

# Computational Neuroscience: Neuronal Dynamics of Cognition



## Neuronal Populations

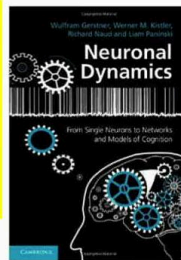
Wulfram Gerstner

EPFL, Lausanne, Switzerland

**Reading:**  
**NEURONAL DYNAMICS**

- Ch. 12.1 – 12.4.3  
(except Section 12.3.7)

Cambridge Univ. Press



### 1. Population activity

- definition and aims

### 2. Cortical Populations

- columns and receptive fields

### 3. Connectivity

- cortical connectivity
- model connectivity schemes

### 4. Mean-field argument

- input to one neuron

### 5. Stationary mean-field

- asynchronous state: predict activity

### 6. Random Networks

- Balanced state



Search MOOC

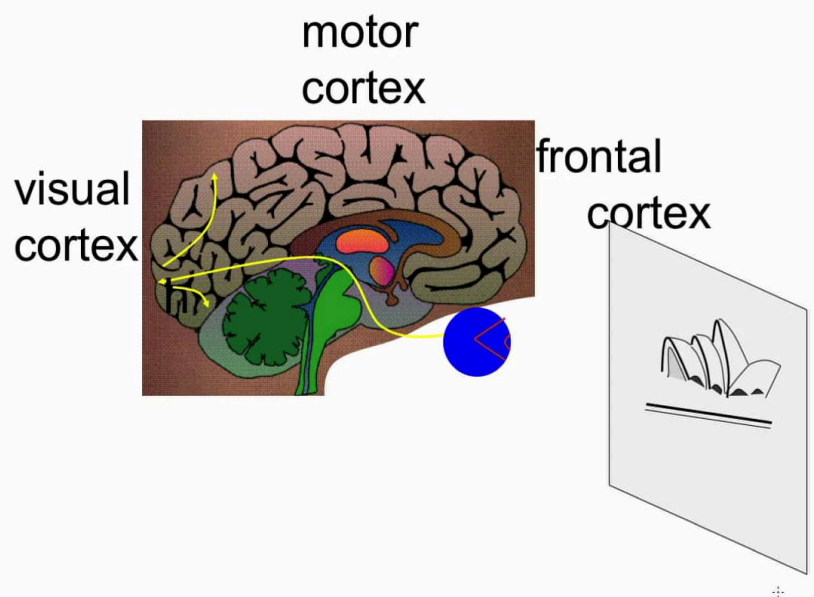


Video





# 1. review: the brain



Welcome to the class, computational neuroscience: neuronal dynamics of cognition. The brain is this fascinating material that we have in our head, it's organized in different areas suppose you watch a movie. So information would enter through the eyes. Go to the back of the head in an area that's called visual cortex, and from there it was spread out to other areas. Now this is a course description of the brain.

Notes

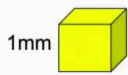
Summary



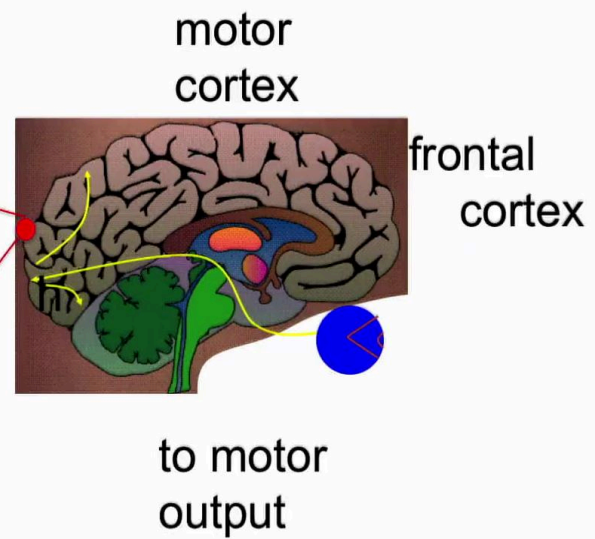
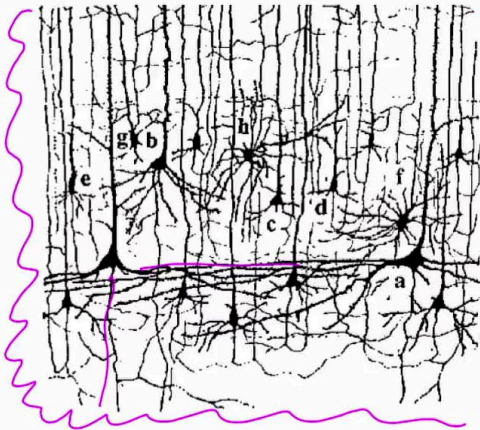
0m 05s



