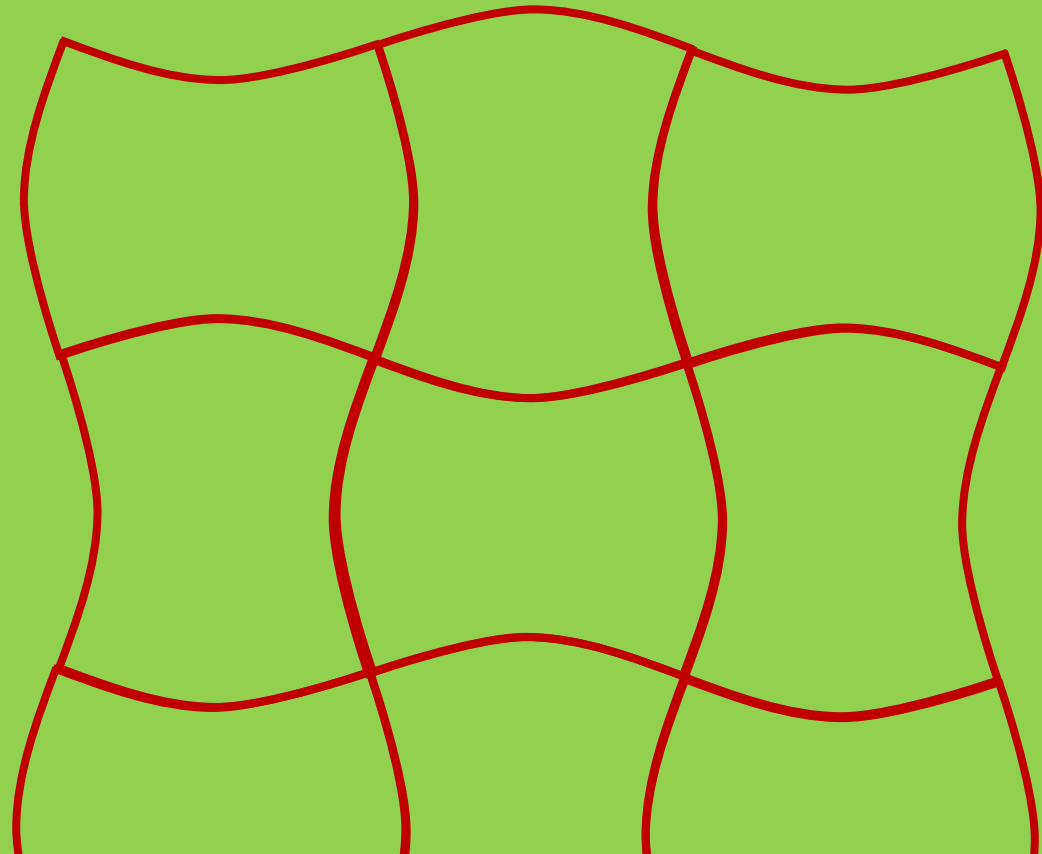
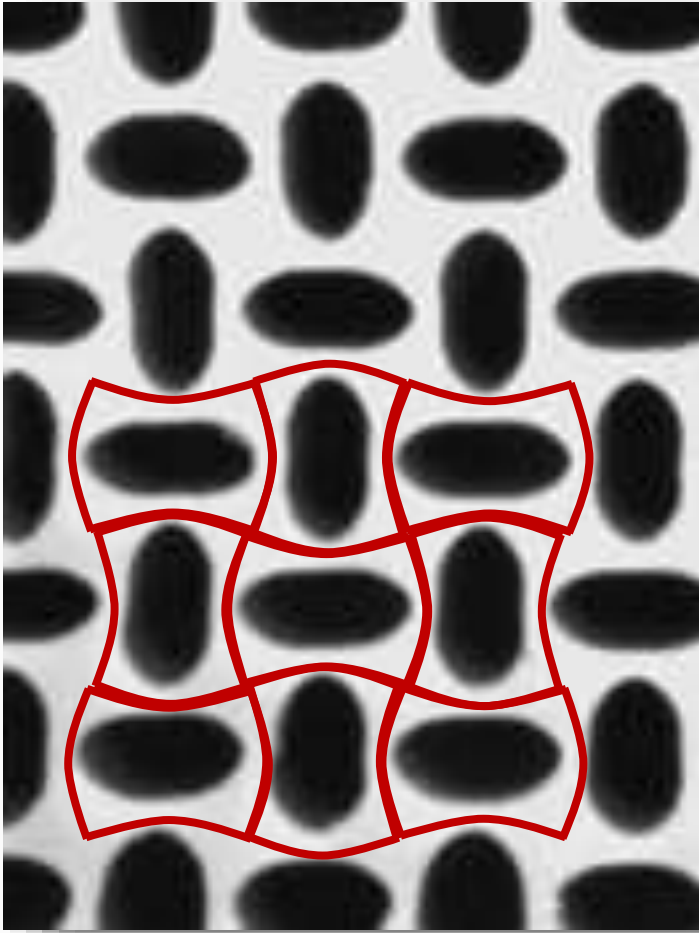
# 3D Metamaterials ?

Pores Deformation



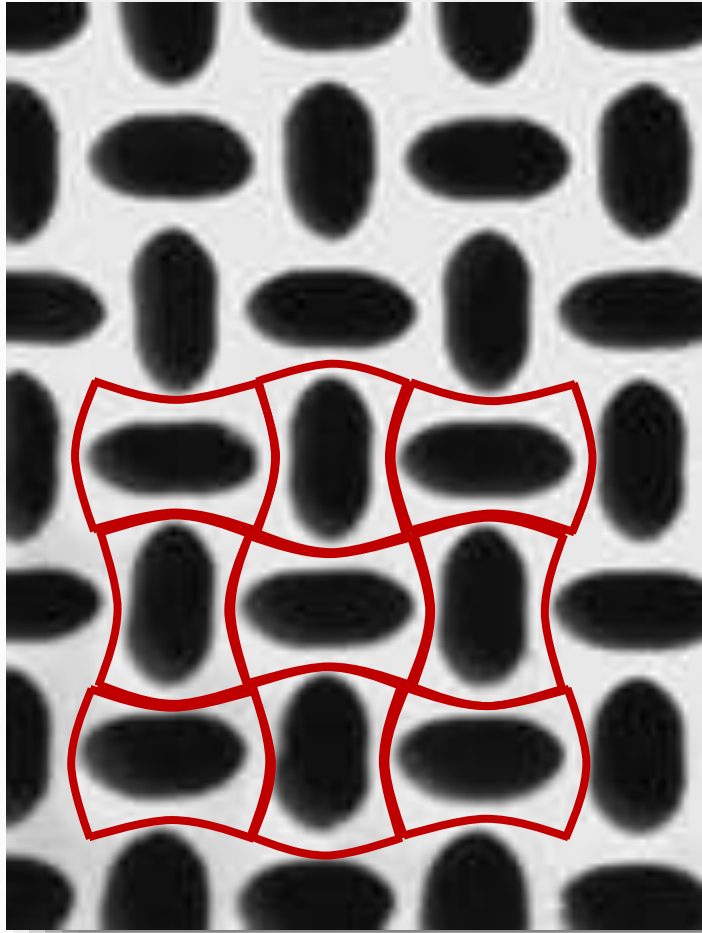
# 3D Metamaterials ?

Pores Deformation

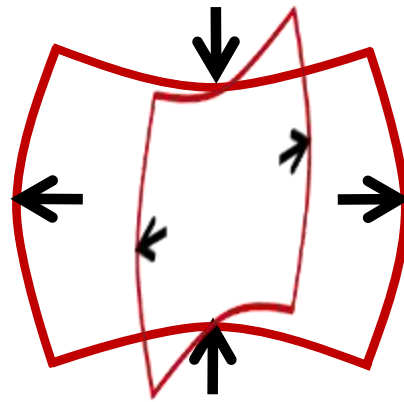


# 3D Metamaterials ?

Pores Deformation



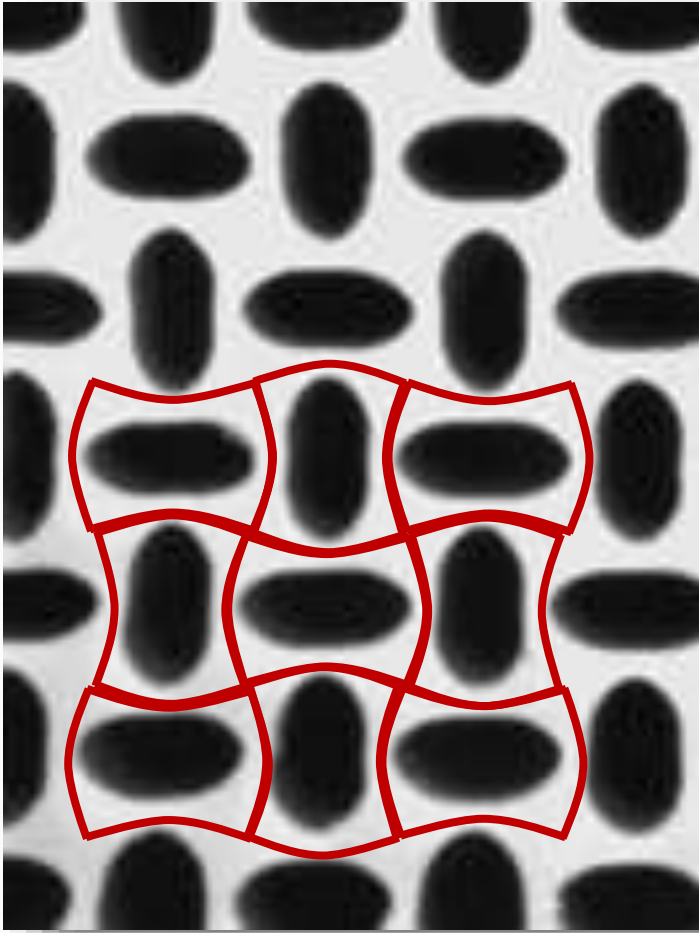
Make it 3D!



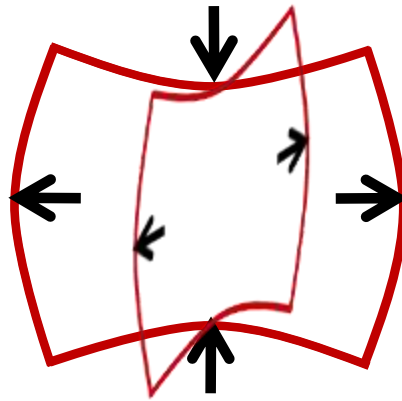


# 3D Metamaterials ?

Pores Deformation



Make it 3D!

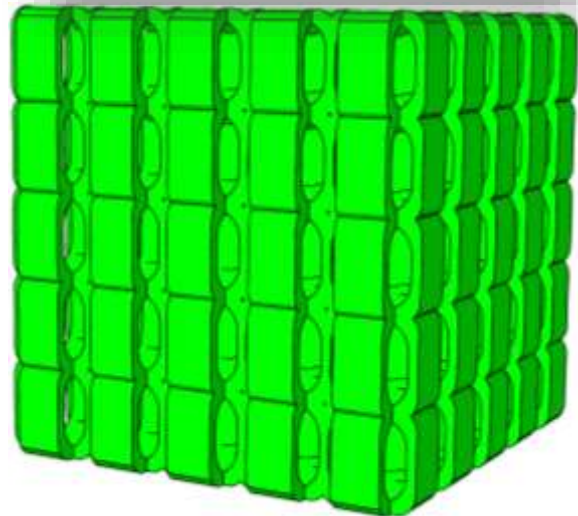


3D Flexible Block

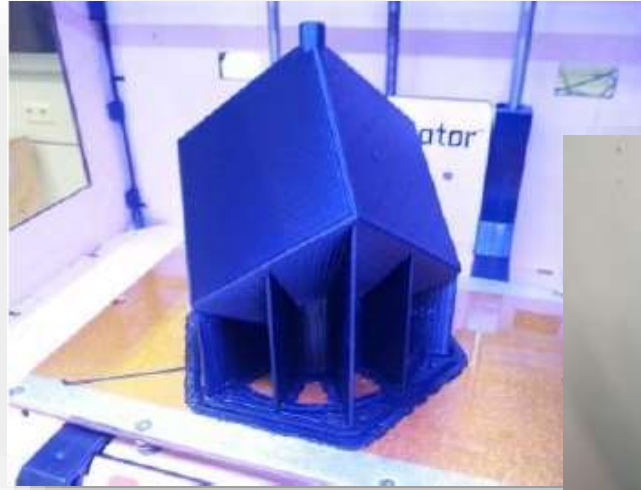


# 3D Metamaterials

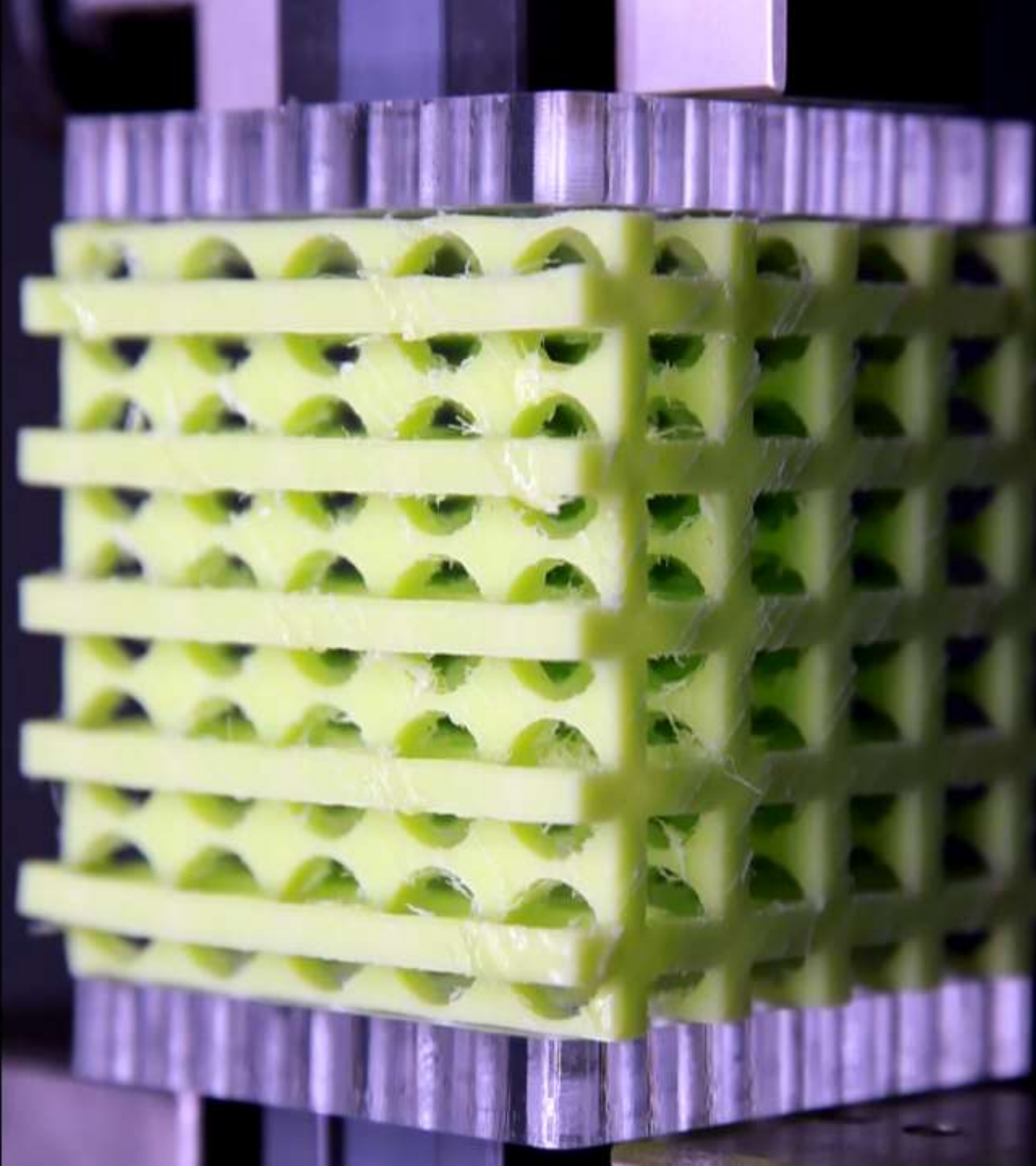
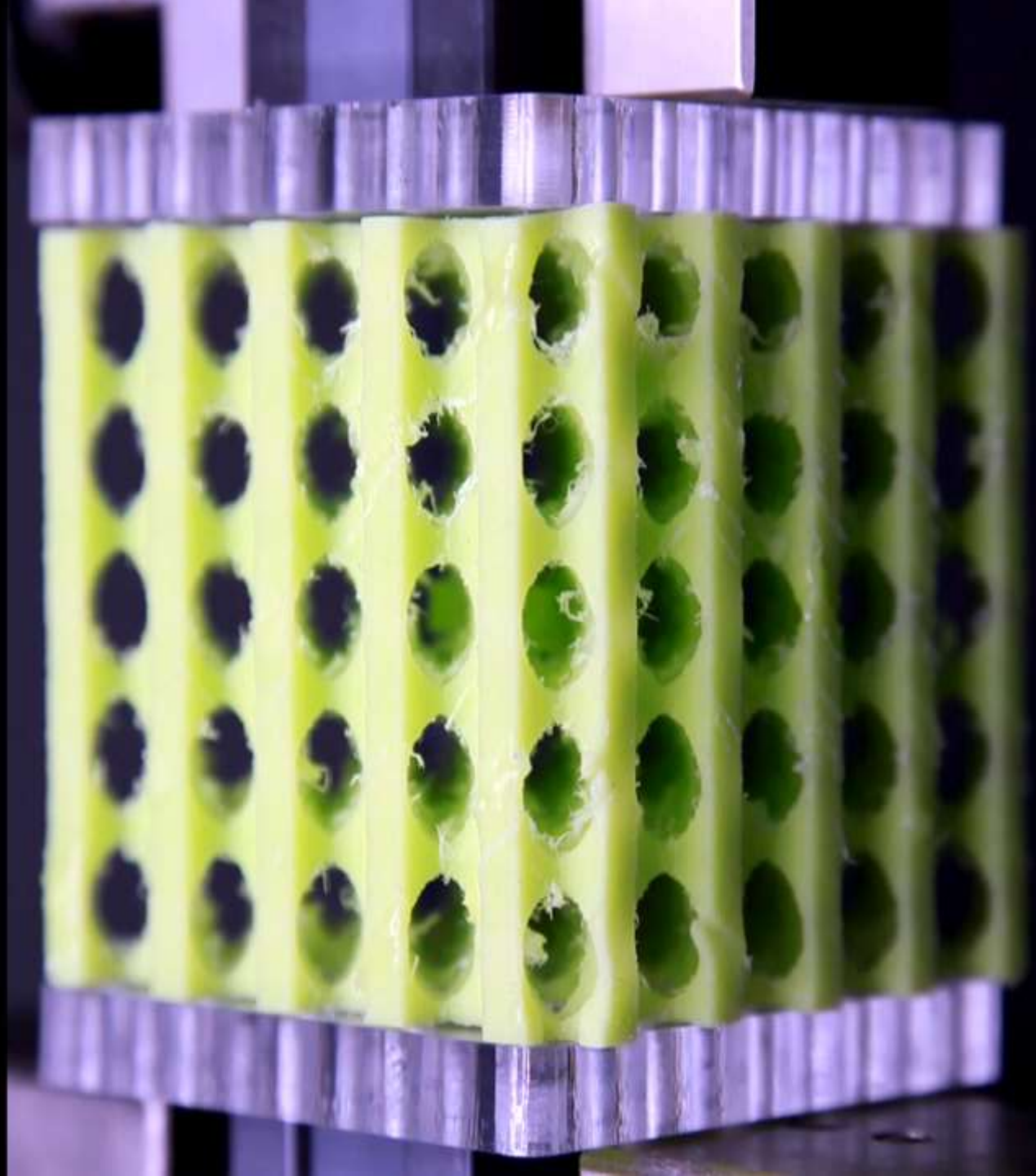
## Conception