# 1. review: the brain



10 000 neurons  
3 km of wire



You can also zoom in. If you zoom in and put a tiny bit of brain material under microscope, you would see a highly organized and highly complicated network of cells, and these cells have these long wire like extensions. So in each cubic millimeter, you would have about 10,000 neurons or more. And if you just put all these wires together, we would have three kilometers of wire. So it's a densely connected network of neurons, a dense network of cells, and the neural network. And if I have 10,000 neurons in a cubic millimeter you can imagine that they have lots of neurons billions of neurons tend to the 10 neurons in the whole brain. This is a lot.

Notes

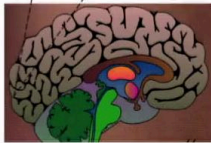
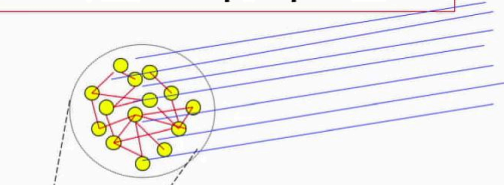
Summary



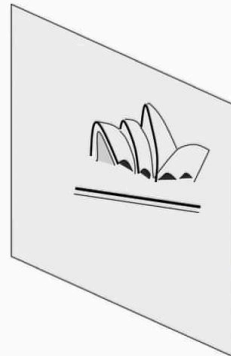


# 1. Population activity, definition

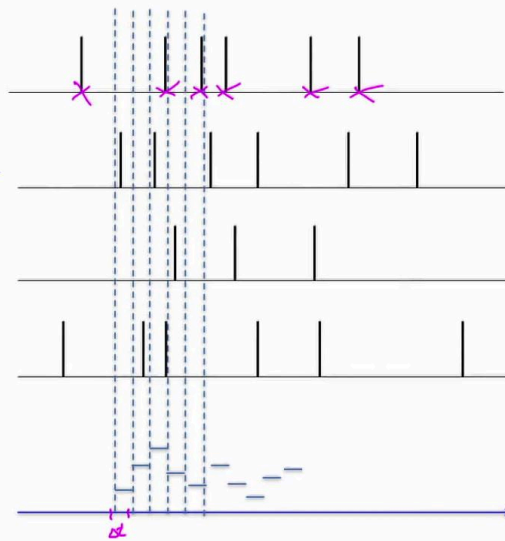
population of neurons  
with similar properties



Brain



stim



neuron 1

neuron 2

Neuron  $K$

time

Now, experimentalists nowadays are able to record from many neurons in parallel. So suppose resuming on the legal network and in this network, you would be able to record, many many neurons, then you would see the activity of these neurons you would see these short electrical pulses. So the first neuron would set out spike here, another spike here another spike here, and so forth, as a function of time. The second neuron would send out in spikes. The third neuron would send out the spikes and so forth. And this is a lot of data. Now one way to analyze this data is you define a very short time window,  $\Delta t$ . And then you just count the number of spikes vertically. Three spikes or one spike or five spikes. And so as a function of time. You see these different levels of activity.

Notes

Summary



1m 13s



# 1. Population activity: definition

population activity - rate defined by population average

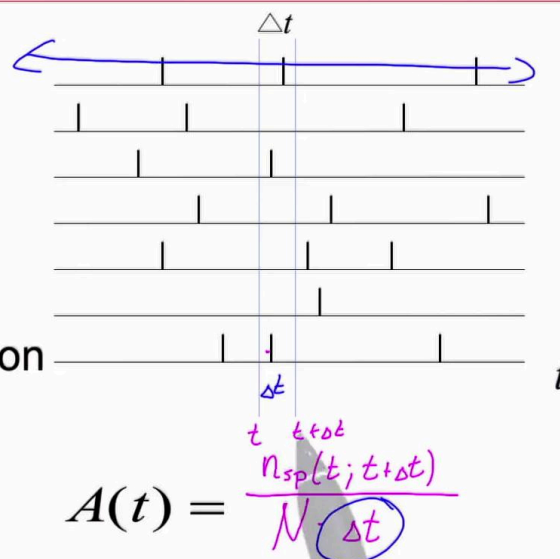
units?  $\frac{1}{\text{time}}$  ; Hz

invariances?

Time scale/averaging?

$\Delta t \approx 1 \text{ ms}$

population  
activity



So formally we count the spikes in this short time window  $\Delta t$ . So I count the number of spikes in spikes between time  $t$ . In the time  $t$  plus  $\Delta t$  spikes of  $T$  plus  $\Delta t$ . And then I normalize. I normalize by the total number of neurons, suppose I've in neurons in total. From each  $i$  record. And then I also normalize by the  $\Delta t$ . So let's, let's look at this quantity, this quantity has units of one over time. Say units of hertz, has the same units as the fine rate. And in fact, it is a fine rate, or whether, in contrast to a single neuron firing rate, where you will do some tempo averaging over many spikes spike count and divided over long time here its spatial averaging. It's a spike count across different neurons, and then you can choose a very short time scale  $\Delta t$ . So the timescale this short  $\Delta t$ , you can for example take one milliseconds, two milliseconds as a timestamp. And therefore, in each little time step,  $\Delta t$   $T$  activity can be different. So you have your record neuronal activity with a high tempo precision. Now, one advantage of divided by  $\Delta t$  is that you get a number that sort of invariant. So you record with a resolution of one millisecond.

Notes

Summary



2m 08s



# 1. Population activity: definition

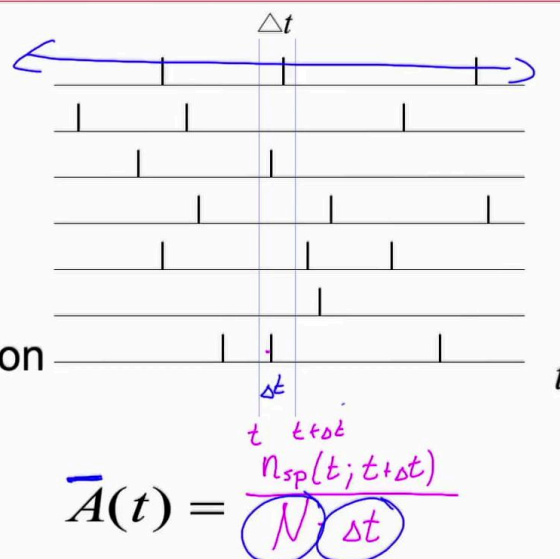
population activity - rate defined by population average

units?  $\frac{1}{\text{time}}$  ; Hz

invariances?  $\Delta t$   
 $N$

Time scale/averaging?  $\Delta t \approx 1 \text{ ms}$

population activity



Your colleague records with a resolution of five milliseconds. If both of you divide by delta t, then you get roughly the same numbers. To be in variance with respect to this notion, delta t. Now, suppose you record from a population of, 100 neurons and you get in this time step delta t, you get a fine rate of 25 Hz, your colleague records from 15 neurons but exactly the same difference in the same area. You also get 50 Hz because you divide by the number of neurons that you have requested from. So, this is a useful quantity, it's the population activity. It's a fine rate defined by a population average. And we can also say it's a bar, because we still average over small time step delta t. But as I said delta t is maybe one millisecond or two milliseconds or 3 million things. So it's a really short. It's not averaged over 500 milliseconds or something.

Notes

Summary

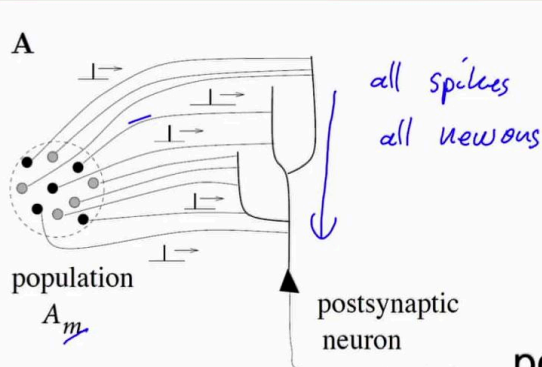


3m 47s



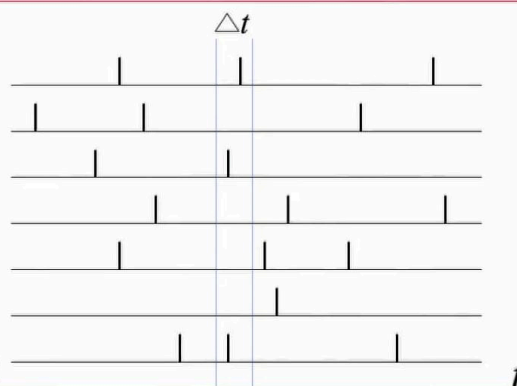
# 1. Population activity: definition

population activity - rate defined by population average



'natural readout'