## Fabrication

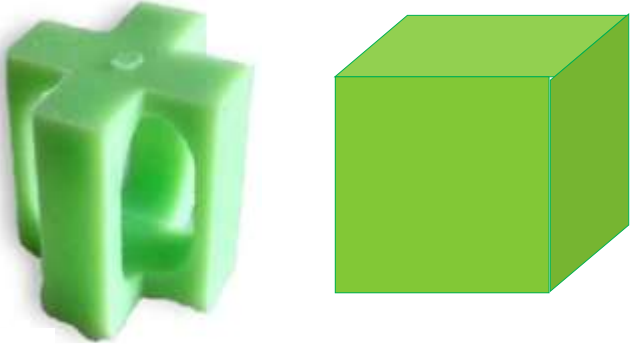




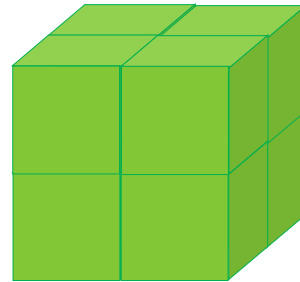


# 3D Metamaterials

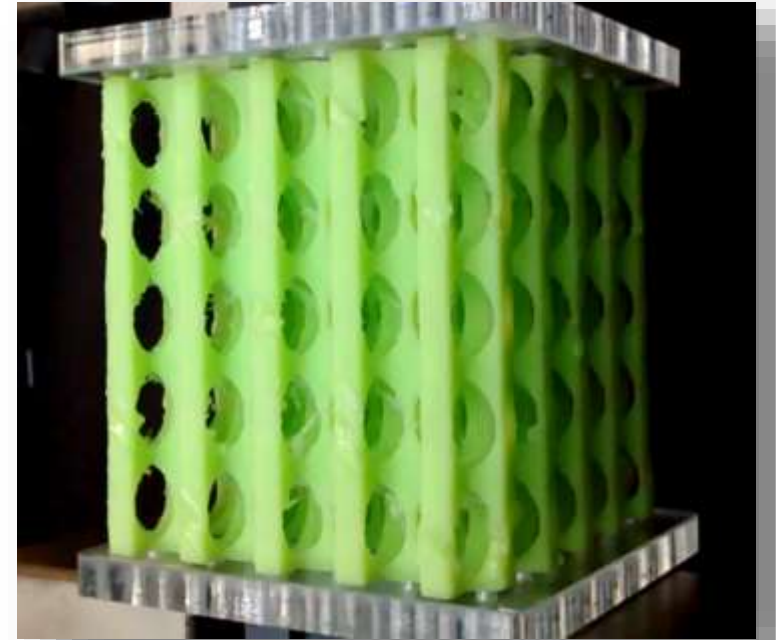
1 Flexible *Block*



Periodic Stacking



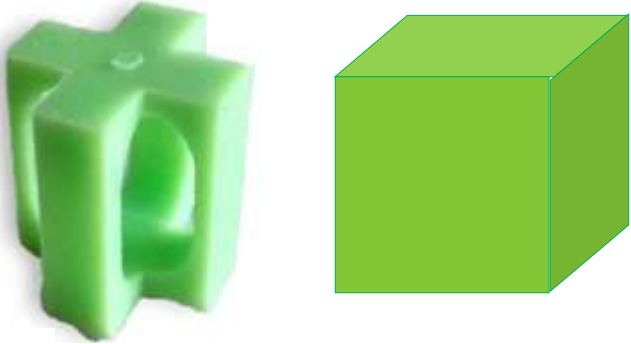
3D printed  
Metacube



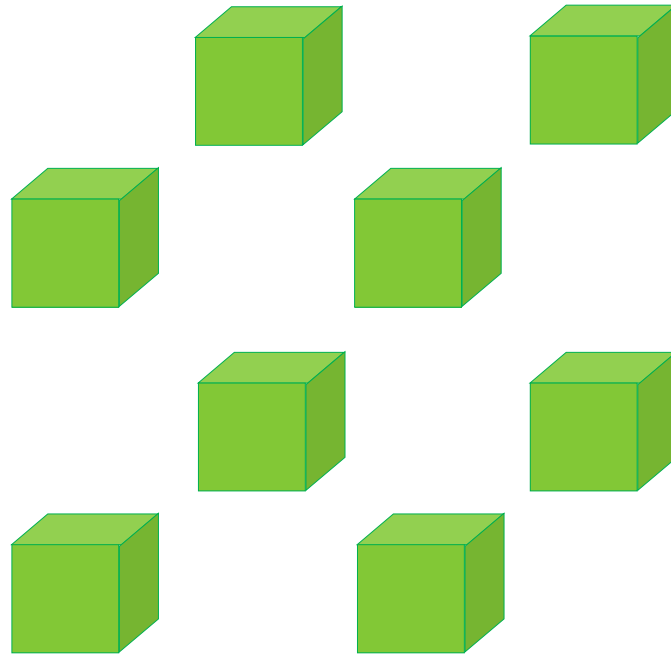


# 3D Metamaterials

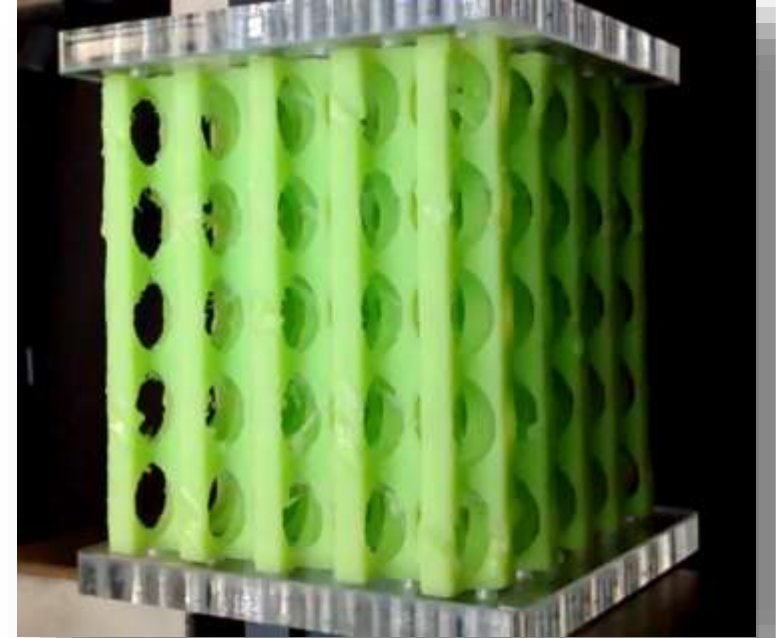
1 Flexible *Block*



Periodic Stacking

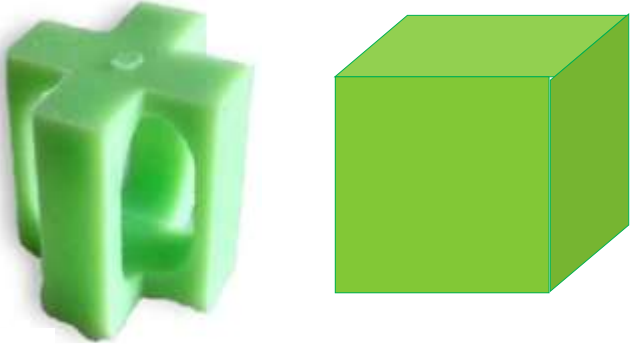


3D printed  
Metacube

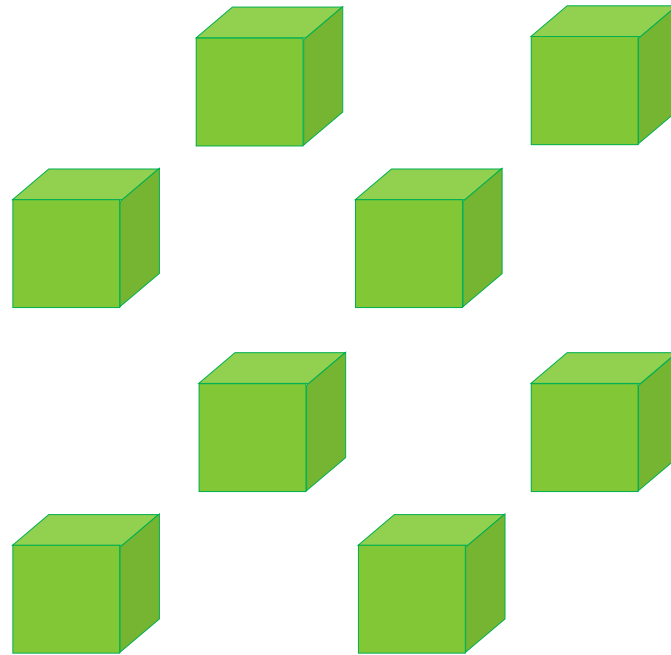


# 3D Metamaterials

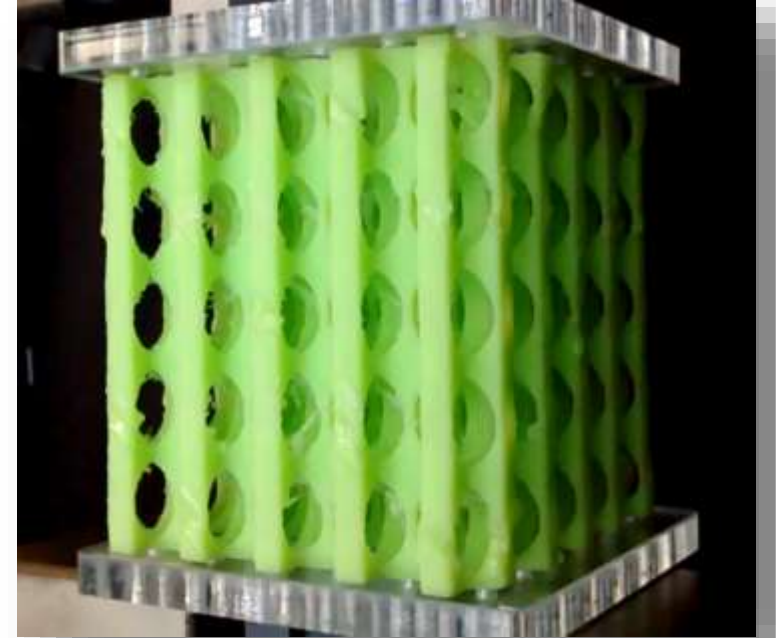
1 Flexible *Block*



Periodic Stacking

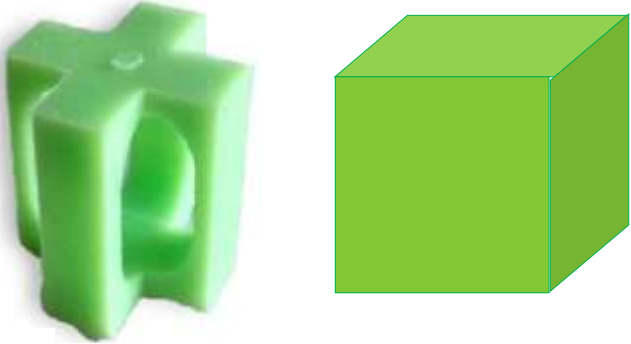


3D printed  
Metacube

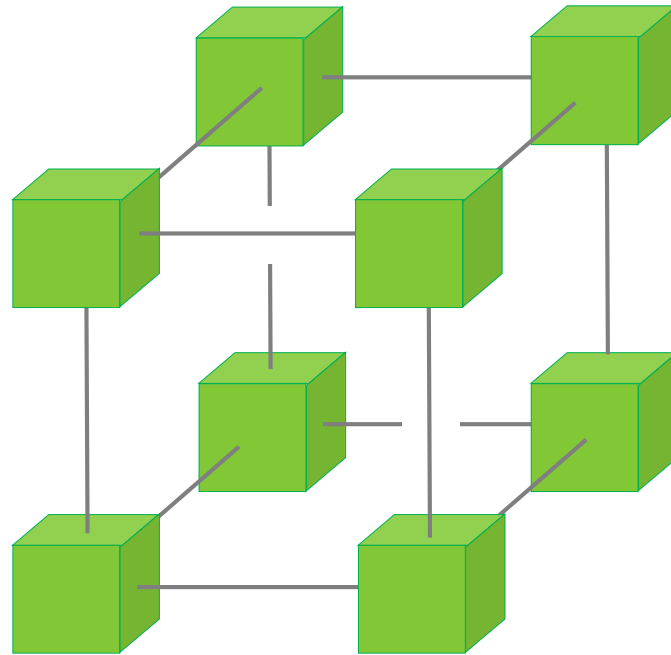


# 3D Metamaterials

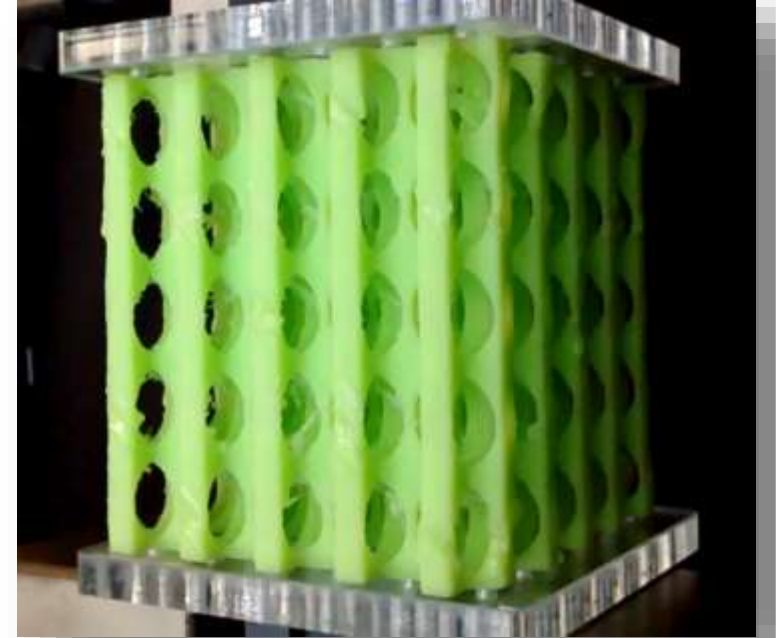
1 Flexible *Block*



Periodic Stacking

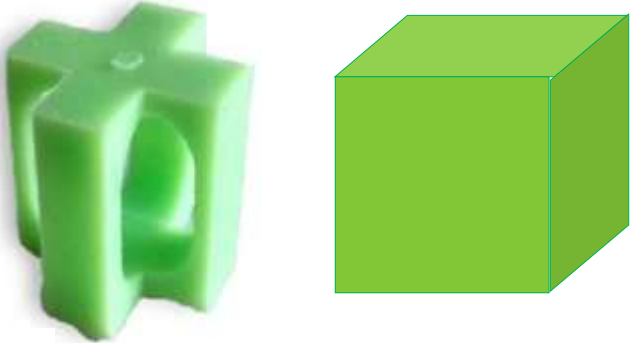


3D printed Metacube

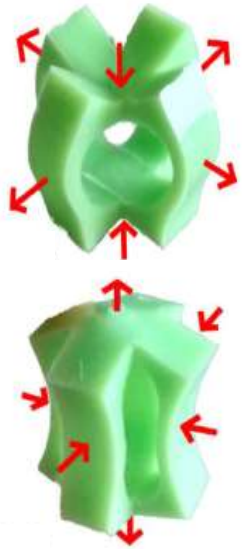


# 3D Metamaterials

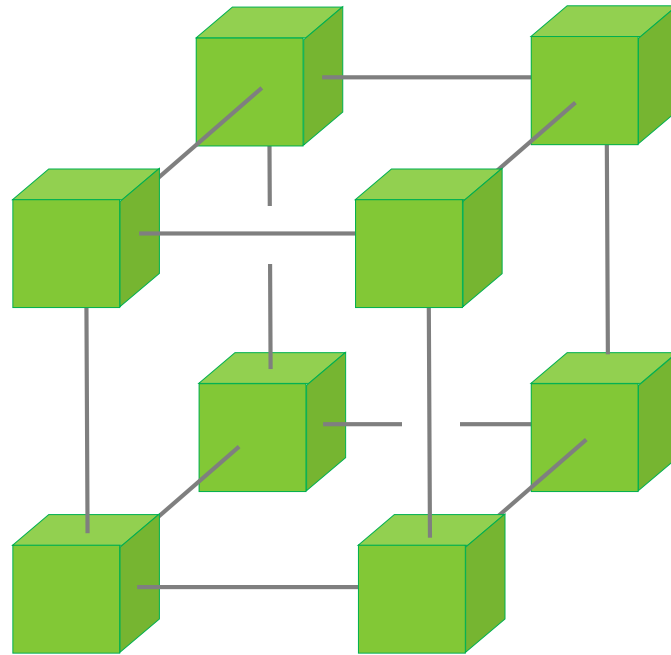
1 Flexible *Block*



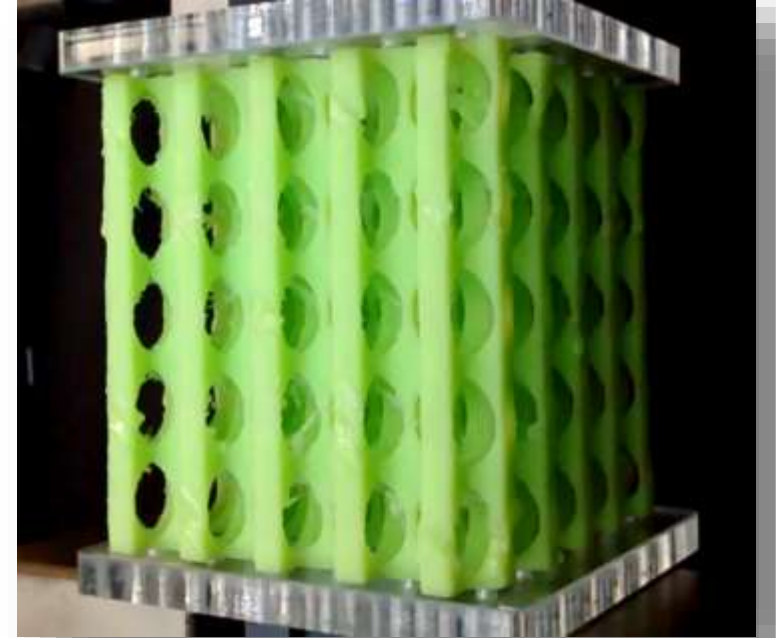
2 Deformed *Bricks*



Periodic Stacking



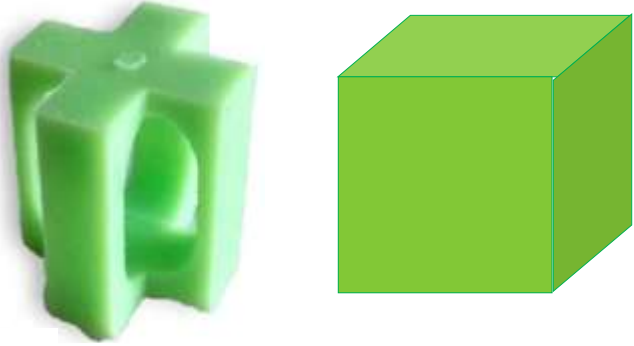
3D printed  
Metacube



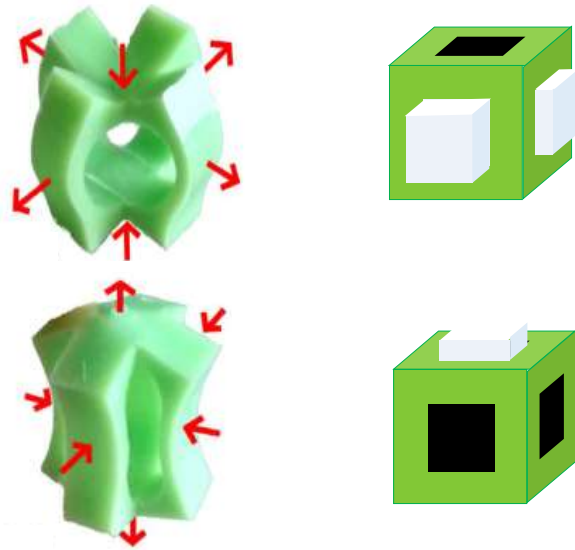


# 3D Metamaterials

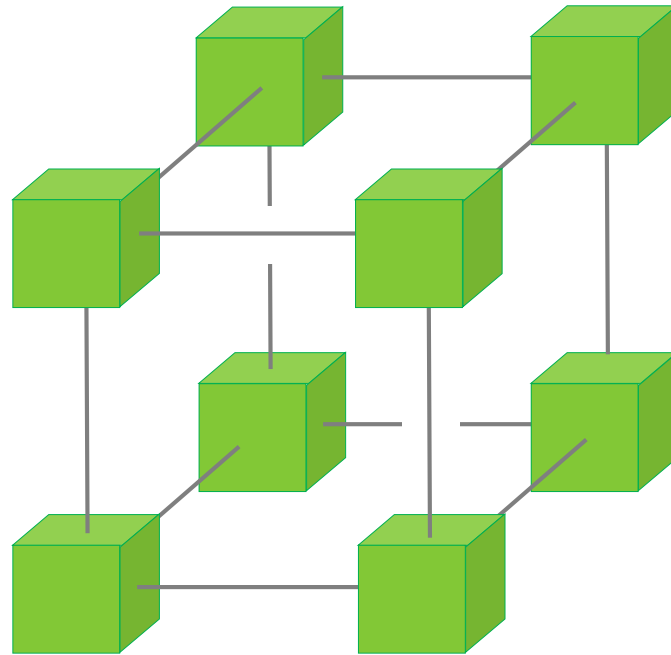
1 Flexible *Block*



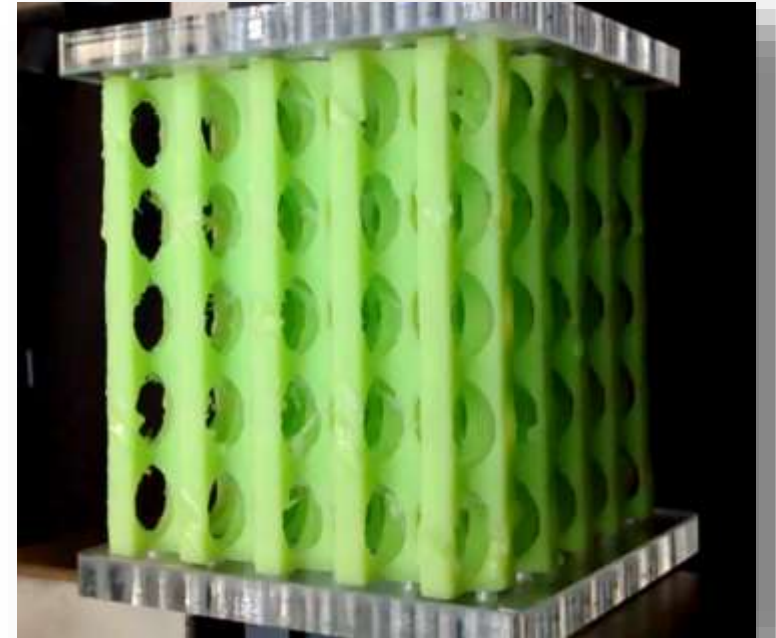
2 Deformed *Bricks*



Periodic Stacking

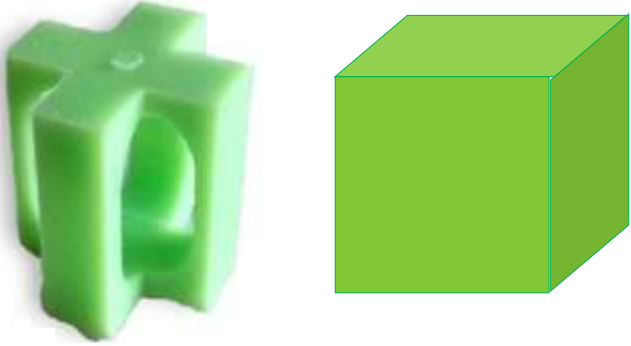


3D printed Metacube

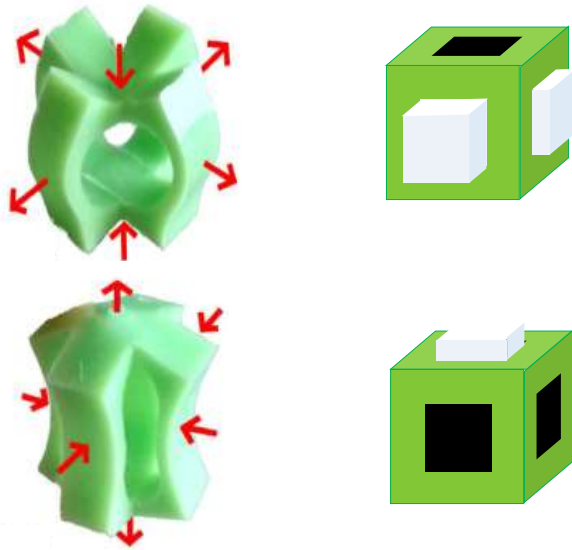


# 3D Metamaterials

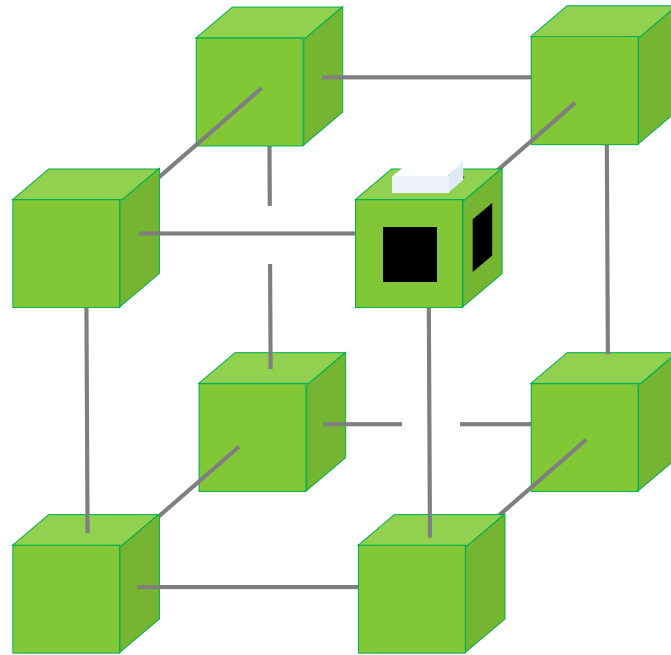
1 Flexible *Block*



2 Deformed *Bricks*

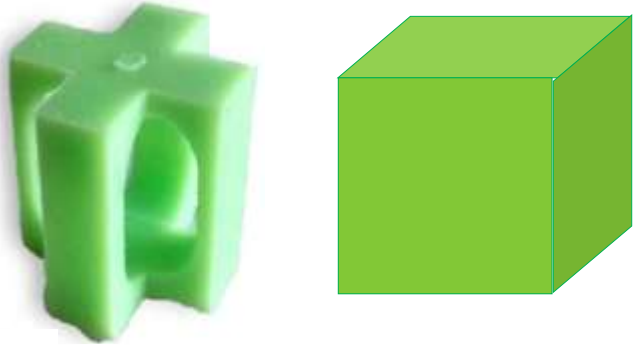


Periodic Stacking

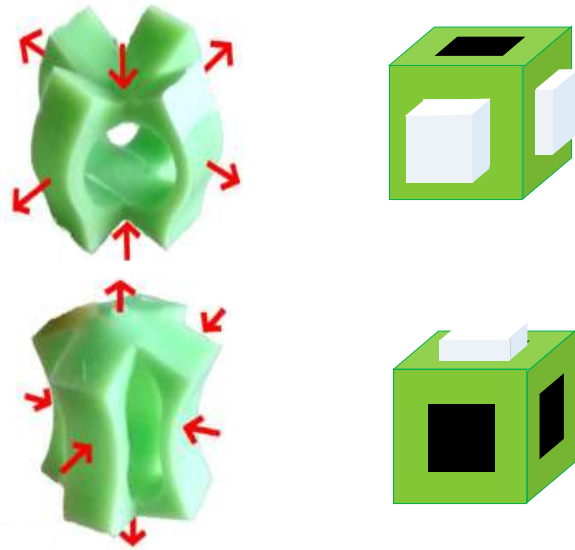


# 3D Metamaterials

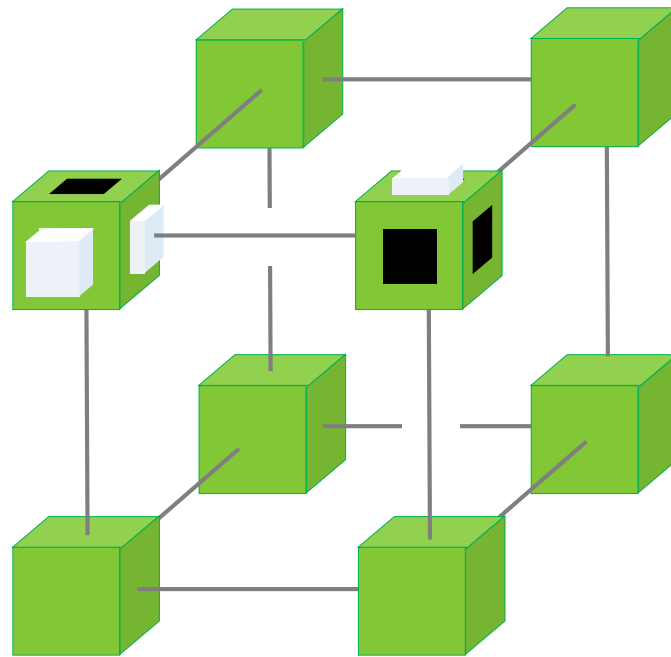
1 Flexible *Block*



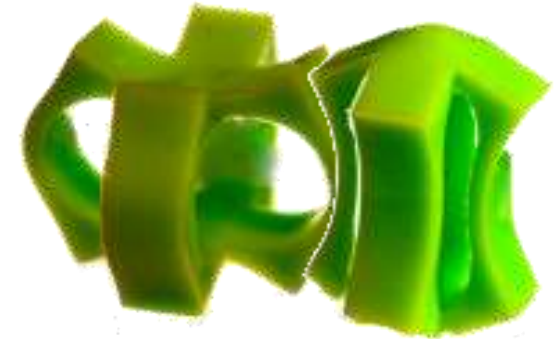
2 Deformed *Bricks*



Periodic Stacking

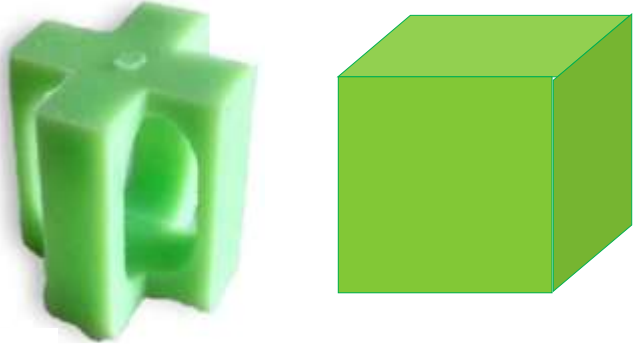


The bricks fit!

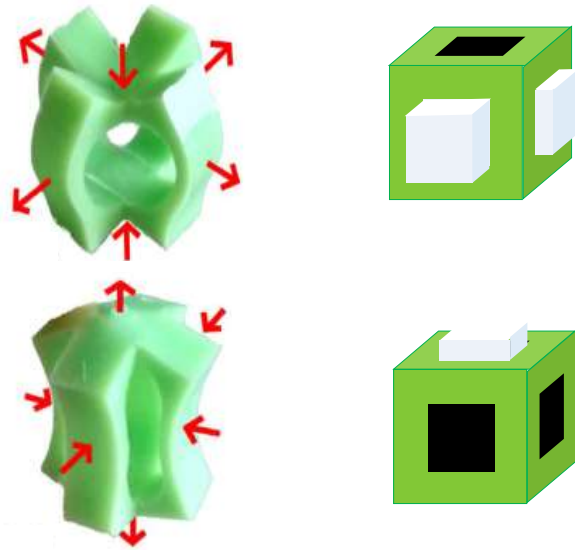


# 3D Metamaterials

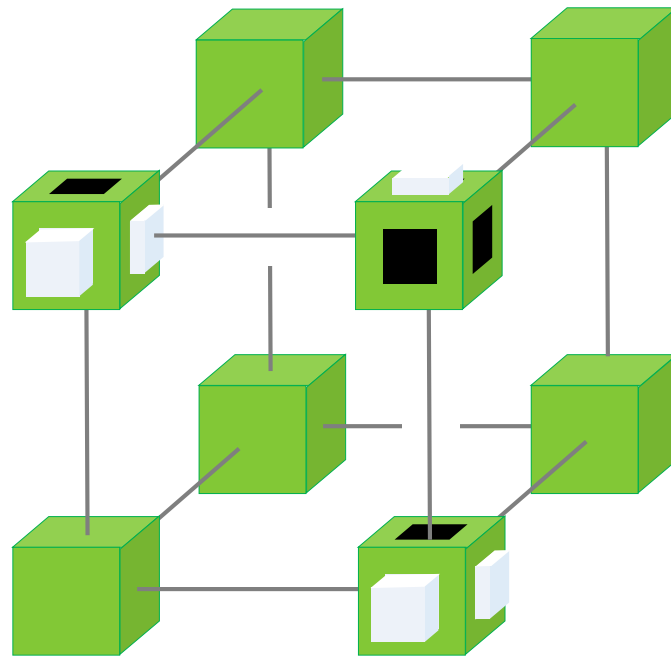
1 Flexible *Block*



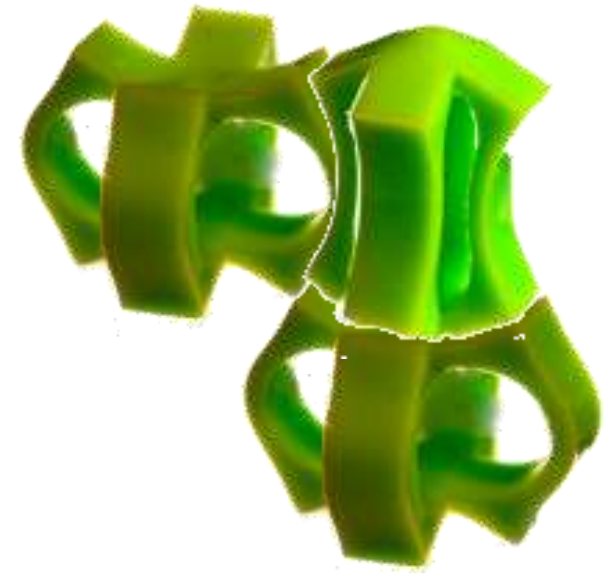
2 Deformed *Bricks*



Periodic Stacking



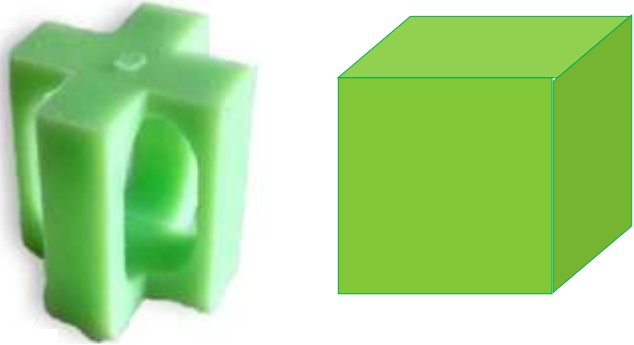
The bricks fit!



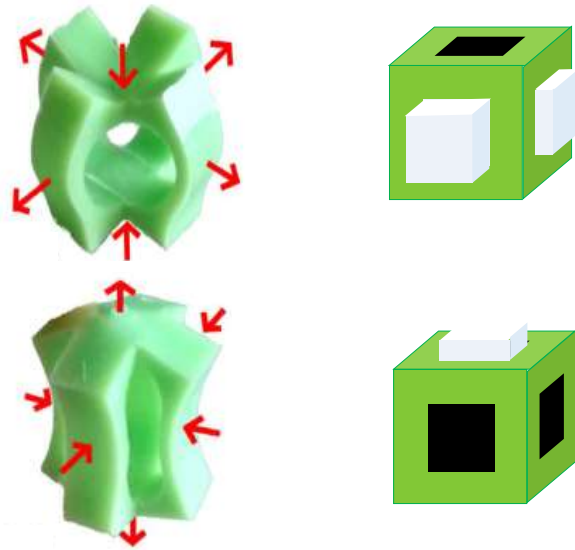


# 3D Metamaterials

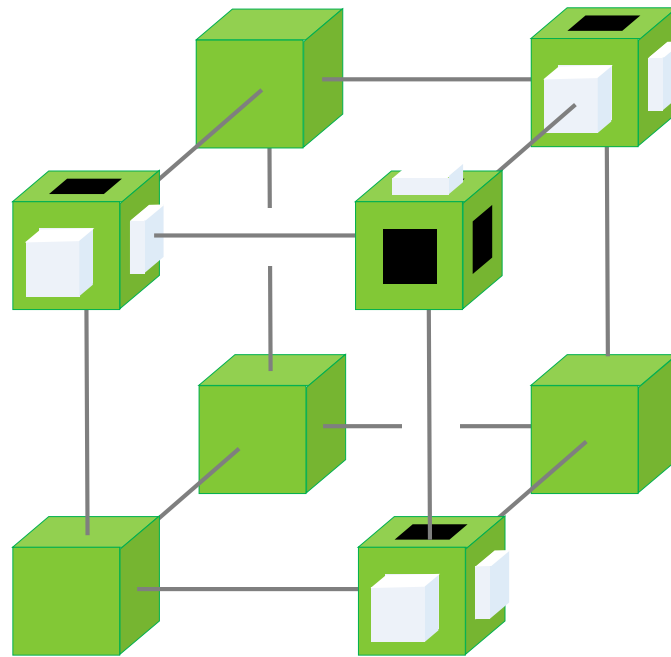
1 Flexible *Block*



2 Deformed *Bricks*



Periodic Stacking

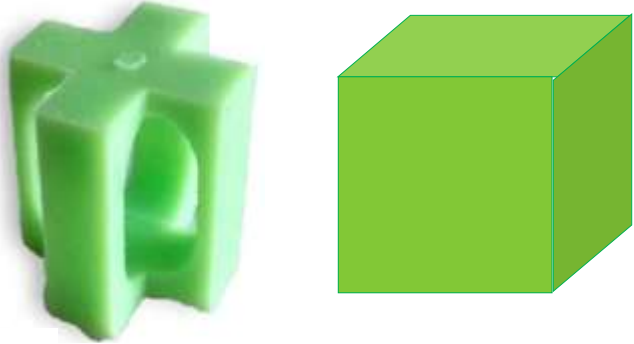


The bricks fit!

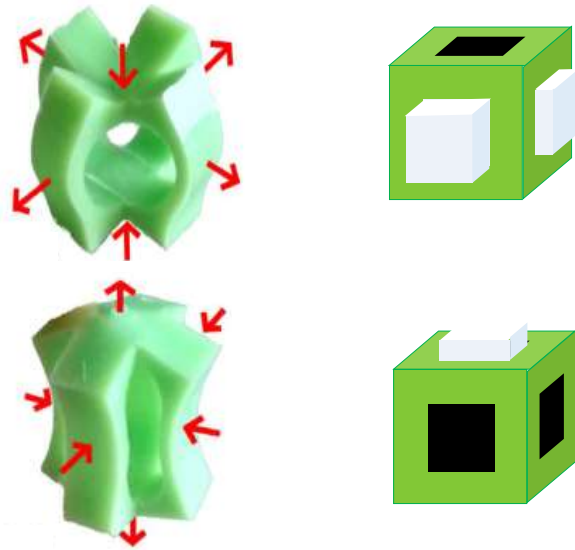


# 3D Metamaterials

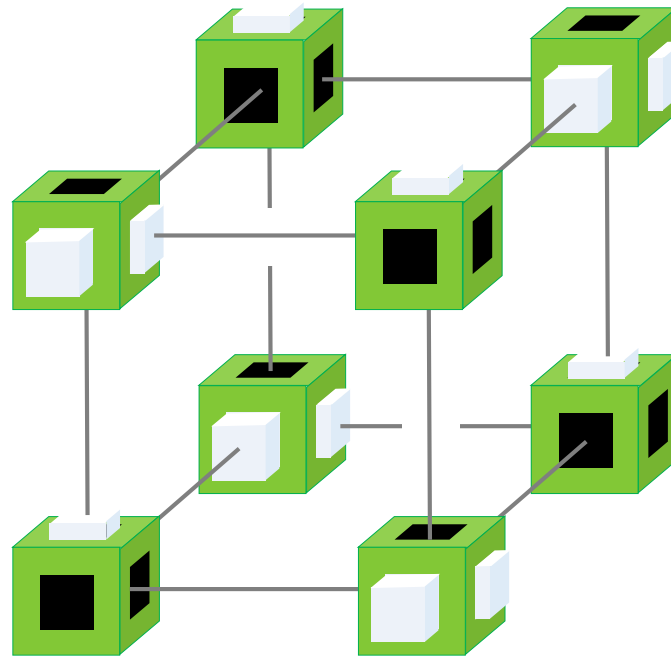
1 Flexible *Block*



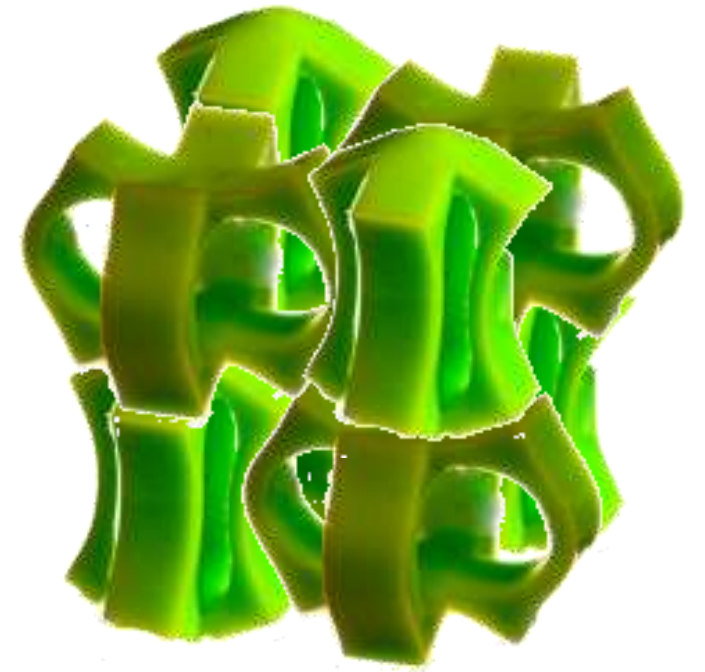
2 Deformed *Bricks*



Periodic Stacking

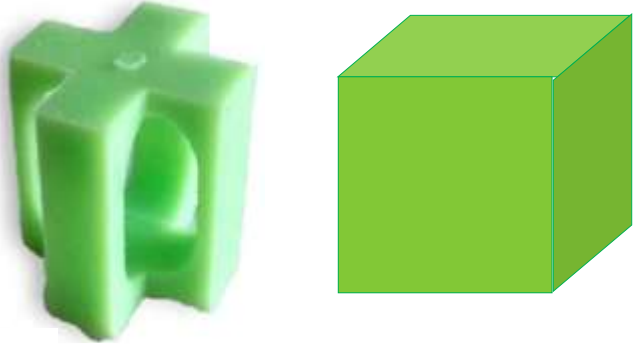


The bricks fit!

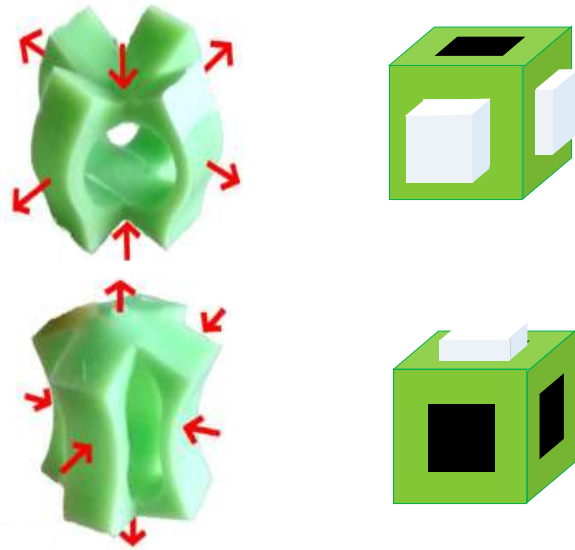


# 3D Metamaterials

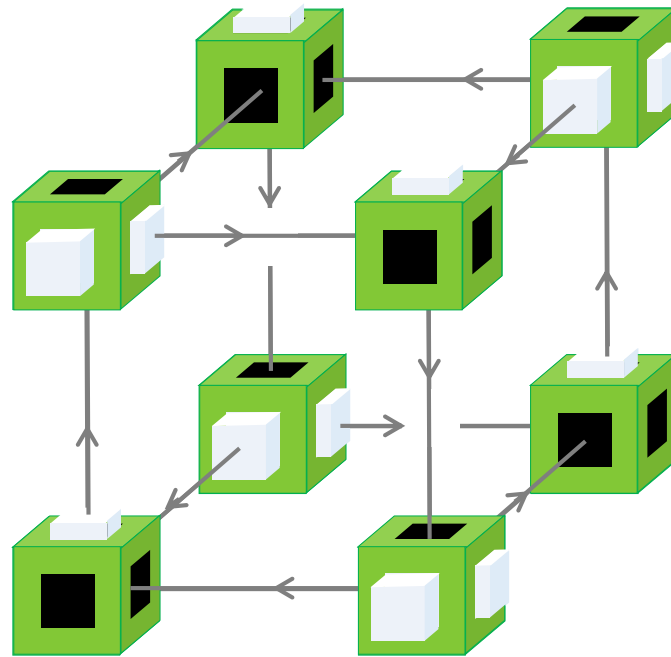
1 Flexible *Block*



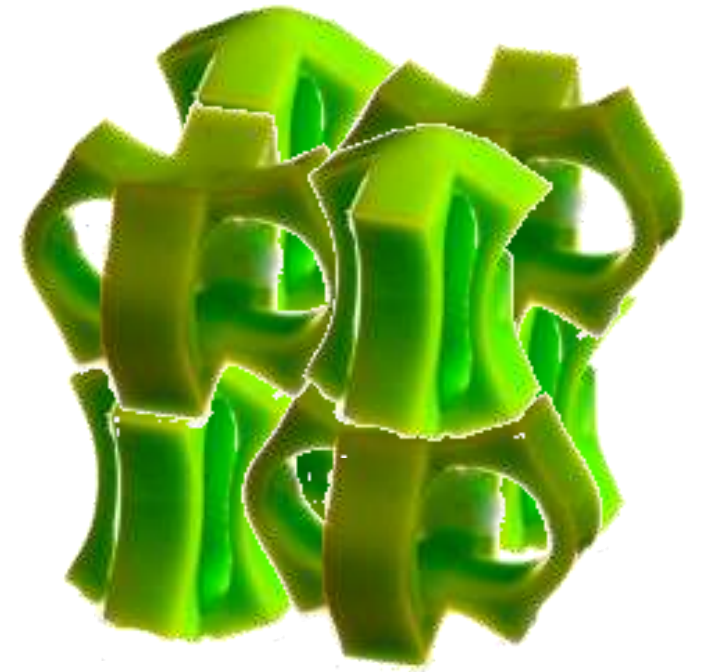
2 Deformed *Bricks*



Periodic Stacking

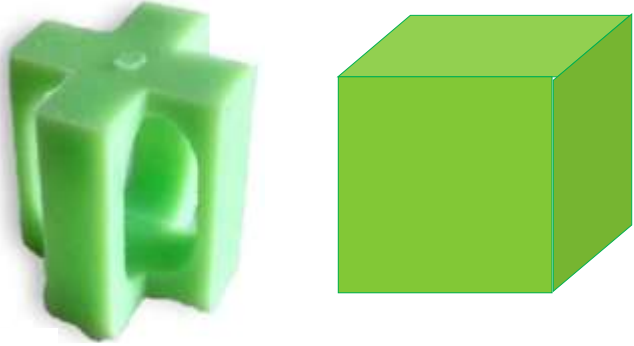


The bricks fit!