population activity



$$\bar{A}(t) = \frac{n(t; t + \Delta t)}{N \Delta t}$$

$$\bar{A}(t) = \lim_{\Delta t \rightarrow 0} \bar{A}(t) = \frac{1}{N} \sum_i \sum_f \delta(t - t_i^f) \quad \text{all spikes all neurons}$$

Image: Neuronal Dynamics,  
Gerstner et al.,  
Cambridge Univ. Press (2014),

So, this quantity, a bar of  $T$  averaged over the population of neurons is the population activity or population rate, and I would argue it's a very natural quantity, in the following sense. Think of a new year and that receives input from that population, say population number  $M$  population with index  $M$ . It receives many spikes. And this neuron, sits here and gets the spike input from all these different neurons. So essentially the input to this neuron is an average of all spikes on neurons. All those neurons that make signals that send signals that make connections to these receiving neuron, the neurons behind the synapse, after the synapse, the post synaptic neuron, and the receiving neuron. So, we still have this little  $\Delta t$  in here, and we can get more independent from  $\Delta t$ , if we say the activity is the limit of this a bar of  $T$  that have defined here in the limit  $\Delta t$  to zero. And then this would just be can make it really small, this will just be the sum of all spikes, and for those who are familiar with his notation, this is the direct delta function or delta distribution by some here, over all new neurons and all spikes, so this is the sum of all spikes and all neurons, and I still have the one over  $N$ .

Notes

Summary

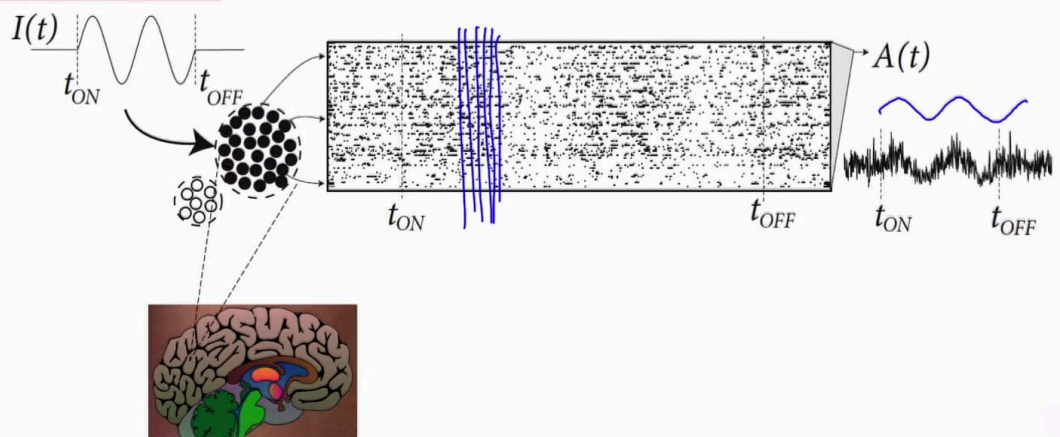


4m 49s



# 1. Population activity: example

population of neurons  
with similar properties



Brain

Image: *Neuronal Dynamics*,  
Gerstner et al.,  
Cambridge Univ. Press (2014),

So let's just consider it an example here, a population of near and somewhere into brain, suppose there's visual stimulation, you're watching a movie. So the input is going up and down, and as a result of this, these neurons fire, and you see all these spike trains. Now if we do this spatial averaging in some small time steps. Some of the neurons divided by  $\Delta t$  divided by the number of neurons, we get this population activity and this population activity is time dependent. So, we have a temporal of fine temporal resolution of this population activity or population, firing rate.