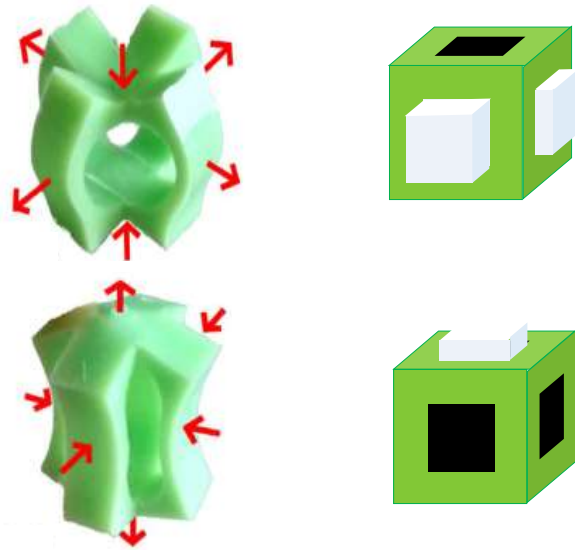


# 3D Metamaterials

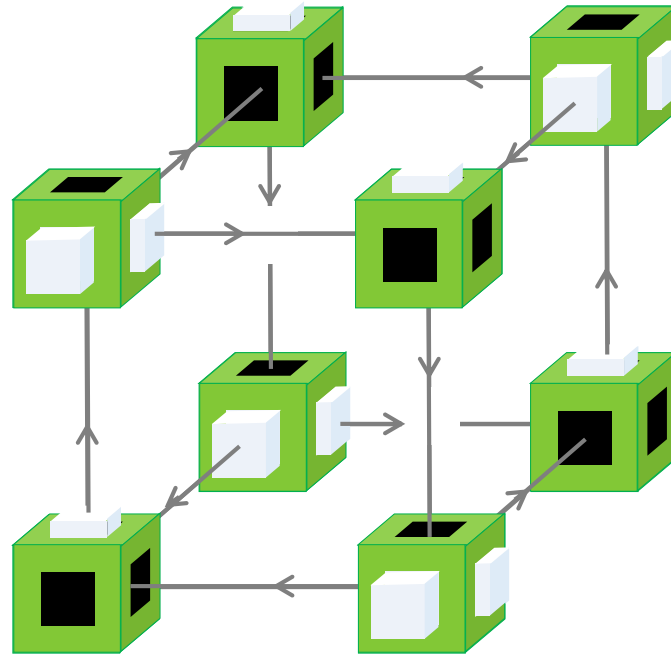
## 1 Flexible *Block*



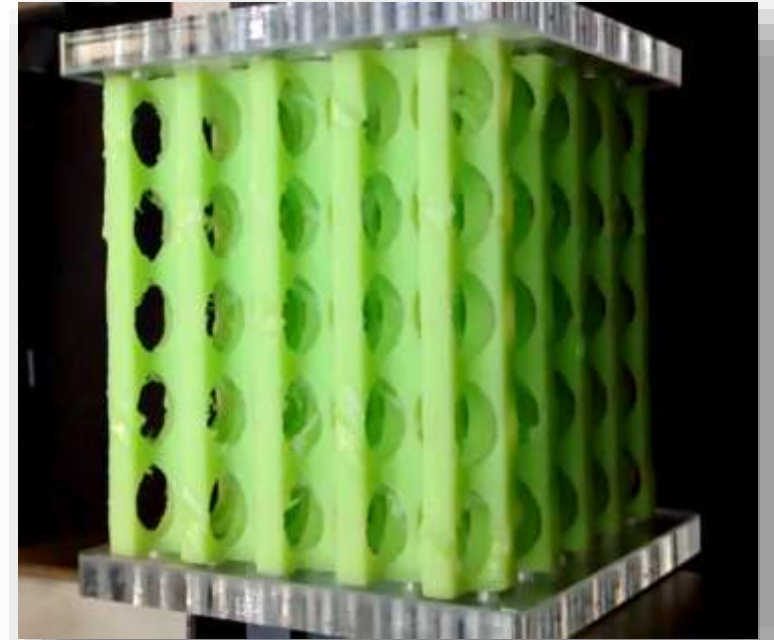
## 2 Deformed *Bricks*



## Periodic Stacking

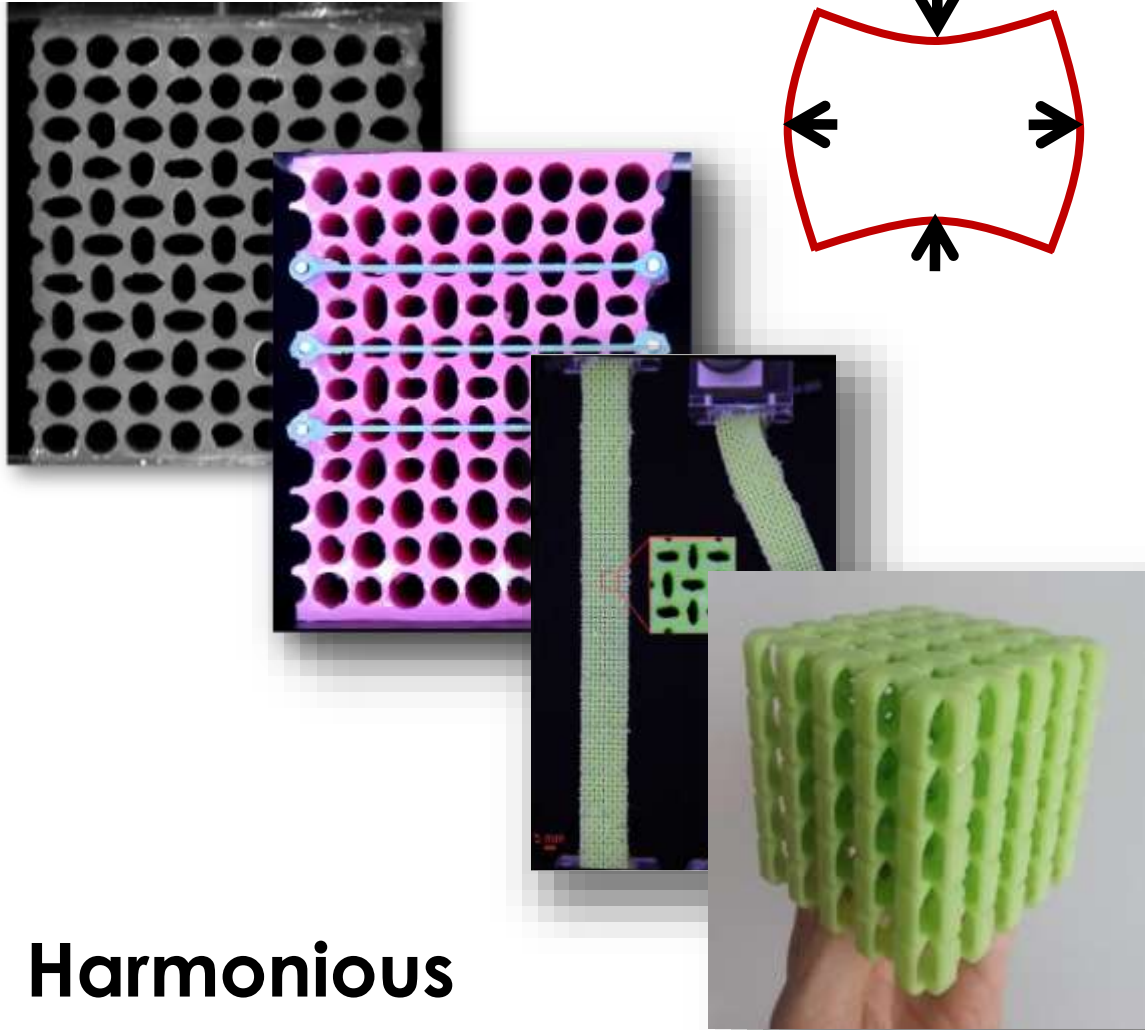


## Cooperative Motion

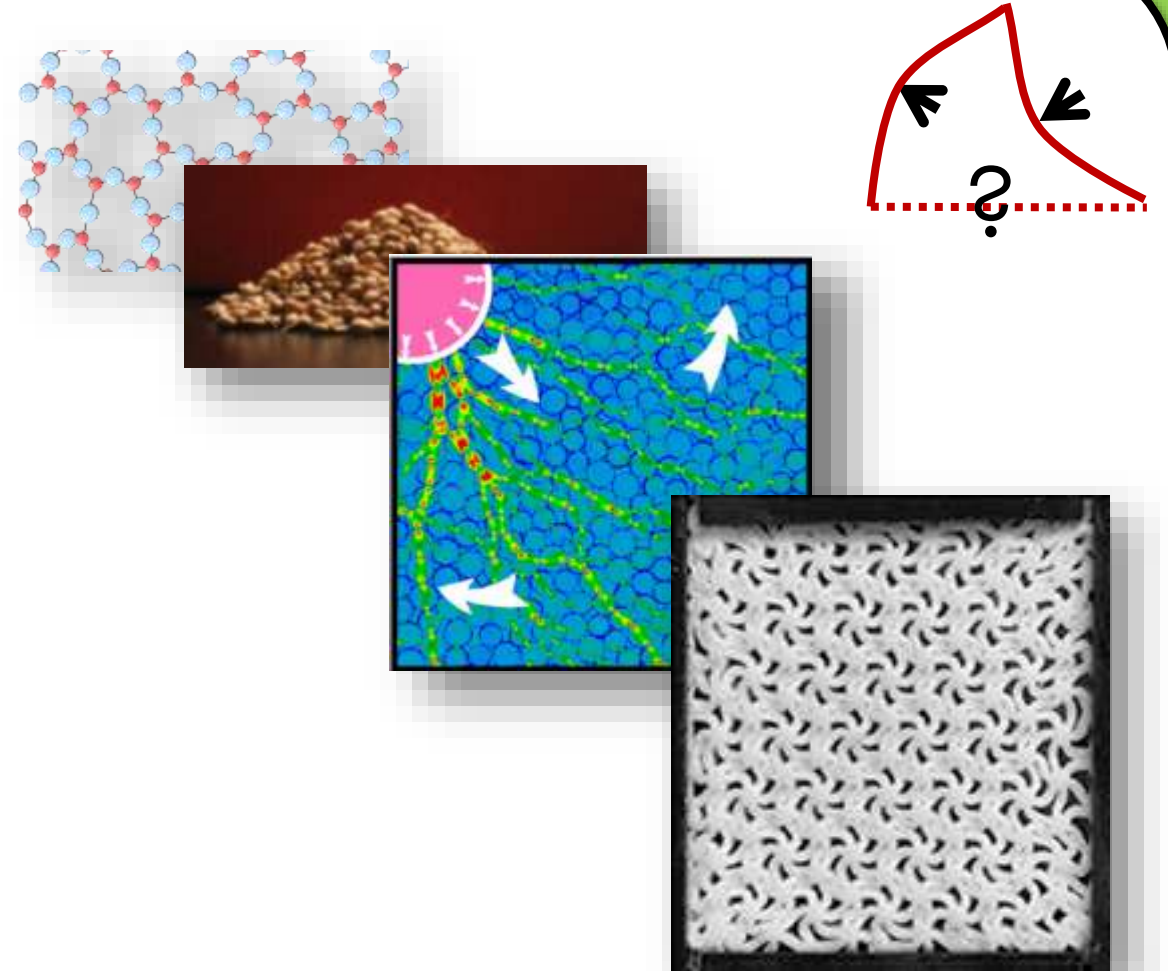




# Beyond Periodic Materials?



**Harmonious**

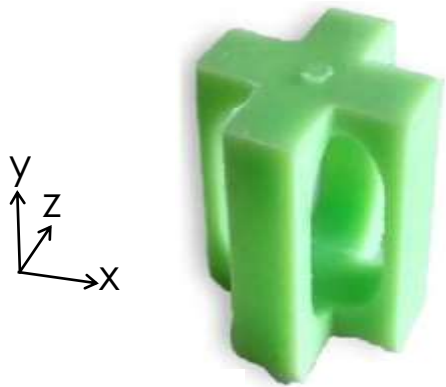


**Frustrated**

Kang et al, 2014

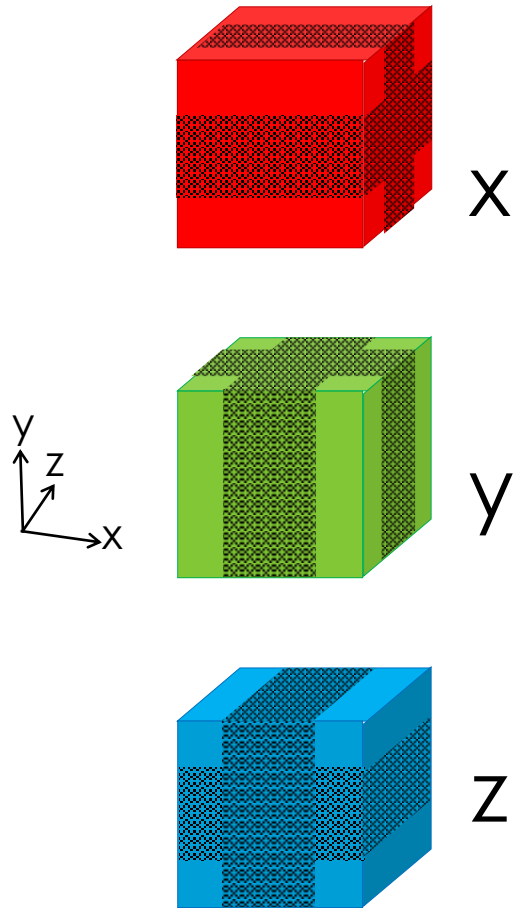
# Voxelated Metamaterials

## Flexible *Blocks*

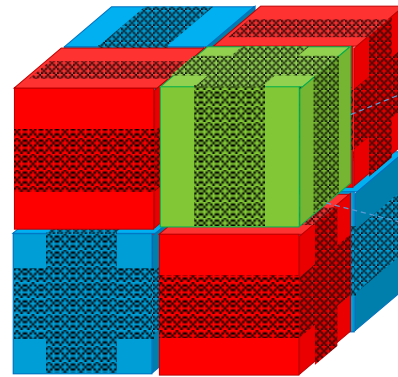


# Voxelated Metamaterials

Flexible *Blocks*



Anisotropic *Bricks*

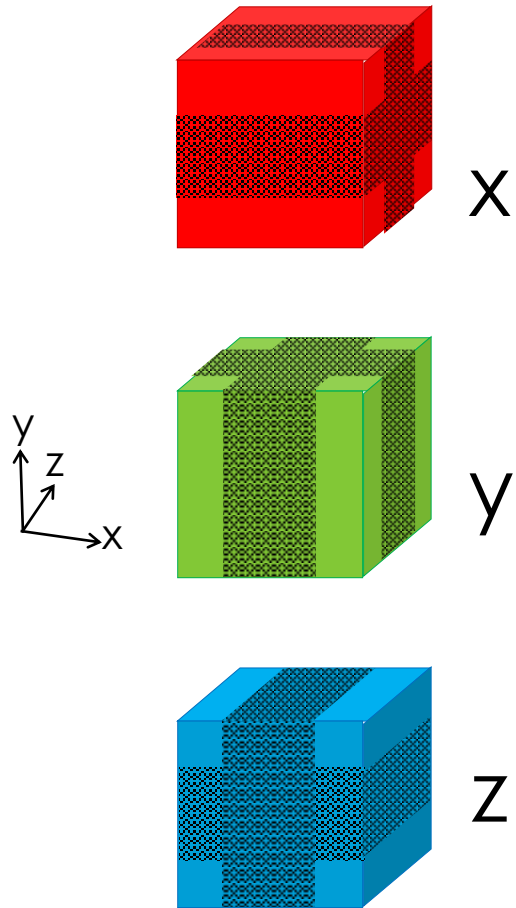


Aperiodic Stacking

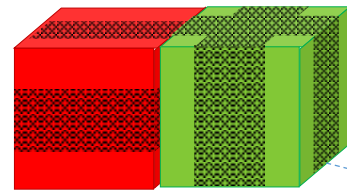


# Voxelated Metamaterials

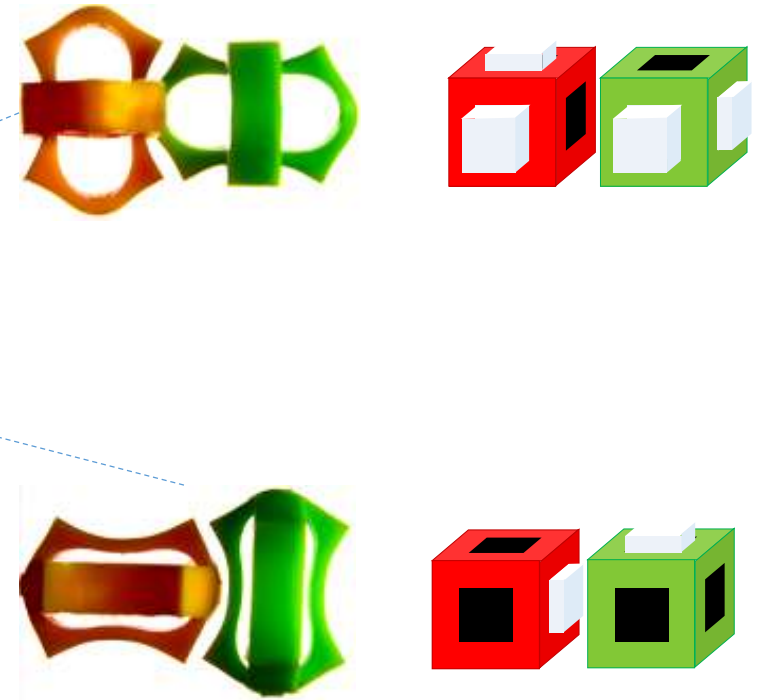
## Flexible *Blocks*



## Anisotropic *Bricks*



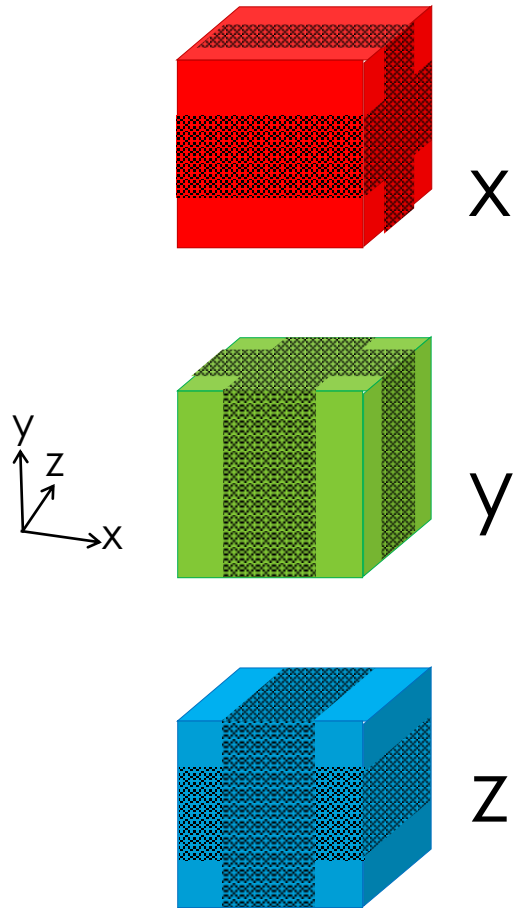
## Aperiodic Stacking



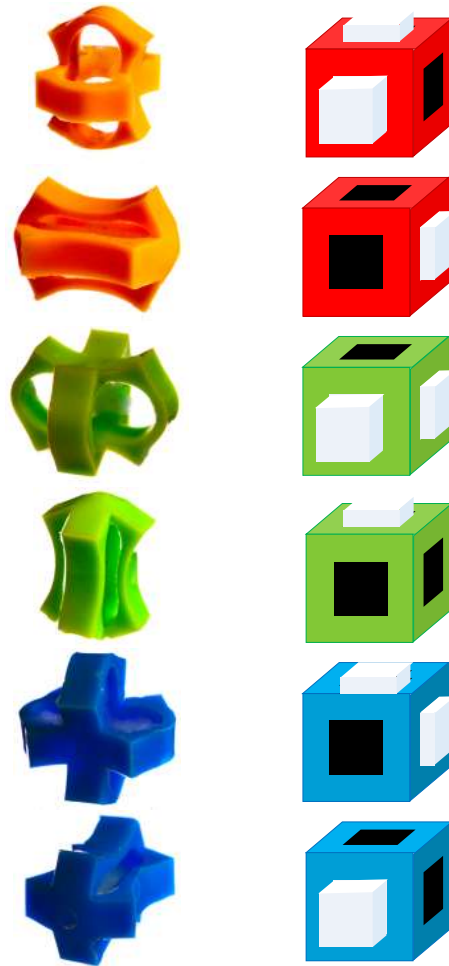


# Voxelated Metamaterials

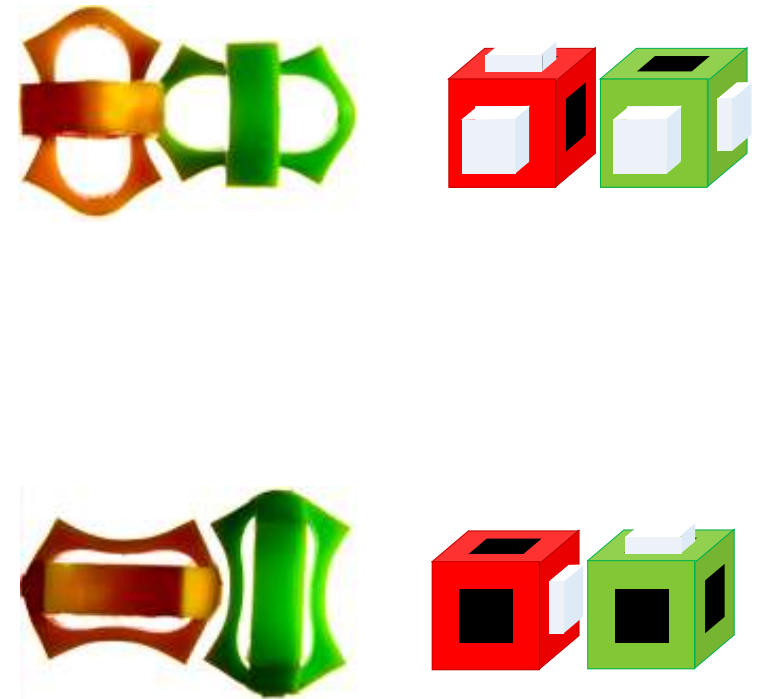
## Flexible Blocks



## Anisotropic Bricks

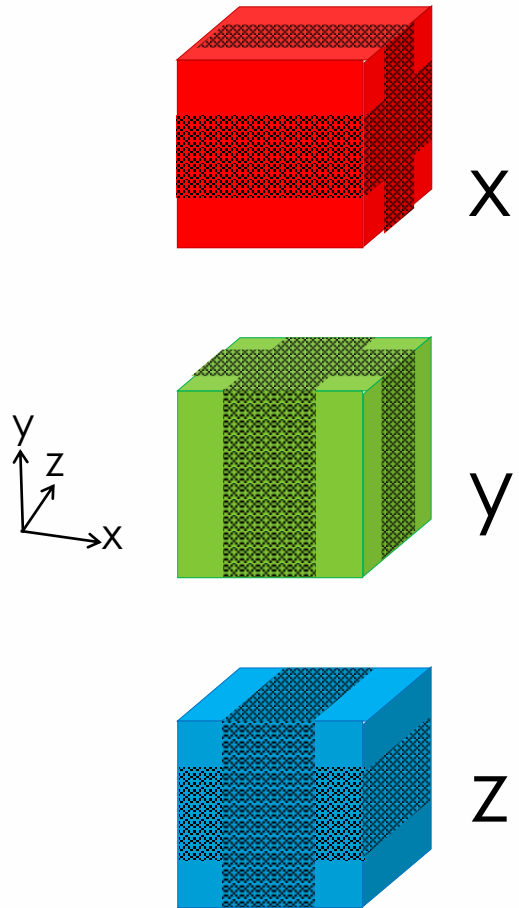


## Aperiodic Stacking

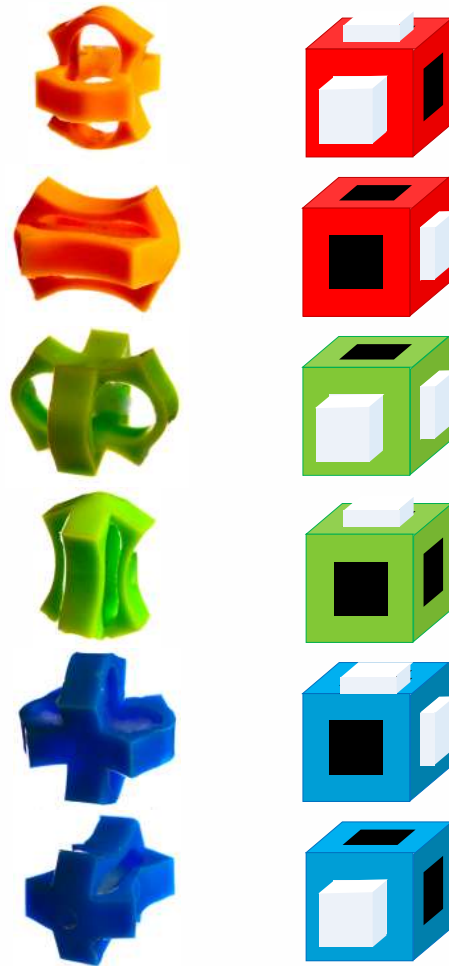


# Voxelated Metamaterials

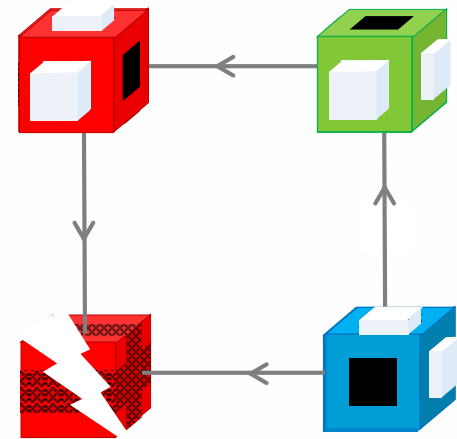
## Flexible Blocks



## Anisotropic Bricks

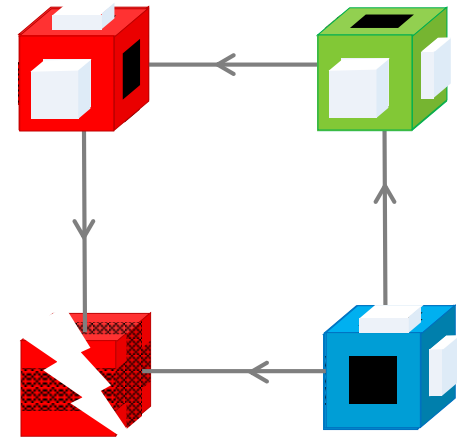


## Aperiodic Stacking



# Voxelated Metamaterial: frustration

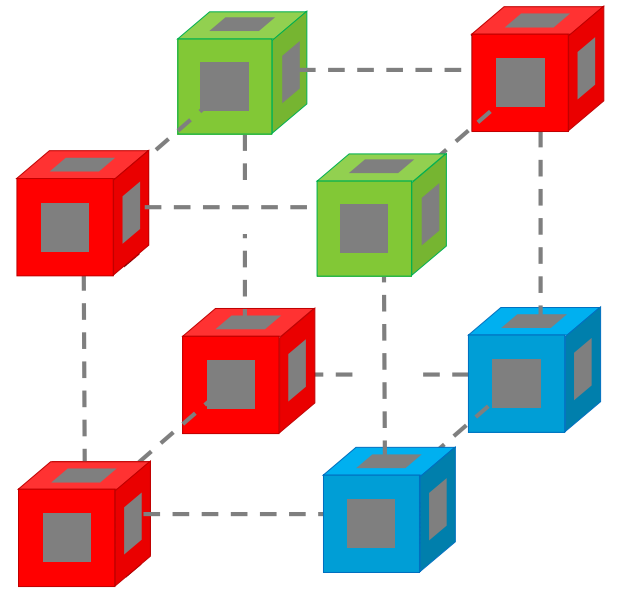
Aperiodic Stacking



Frustrated

# Voxelated Metamaterial: frustration

Aperiodic

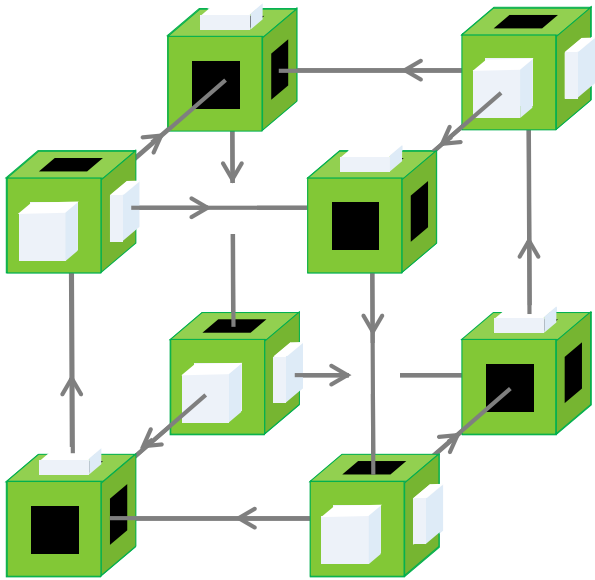


Frustrated

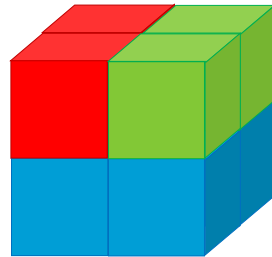


# Periodic and Frustrated

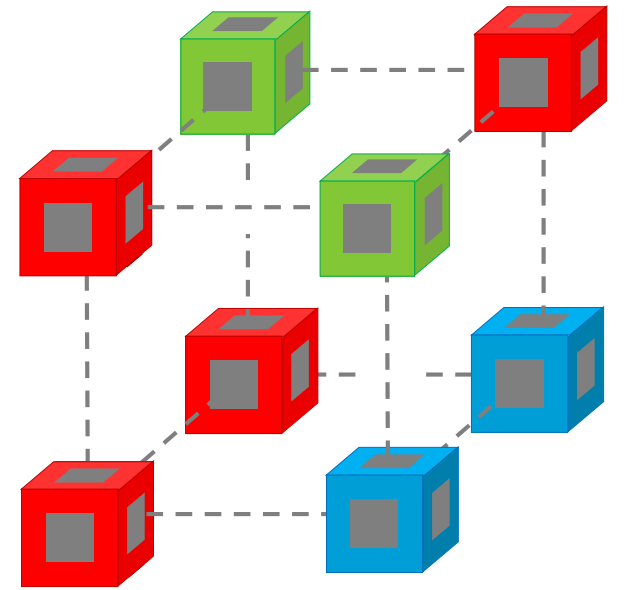
Periodic



Non-Frustrated



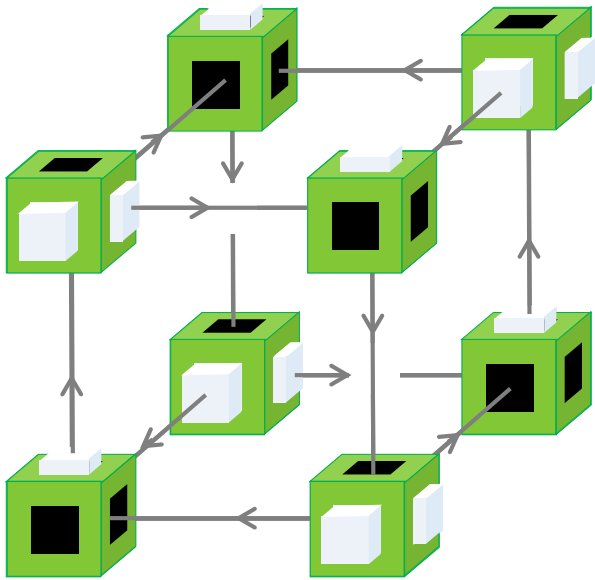
Aperiodic



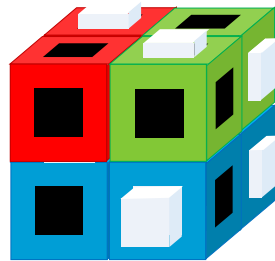
Frustrated

# Periodic and Frustrated

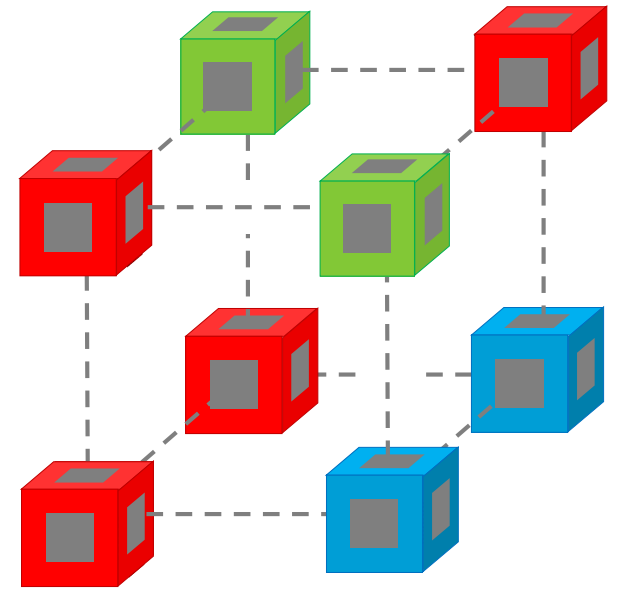
Periodic



Non-Frustrated



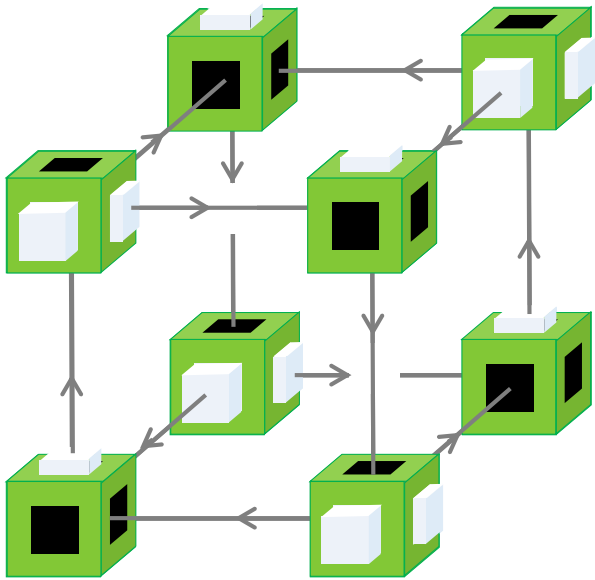
Aperiodic



Frustrated

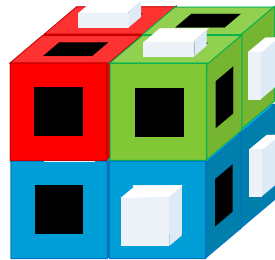
# Periodic and Frustrated

Periodic

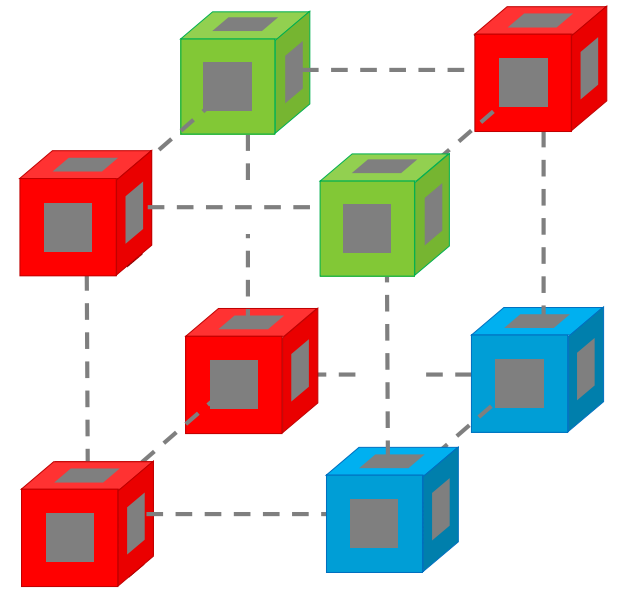


Non-Frustrated

Can it fit?



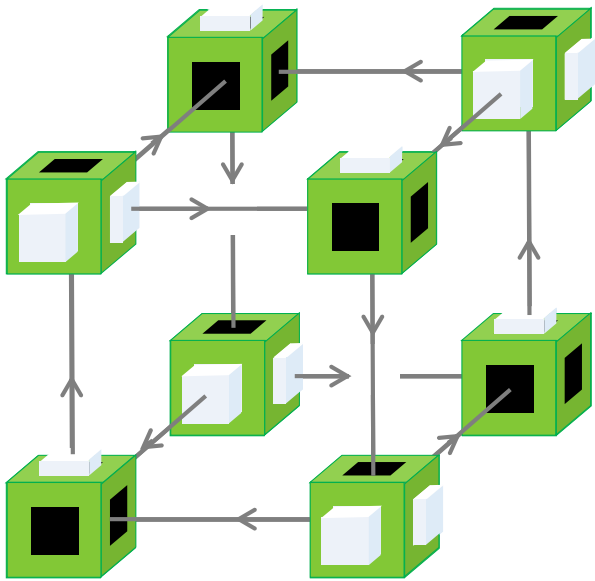
Aperiodic



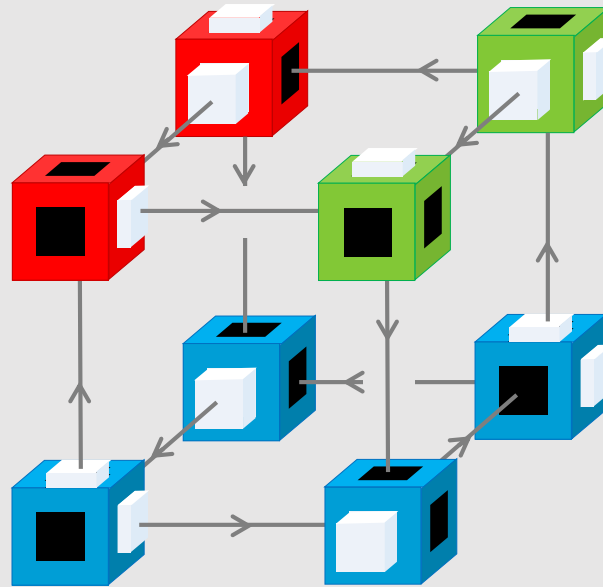
Frustrated

# Aperiodic yet Frustration-Free

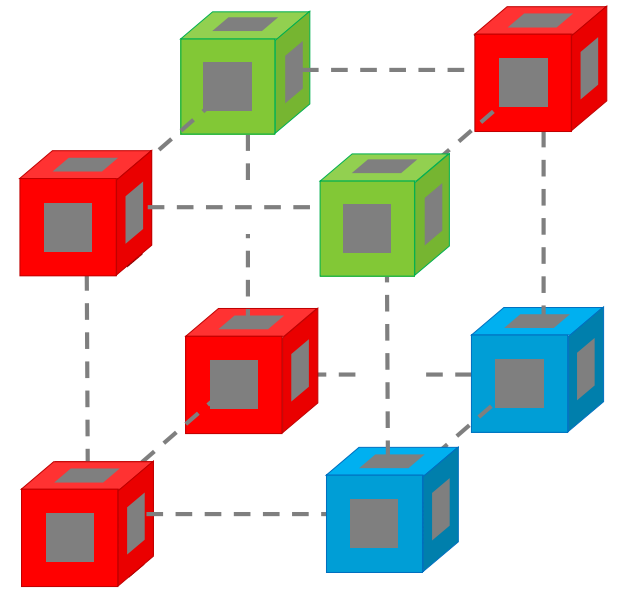
Periodic



Non-Frustrated



Aperiodic

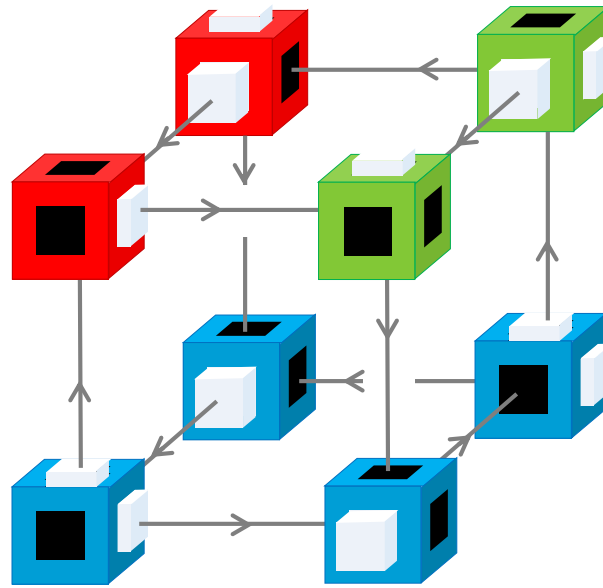
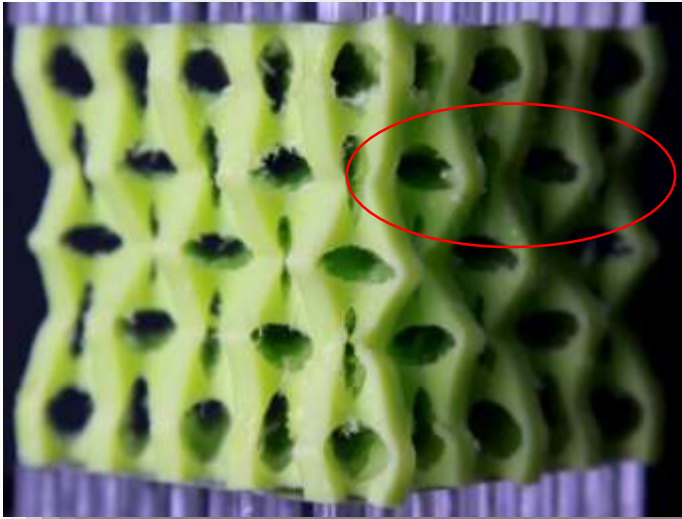


Frustrated



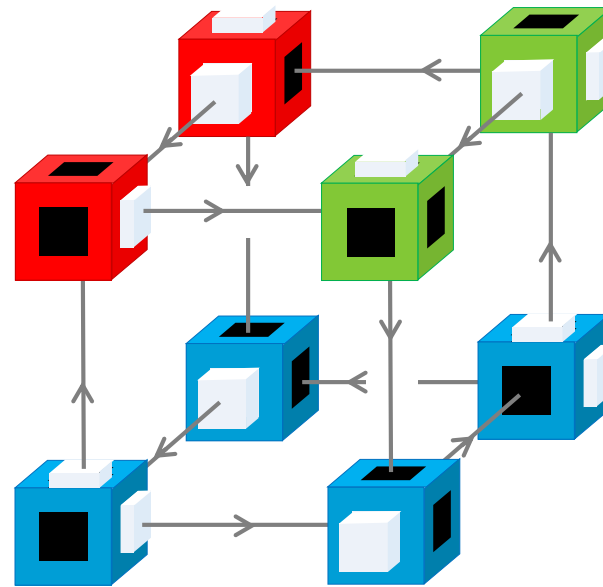
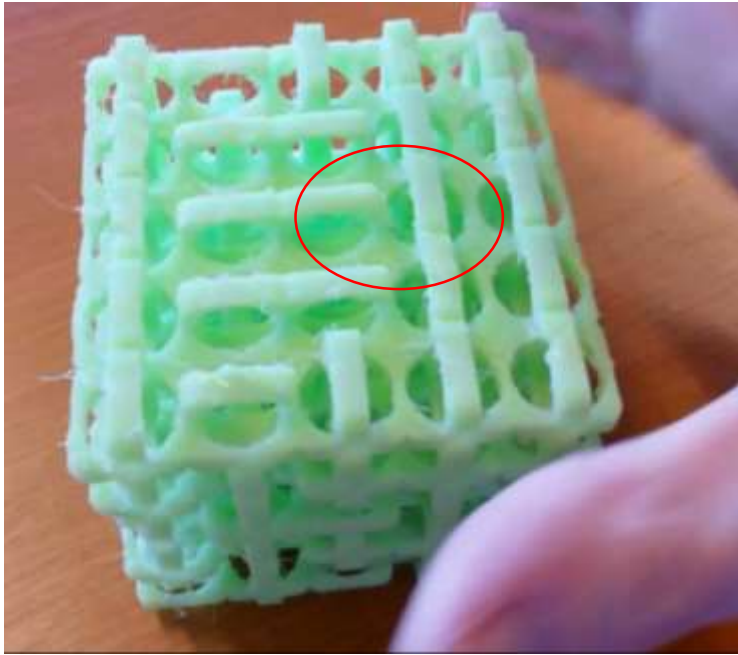
# Combinatorial Stacking Properties