Notes

Summary

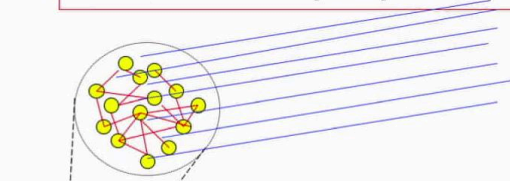


6m 21s



# 1. Scales of neuronal processes

population of neurons  
with similar properties



Brain

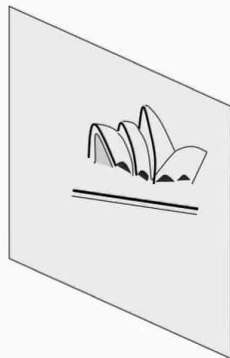
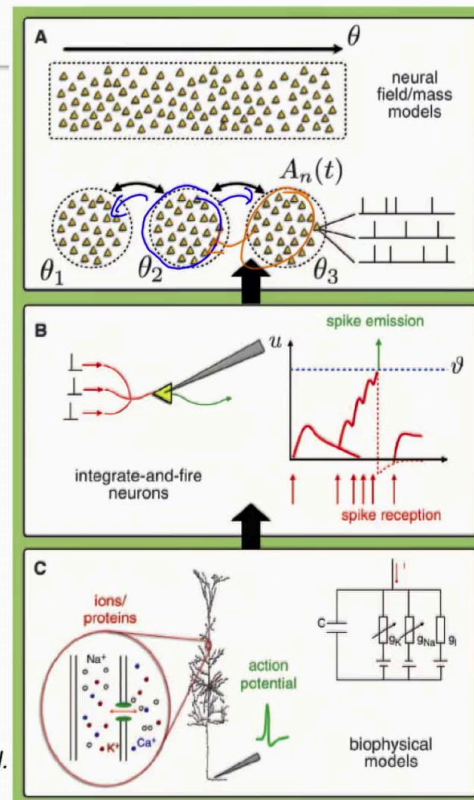


Image: Gerstner et al.  
Science (2012),



For now, the aim for today's lecture is the following. We could describe the brain on the level of individual neurons and even on the level of individual neurons we could choose, very detailed models that are called biophysical models or compartmental neurons neuron models, or we could use the description on the level of integrated firing neurons if a spike arrives, it causes response, the responses are added, until total membrane potential reaches a threshold, and the spikes emitted, afterwards we restart. It's still a single neuron description, or we could simplify further and preach the scale to a description by populations. And instead of saying, Well, I have 10,000 neurons, these neurons interactive spikes. I now say, I have one population of neurons, and this new population of neurons index with other populations, and it will receive input from other populations. So the inaction is no longer on the level of spikes, but directly on the level of populations.

Notes

Summary



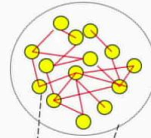
7m 00s



# 1. Population activity

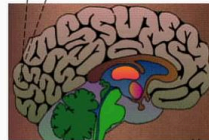


population of neurons  
with similar properties



population activity  
→  $A(t)$

- do populations exist?
- how do they interact?
- can we predict  $A(t)$  ?



To summarize. In this section we have seen that we can define the population activity in a population of neurons, with similar properties. If you want to do a spatial averaging it's nice to have neurons that are somewhat similar, then it makes sense to do this spatial average. But then the question arises. Are there such populations in the brain? Do such populations exist? And if so, can we predict what the activity would be? And how different populations do interact? These are the questions that people address this week. Stay tuned to find out about the mathematical approaches that will enable us to answer these questions. But before we continue. Let's look at the quiz.

Notes

Summary



8m 10s



## Quiz 1, now

The population activity

- ☐ Is a firing rate
- ☐ Is a fast variable on the time scale of milliseconds
- ☐ Is proportional to the number of spikes counted across a population in a short time window
- ☐ Is defined as the number of spikes counted across a population in a short time window

Notes

Summary

9m 00s





## Additional information: Computational Neuroscience



Wulfram Gerstner  
EPFL, Lausanne,  
Switzerland

### Additional links to short MOOC - videos

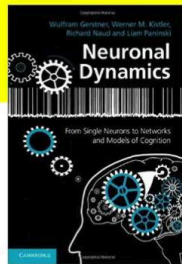
<http://lcn.epfl.ch/~gerstner/NeuronalDynamics-MOOC1.html>

#### - Dirac delta-function in computational neuroscience

<https://www.youtube.com/watch?v=l3hvrX33lZc>

### Background Reading: NEURONAL DYNAMICS

- Ch. 1.3.
- Ch. 12.1



Cambridge Univ. Press

#### - Integrate-and-fire model, a first introduction

<https://www.youtube.com/watch?v=gU9UzFeg8f4>

### Textbook also online:

<http://neurondynamics.epfl.ch/>

Notes

Summary



9m 06s