Surface Texture



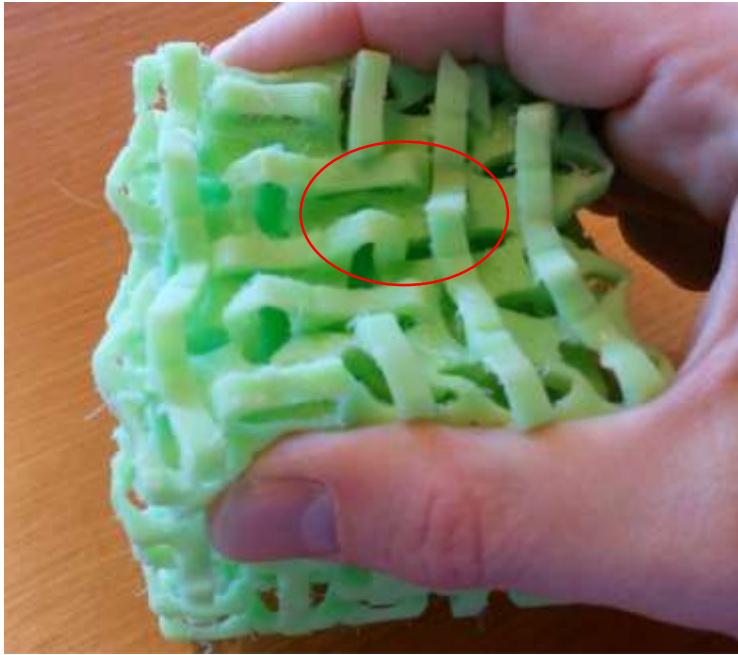
# Combinatorial Stacking Properties

Surface Texture

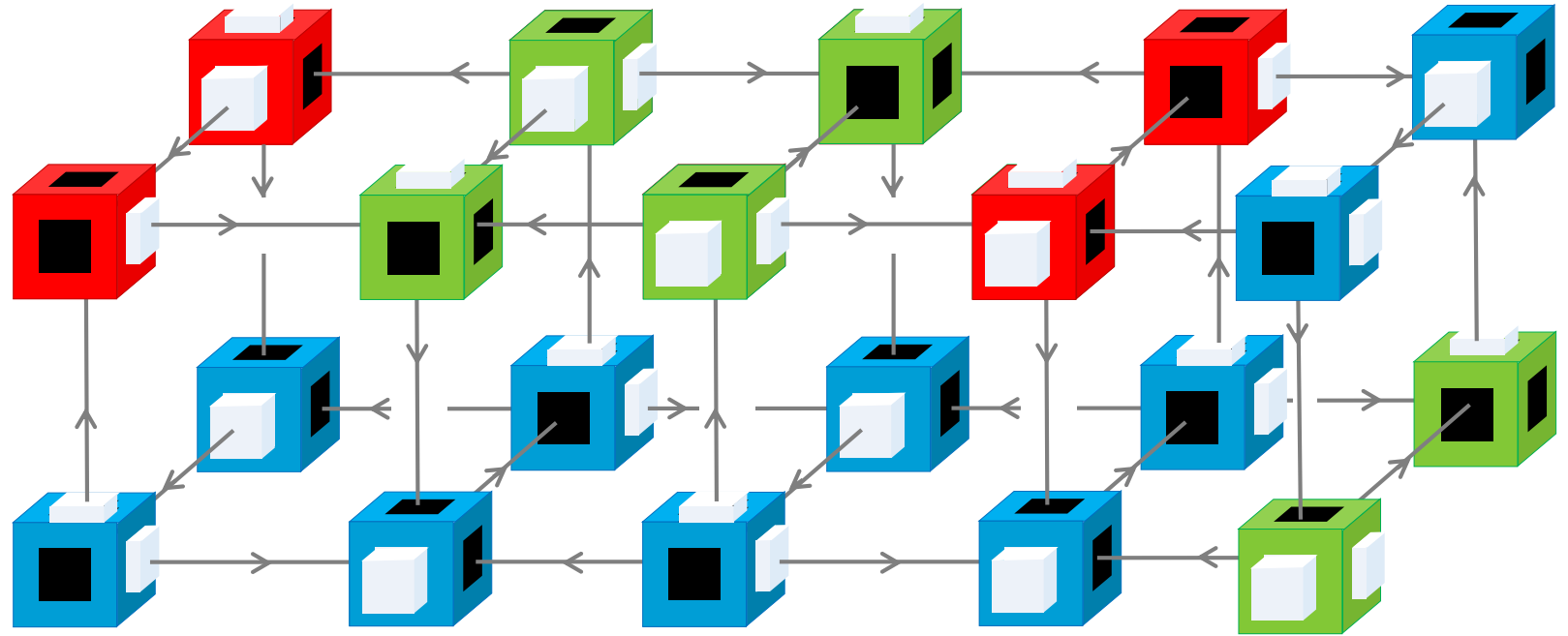


# Combinatorial Stacking Properties

Surface Texture

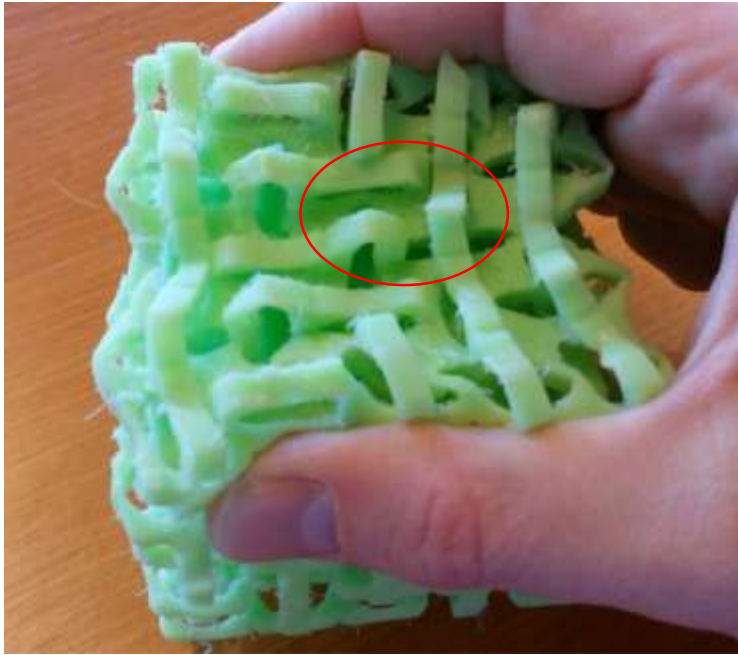


3D Jigsaw Puzzle

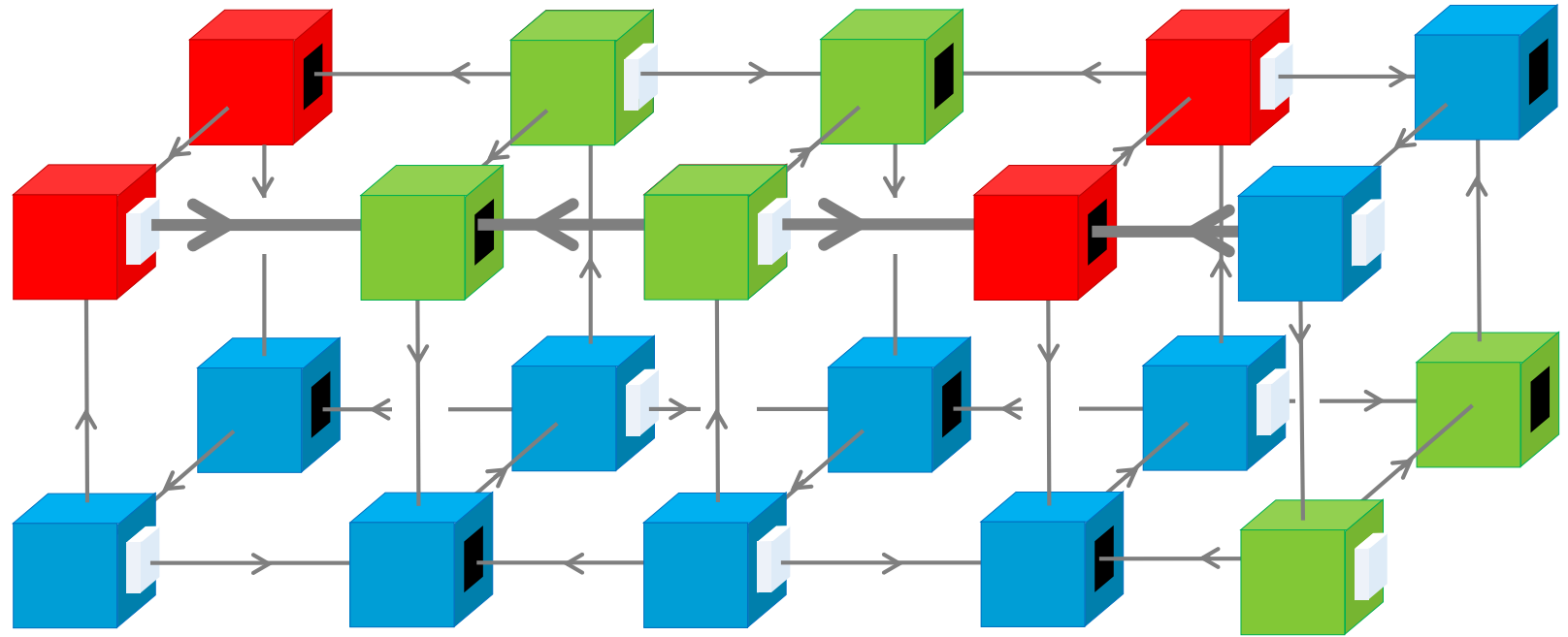


# Combinatorial Stacking Properties

Surface Texture

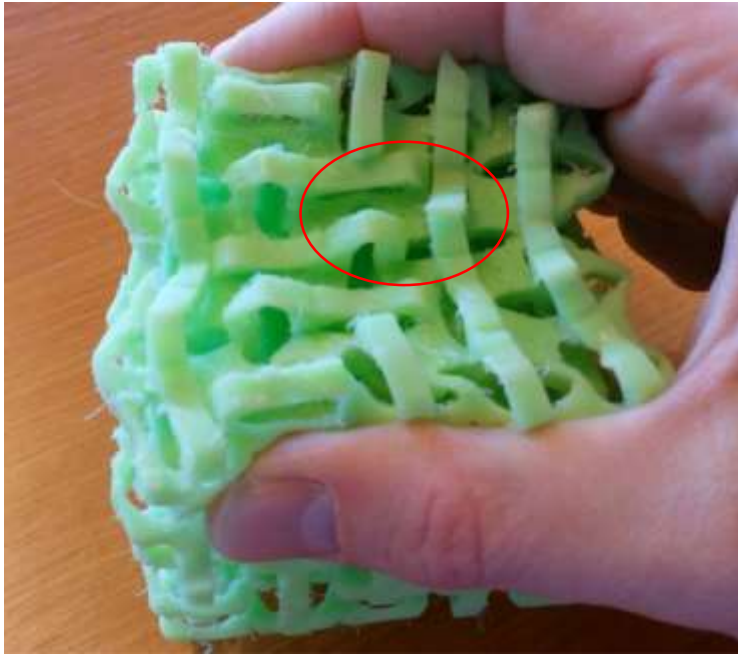


The Surface determines the Bulk

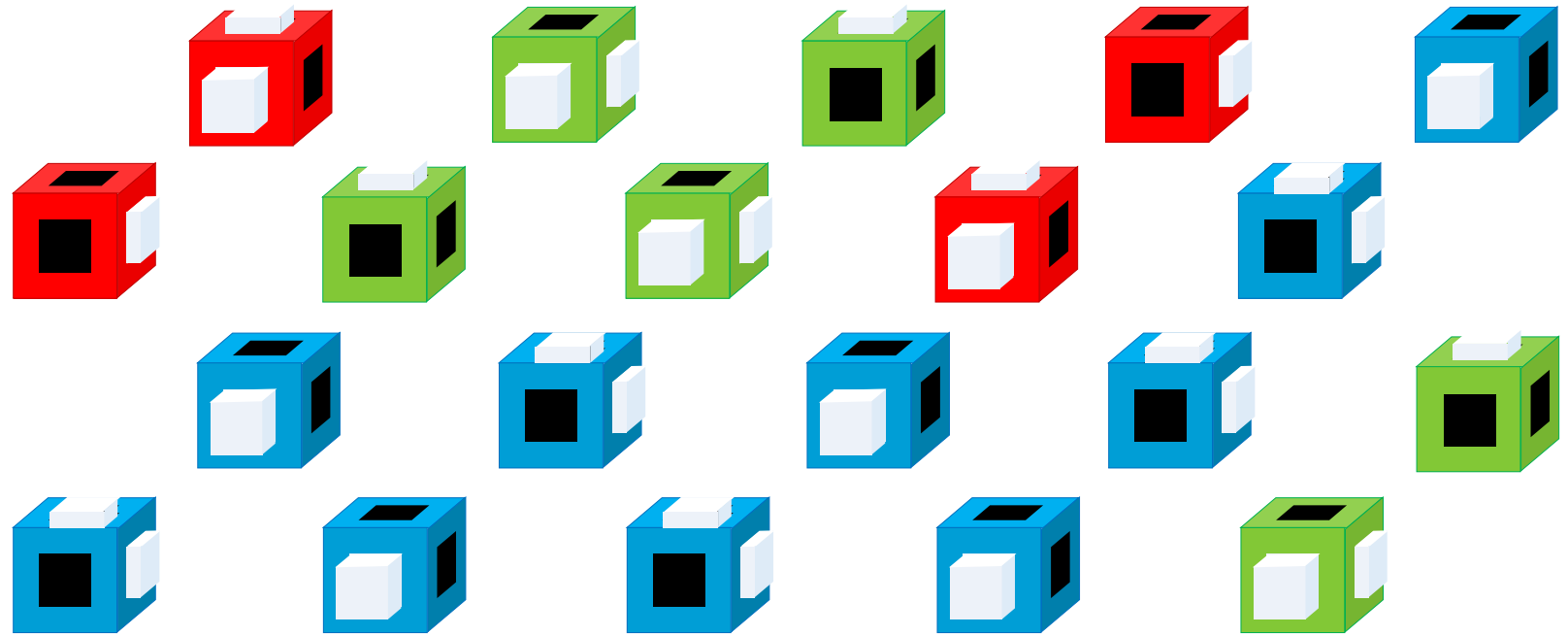


# Combinatorial Stacking Properties

Surface Texture



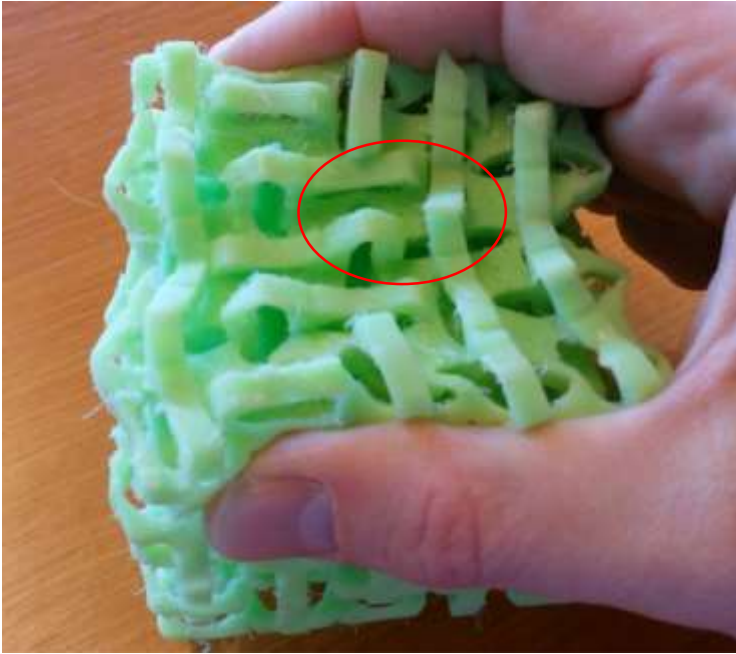
The Surface determines the Bulk



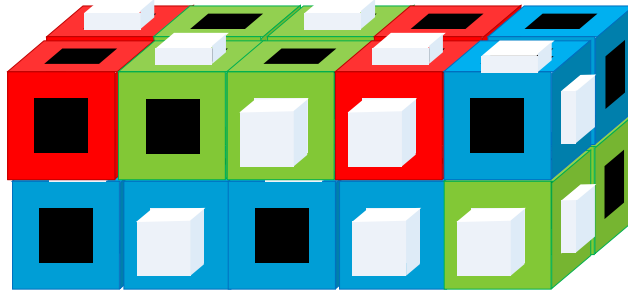


# Combinatorial Stacking Properties

Surface Texture

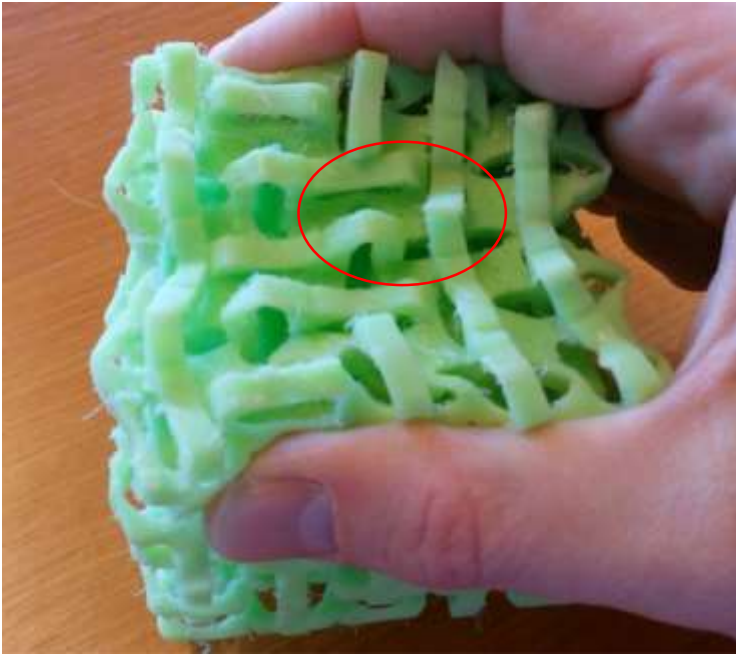


3D Jigsaw Puzzle

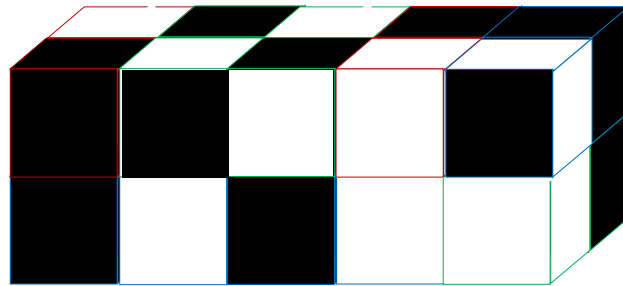


# Texture Properties

## Surface Texture



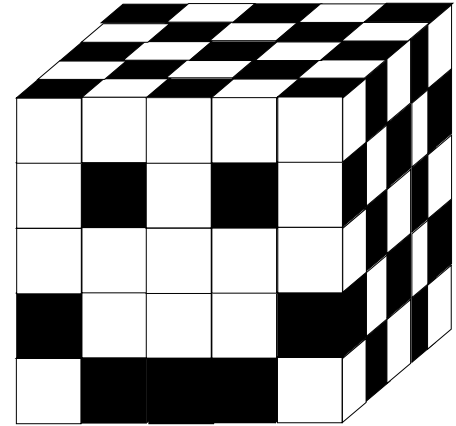
## 3D Jigsaw Puzzle



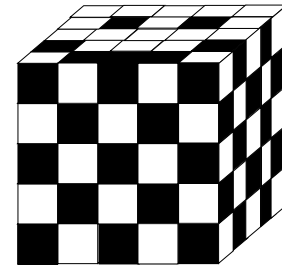
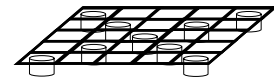
#  $L \times L \times L$  Configs?

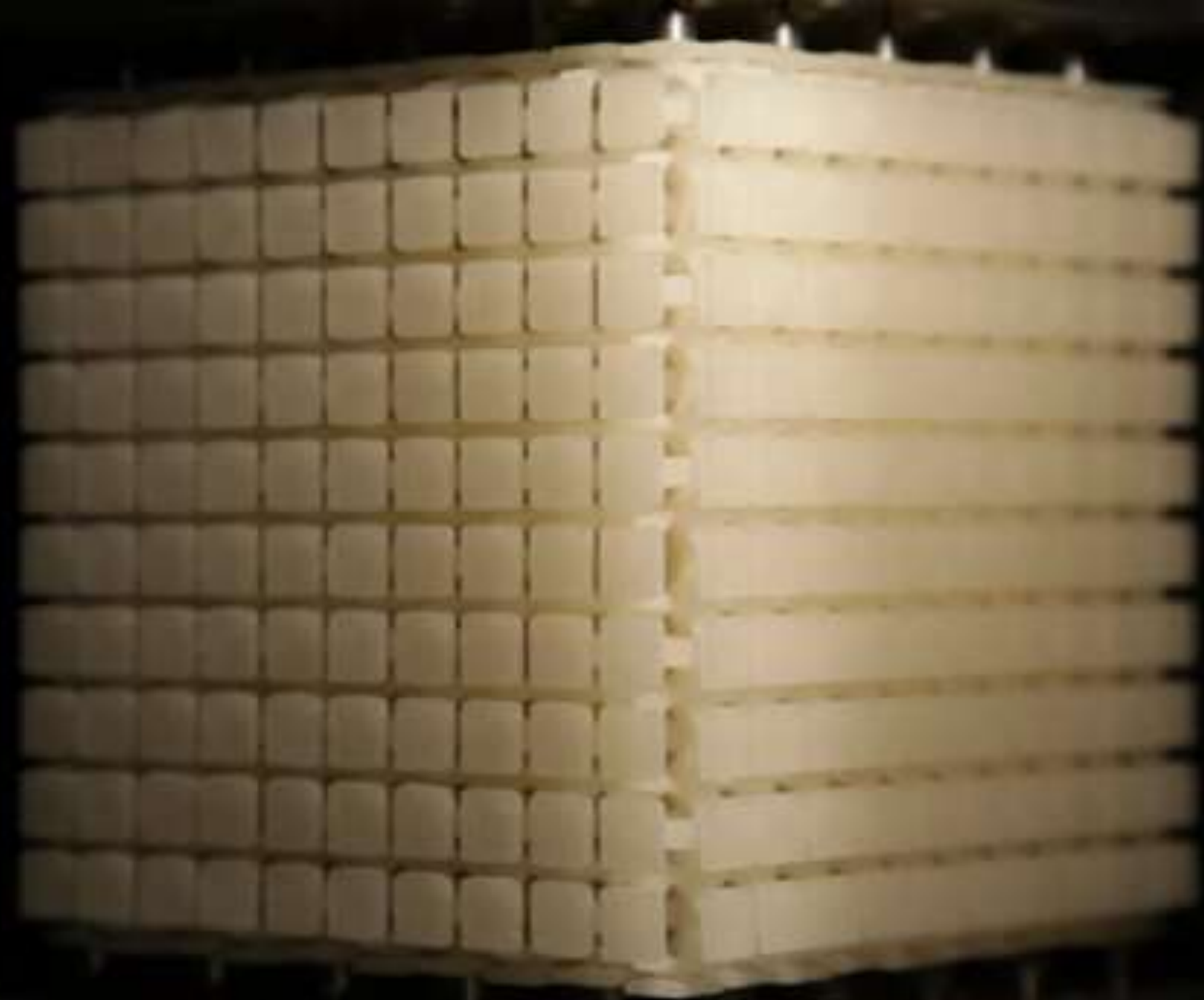
$$3^L \rightarrow 2^{3L^2}$$

## Rational Design?



Mechanics?







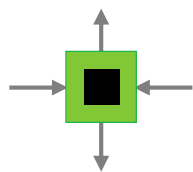
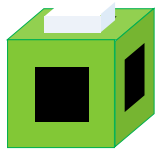
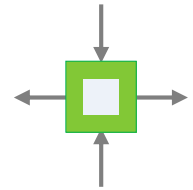
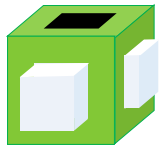
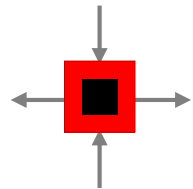
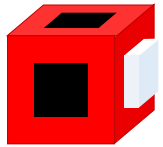
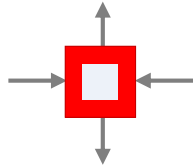
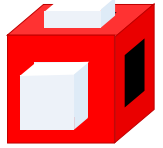
Back: Holographic



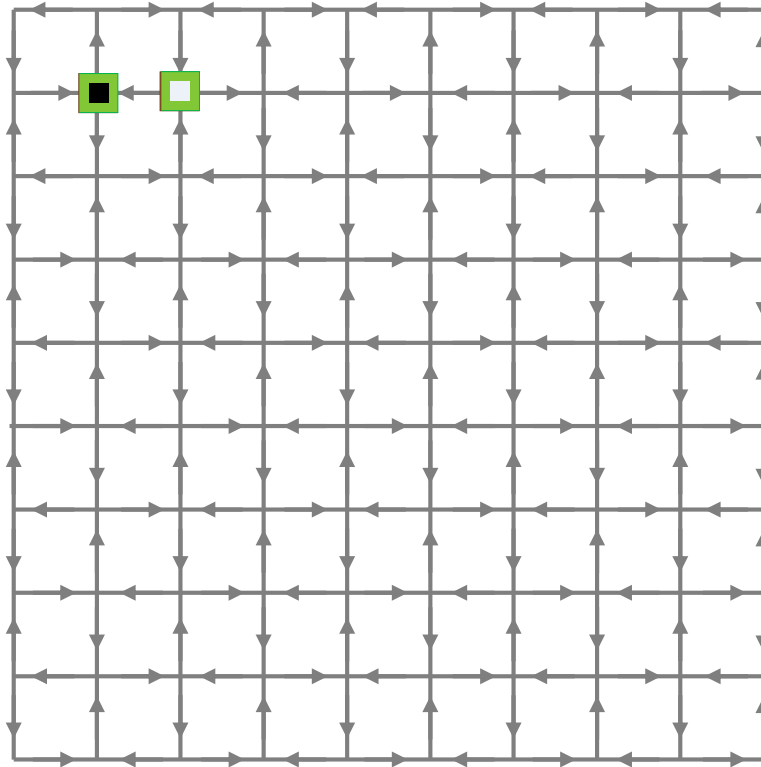
Side: Motif Stacking

# Rational Design

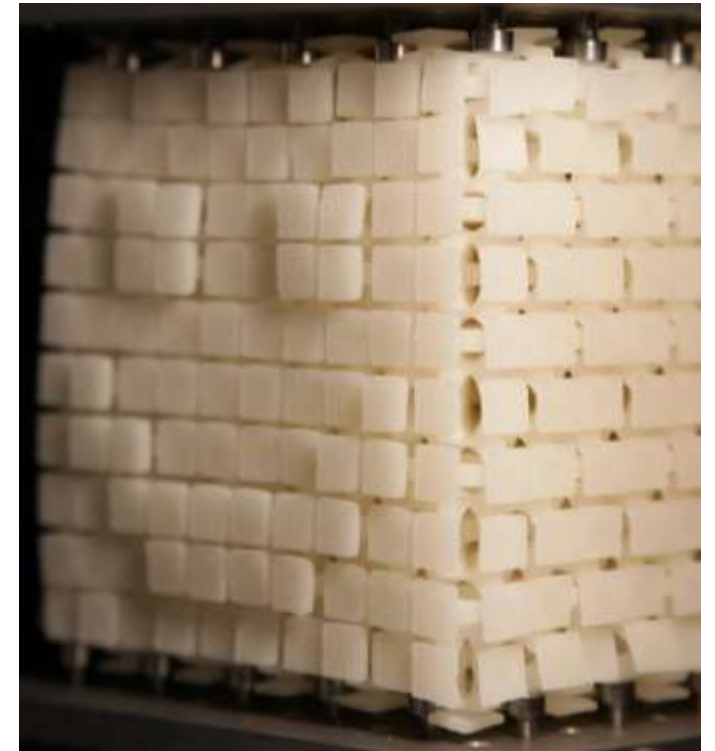
Red & Green Voxels



Free Choice  
of Texture



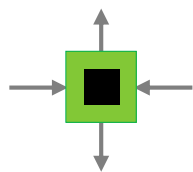
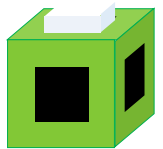
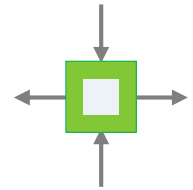
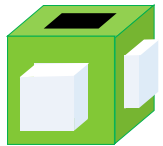
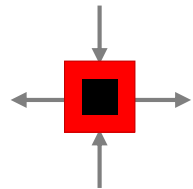
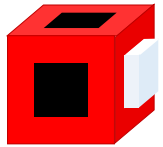
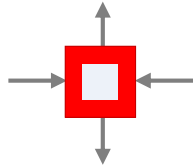
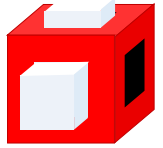
Programmable  
Shape-Shifter



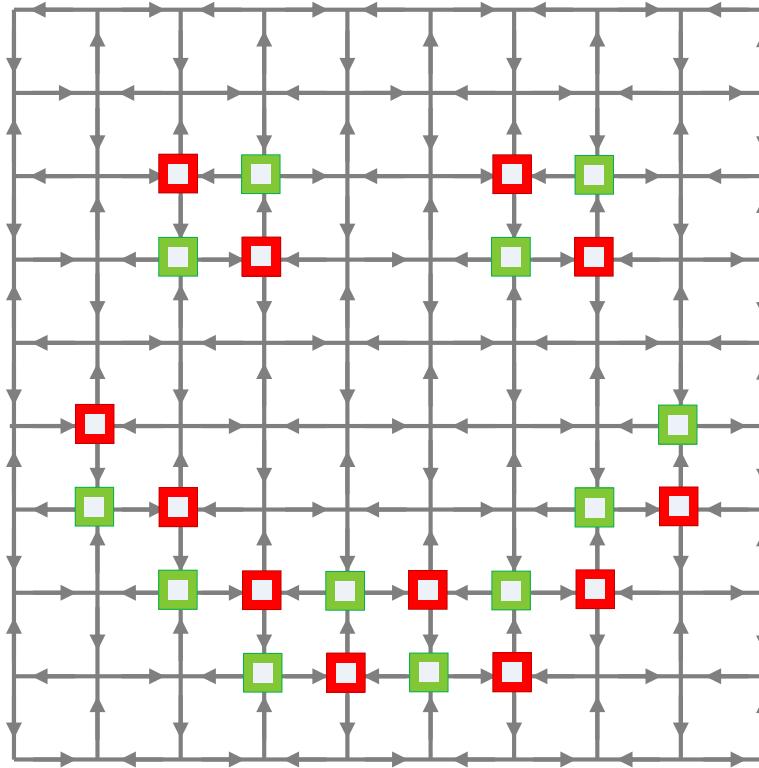


# Rational Design

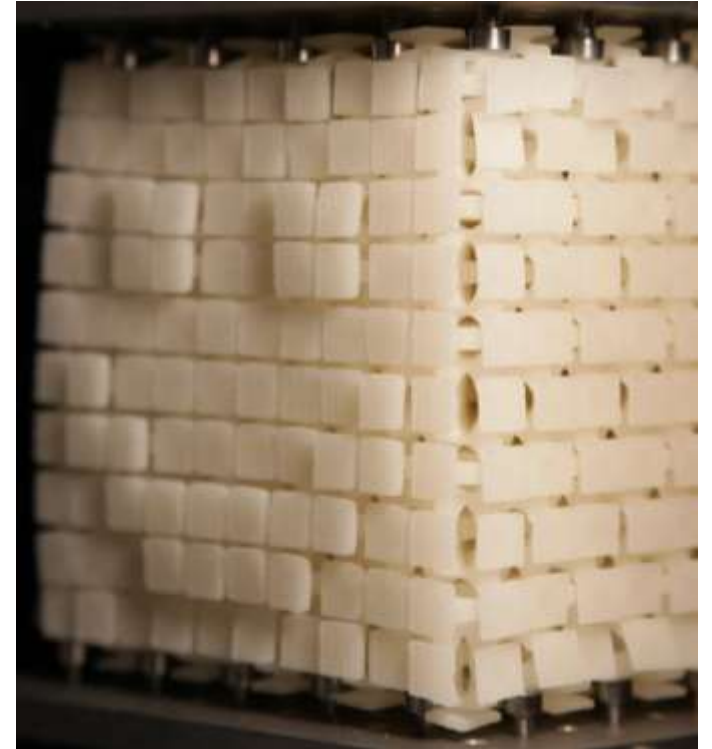
## Red & Green Voxels



## Free Choice of Texture

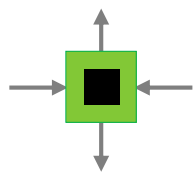
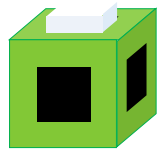
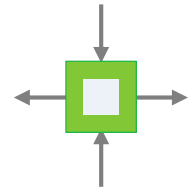
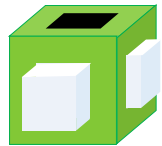
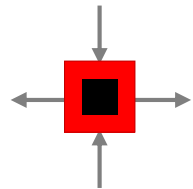
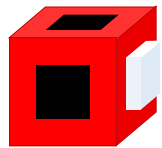
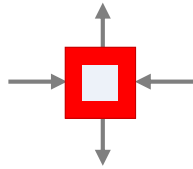
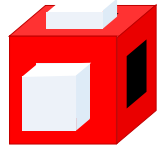


## Programmable Shape-Shifter

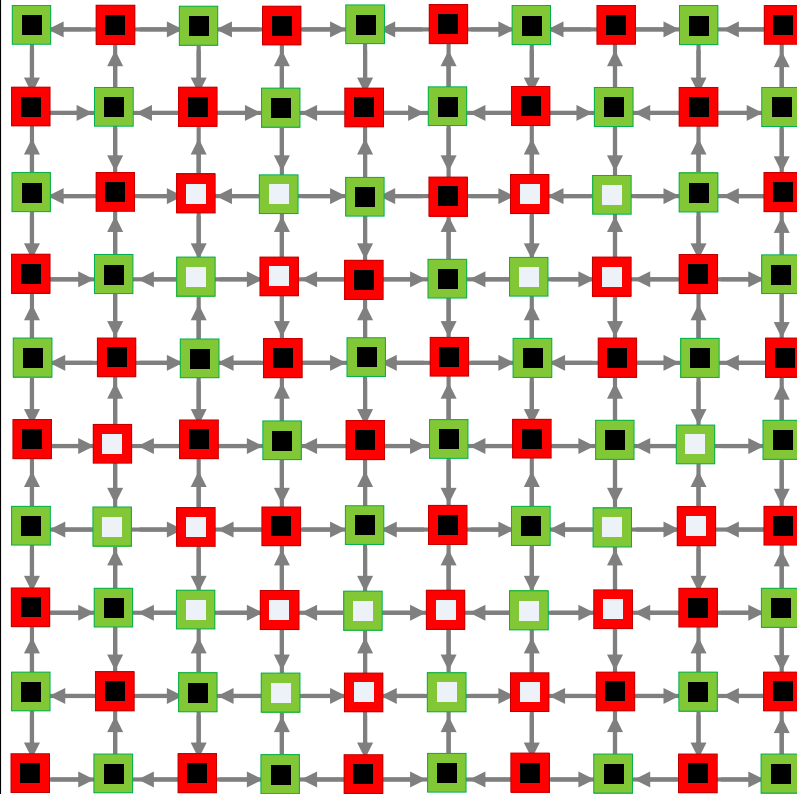


# Rational Design

Red & Green Voxels



Free Choice  
of Texture

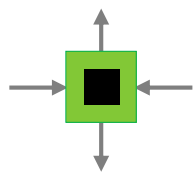
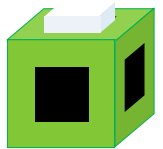
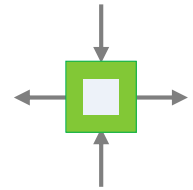
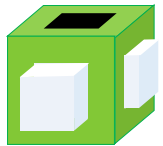
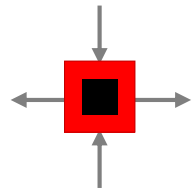
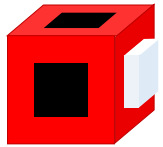
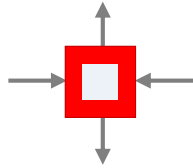
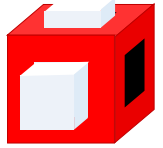


Programmable  
Shape-Shifter

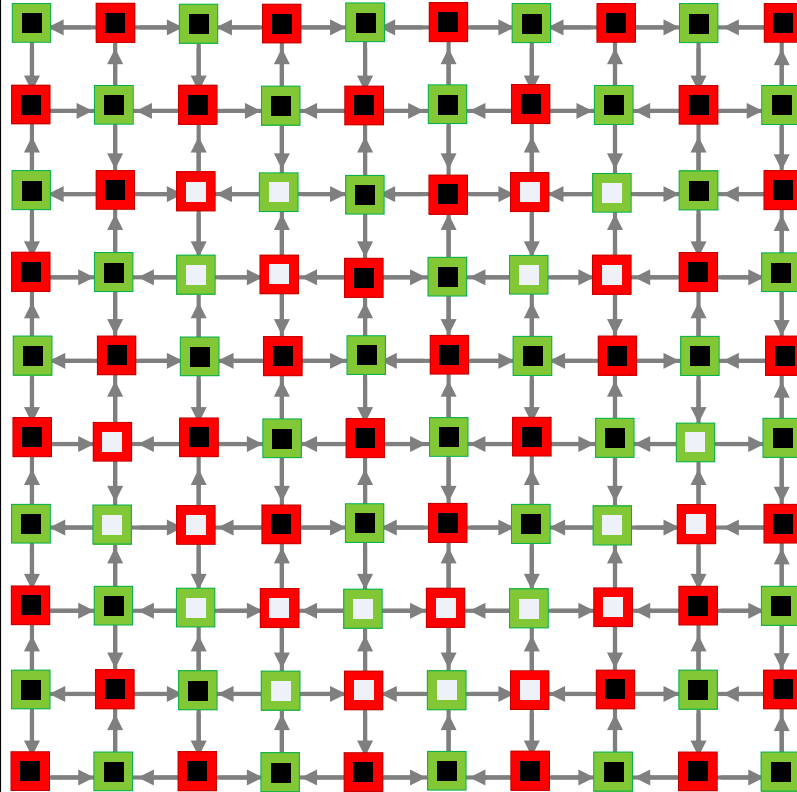


# Rational Design

Red & Green Voxels

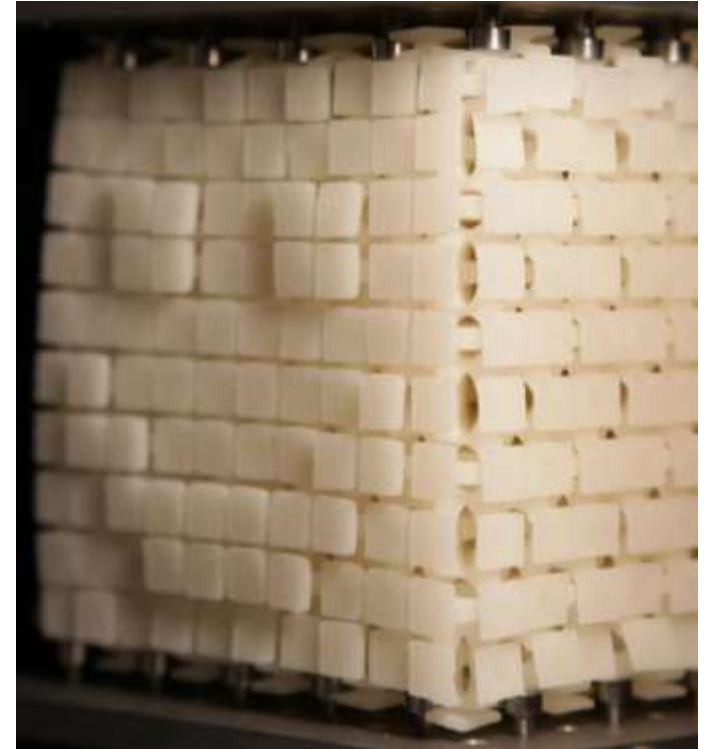


Free Choice  
of Texture



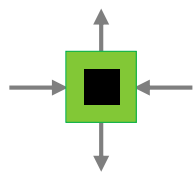
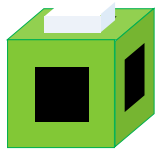
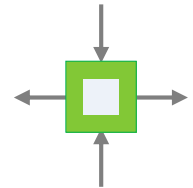
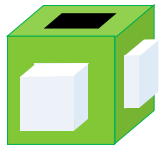
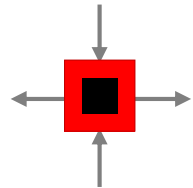
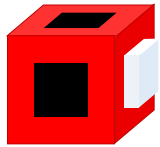
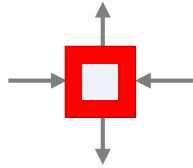
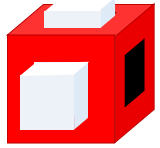
#  $L \times L \times 1$  Motifs:  $2^{L^2} \times 2$

Programmable  
Shape-Shifter

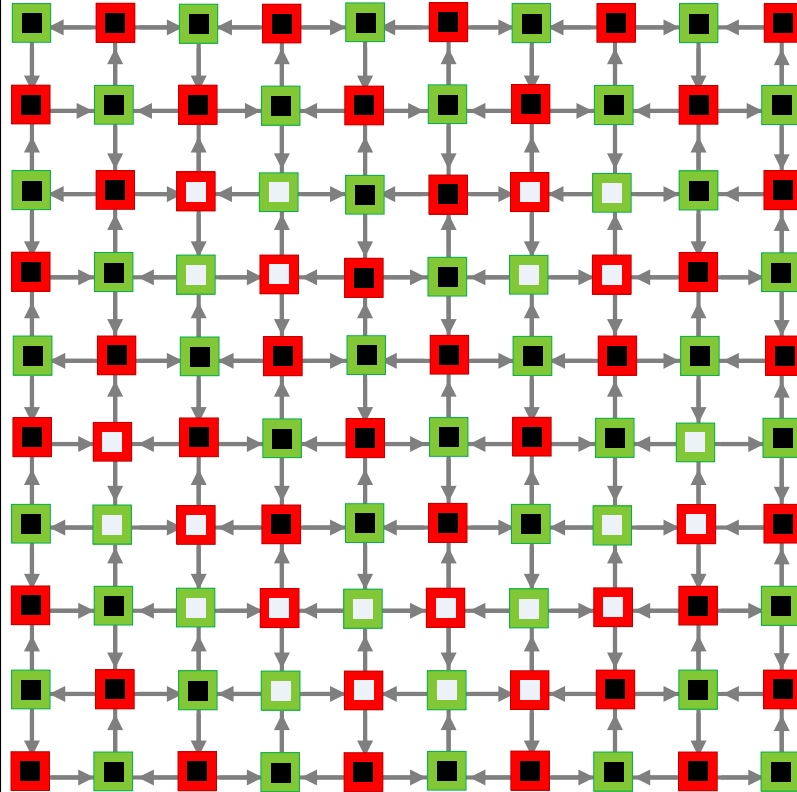


# Rational Design

Red & Green Voxels

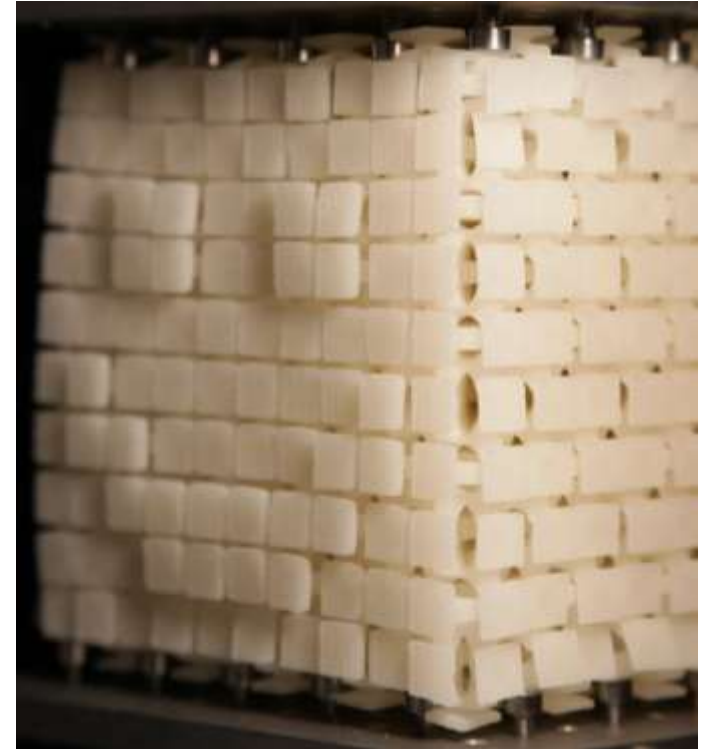


Free Choice  
of Texture

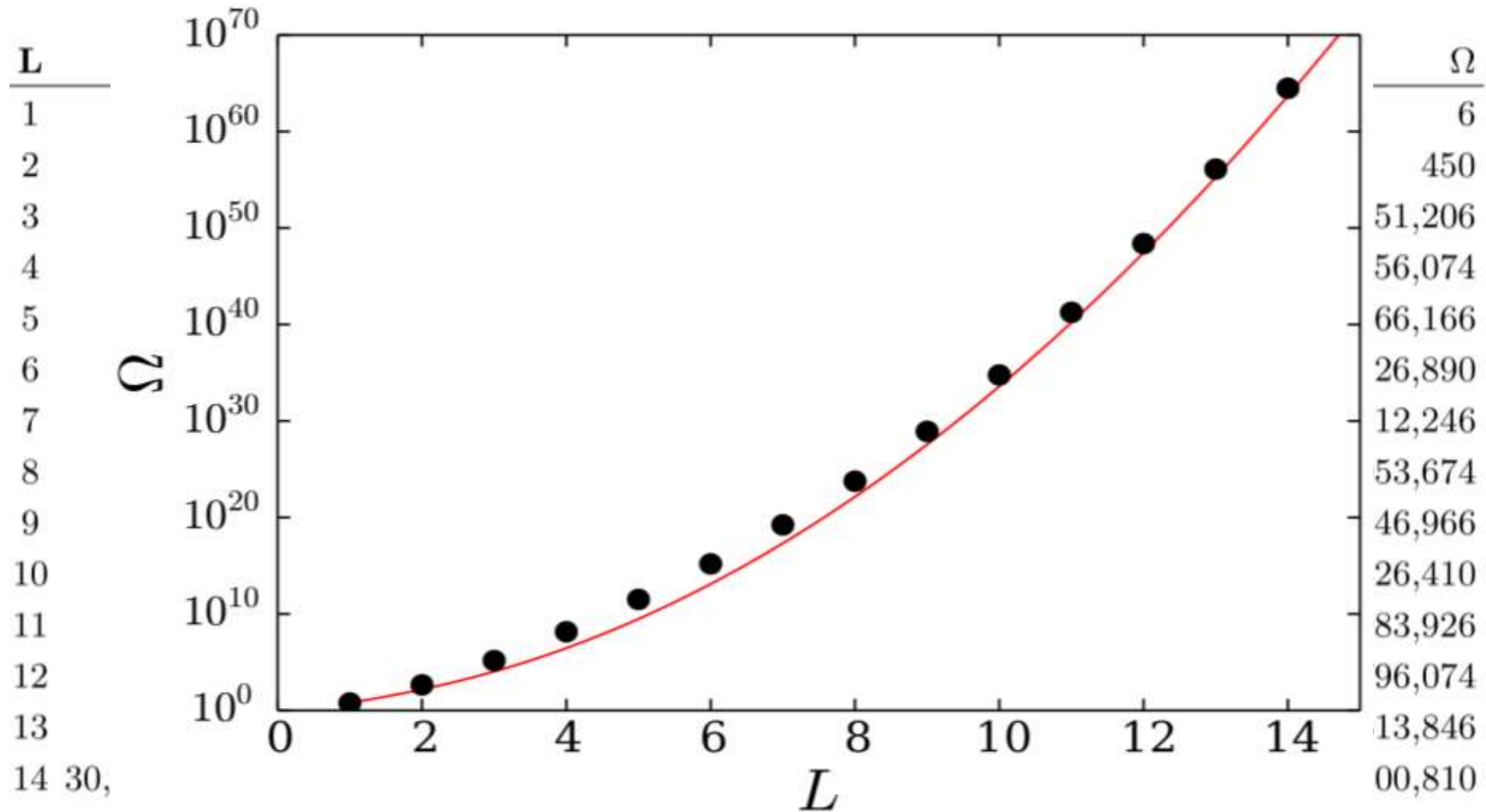


#  $L \times L \times L$  Motifs:  $2^{L^2} \times 2^L$

Programmable  
Shape-Shifter



# How many $L^3$ cubes?

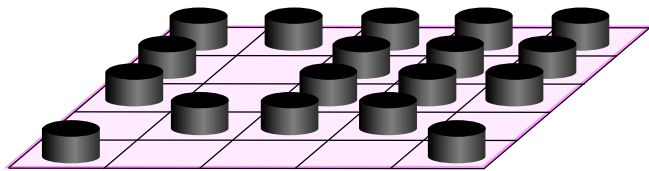
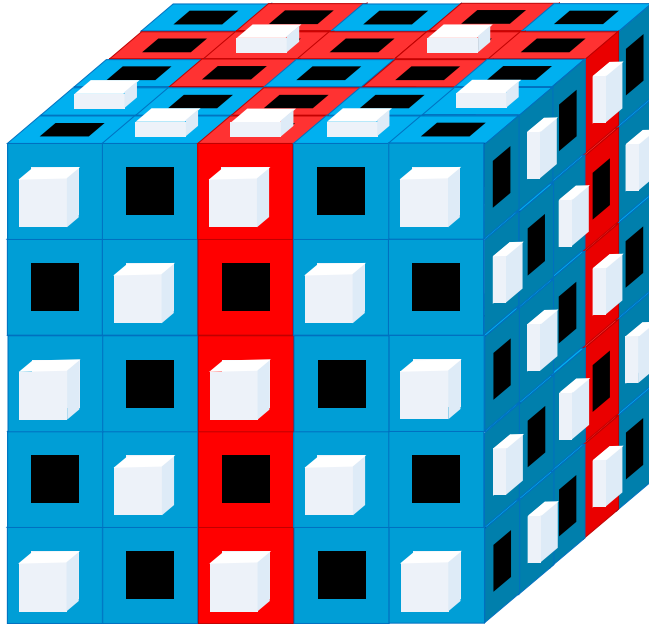
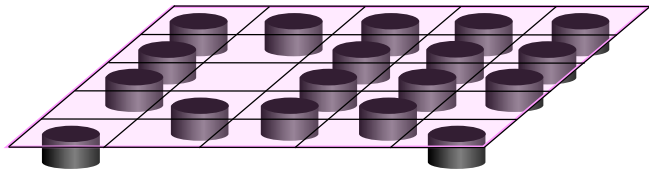


Lower Bound:  $2^{L^2} \times 2^L = 2^{L+L^2}$

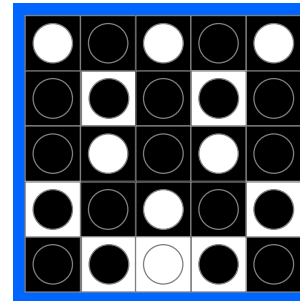
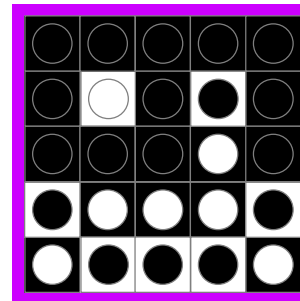
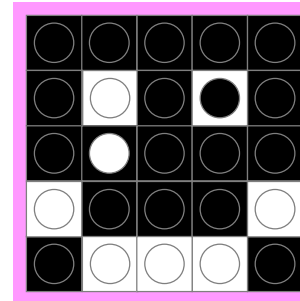
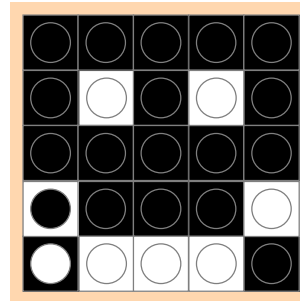
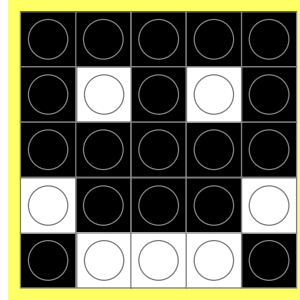


# Machine Matter: Lock & Key

Lock

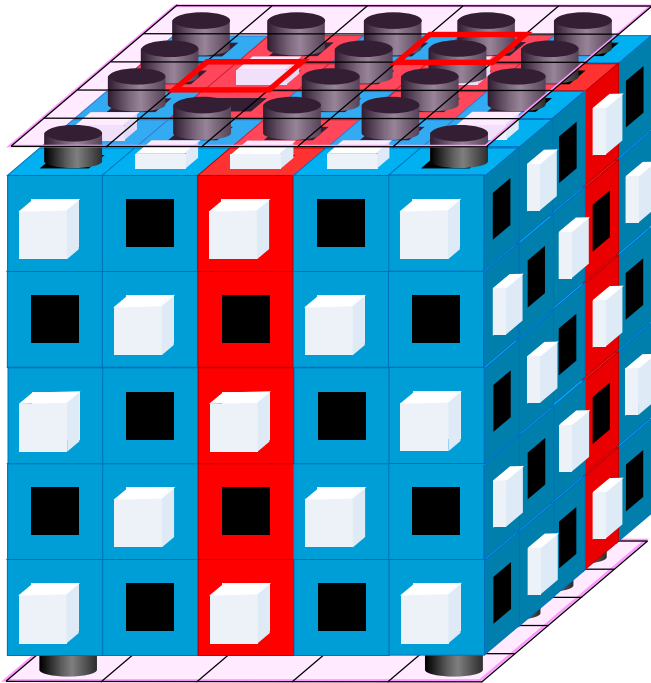


Keys

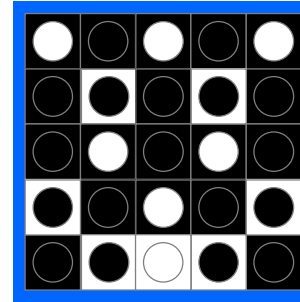
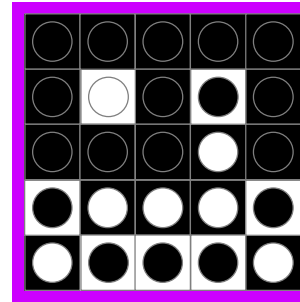
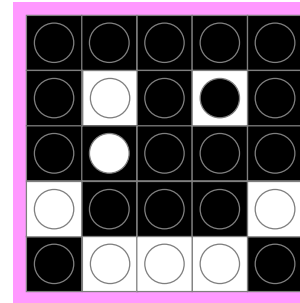
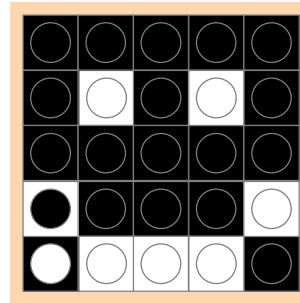
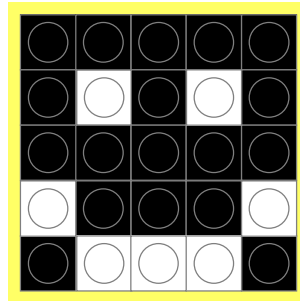


# Machine Matter: Lock & Key

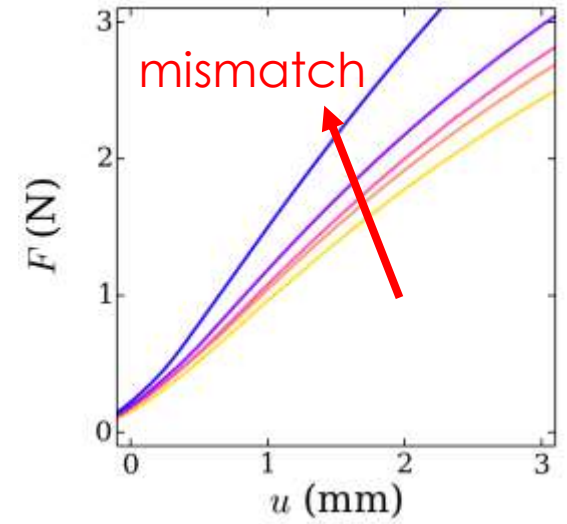
Lock



Keys

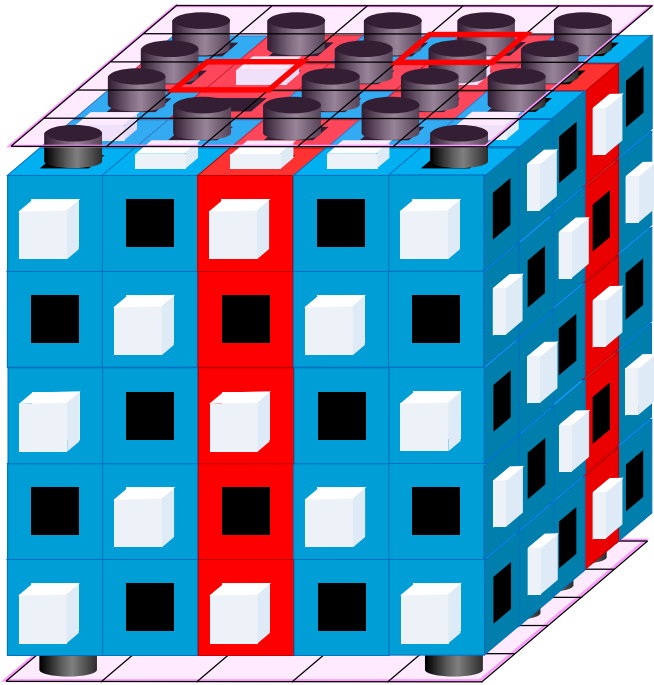


Pattern Analysis

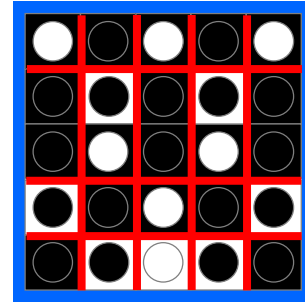
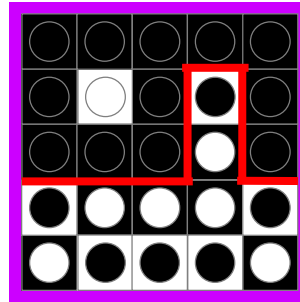
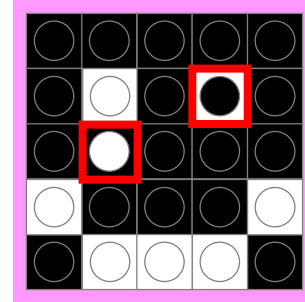
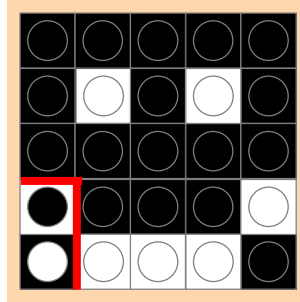
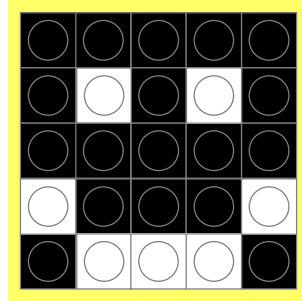


# Machine Matter: Lock & Key

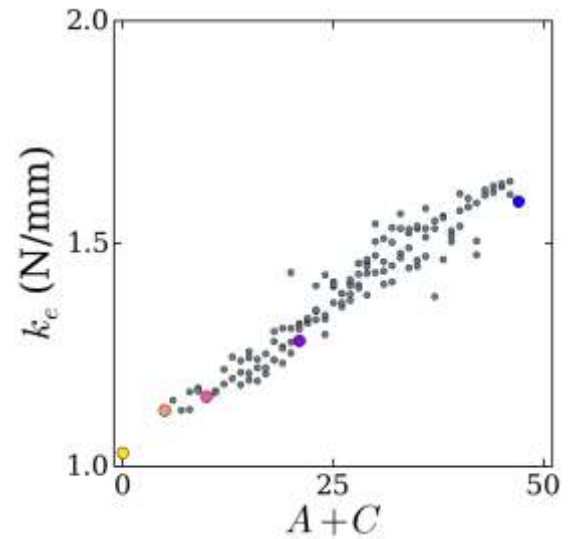
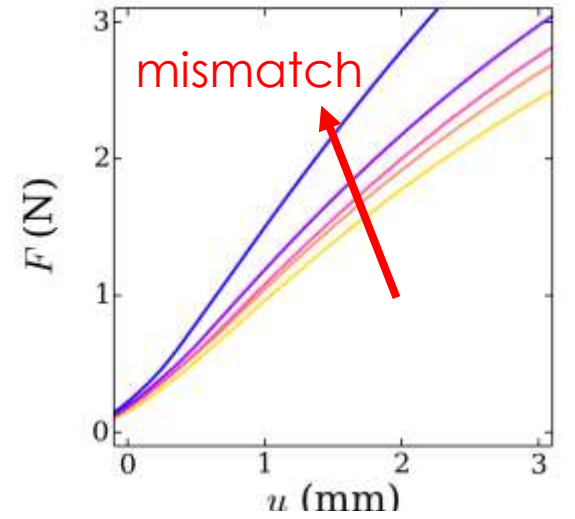
Lock



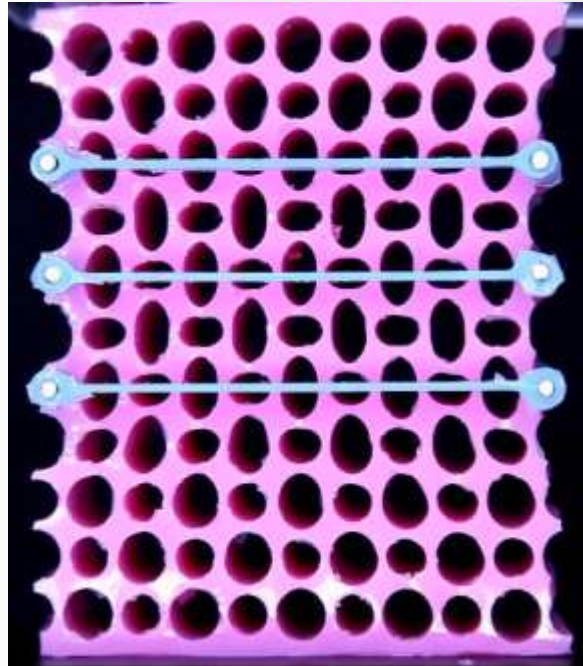
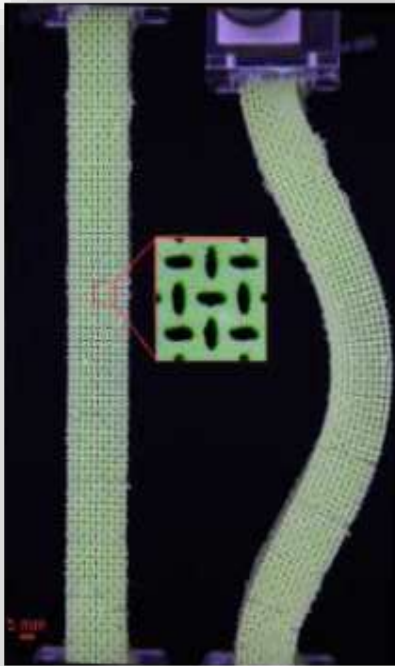
Keys



Pattern Analysis



# From Flexible Mechanical Metamaterials to Machine Materials



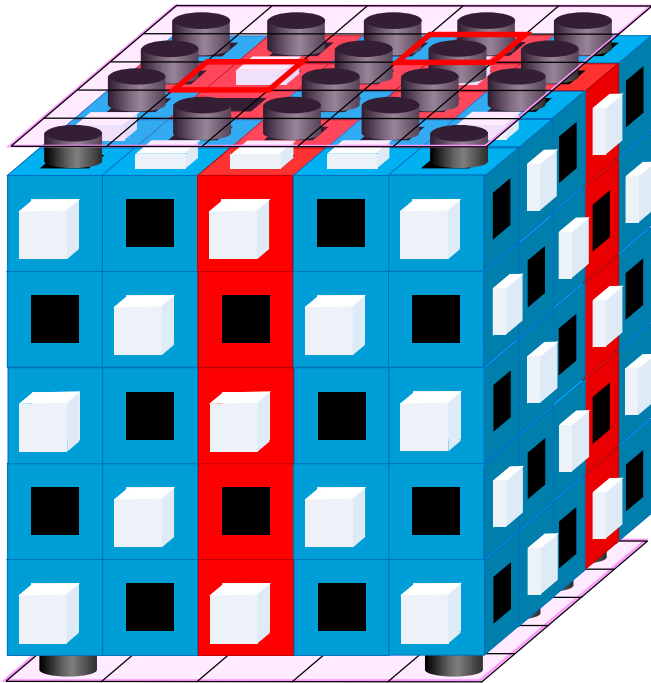
Thanks to B. Florijn, L. Lubbers, K. de Reus & M. van Hecke (Leiden & AMOLF)  
J. Overvelde & K. Bertoldi (Harvard), E. Teomy & Y. Shokef (Tel-Aviv)



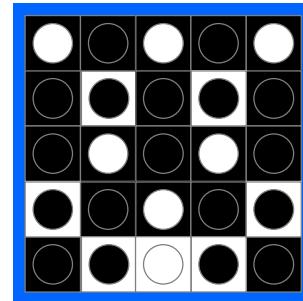
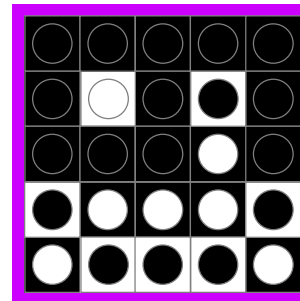
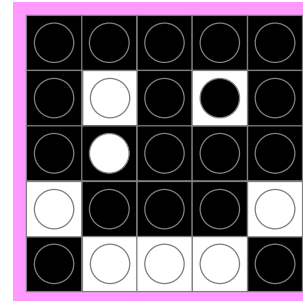
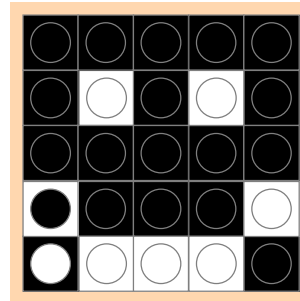
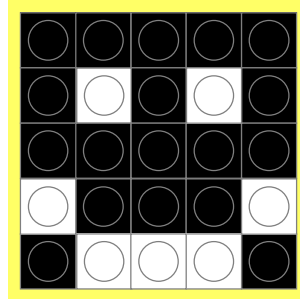


# Machine Matter: Lock & Key

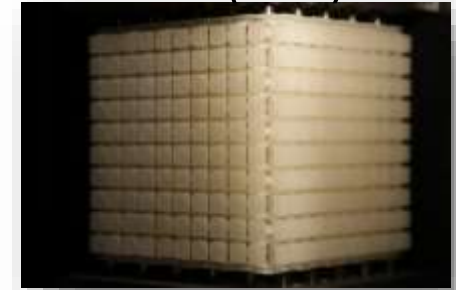
## SmiLock



## Keys



## How to 3D print? SLS (TPU)



## Polyjet (Tango Black)

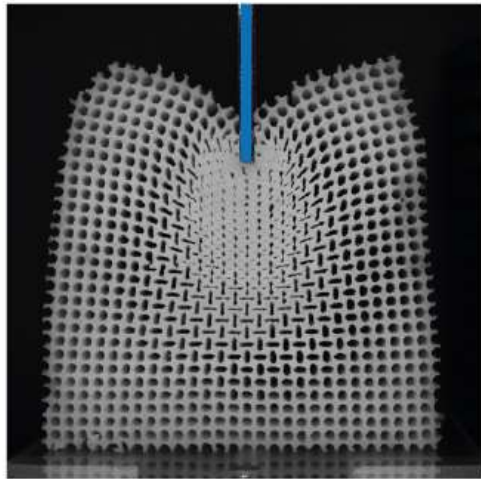
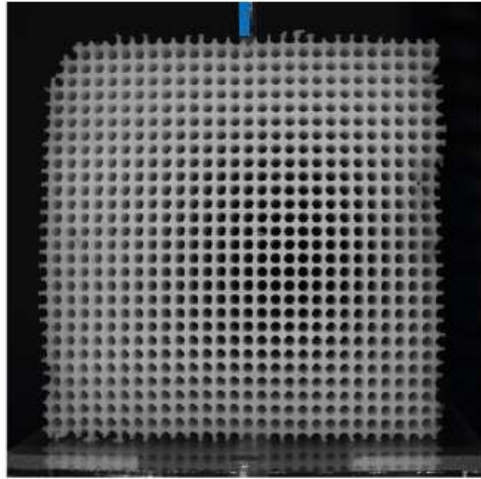


## FDM + Casting (Silicone)

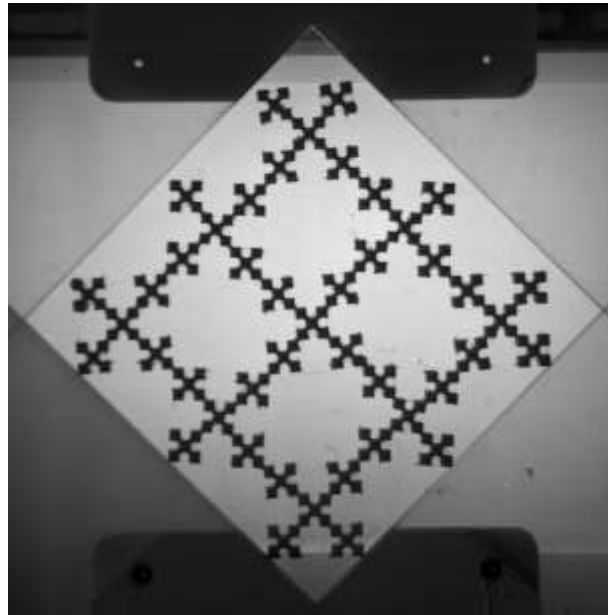


# Outlook

## Inhomogeneities



## Vacancies



## Non-reciprocity

